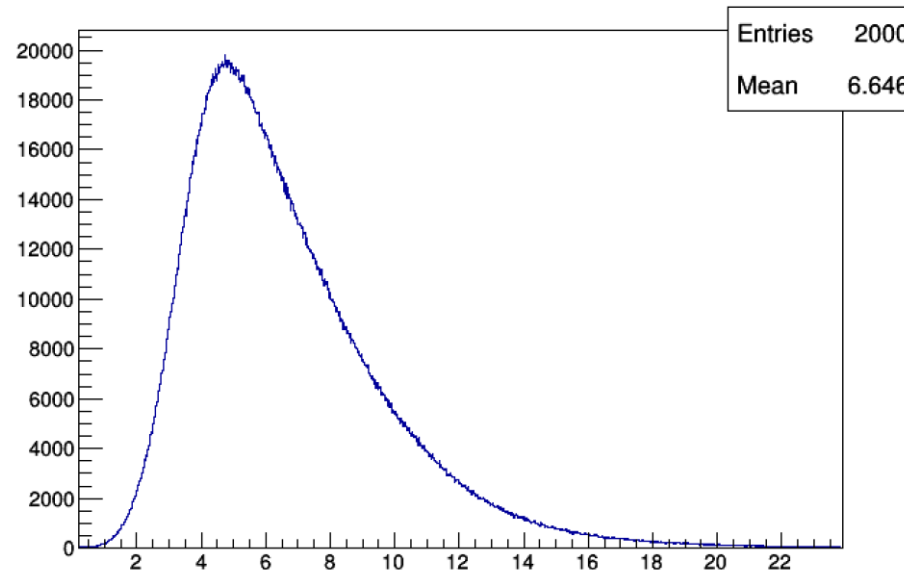


Phase scan analysis (modulated signal)

Logbook: BOA_Logbook_Sept-2018 pages 67-68 ($B_0 = 125, 124, 123, 122$ uT)

Data: T231018_PhaseScanMod_0031.tof -> _0072.tof (skip 51,52)

Ramsey_phase_mod-1000003.dat -> _mod-1000007.dat (skip 5)

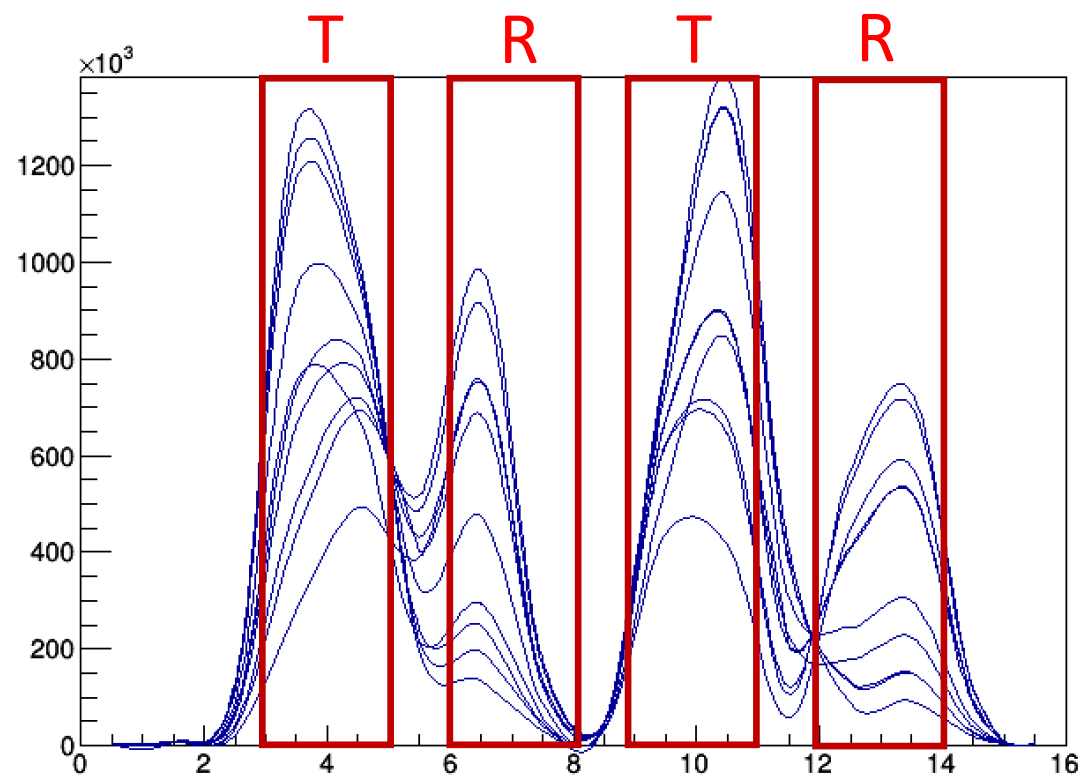
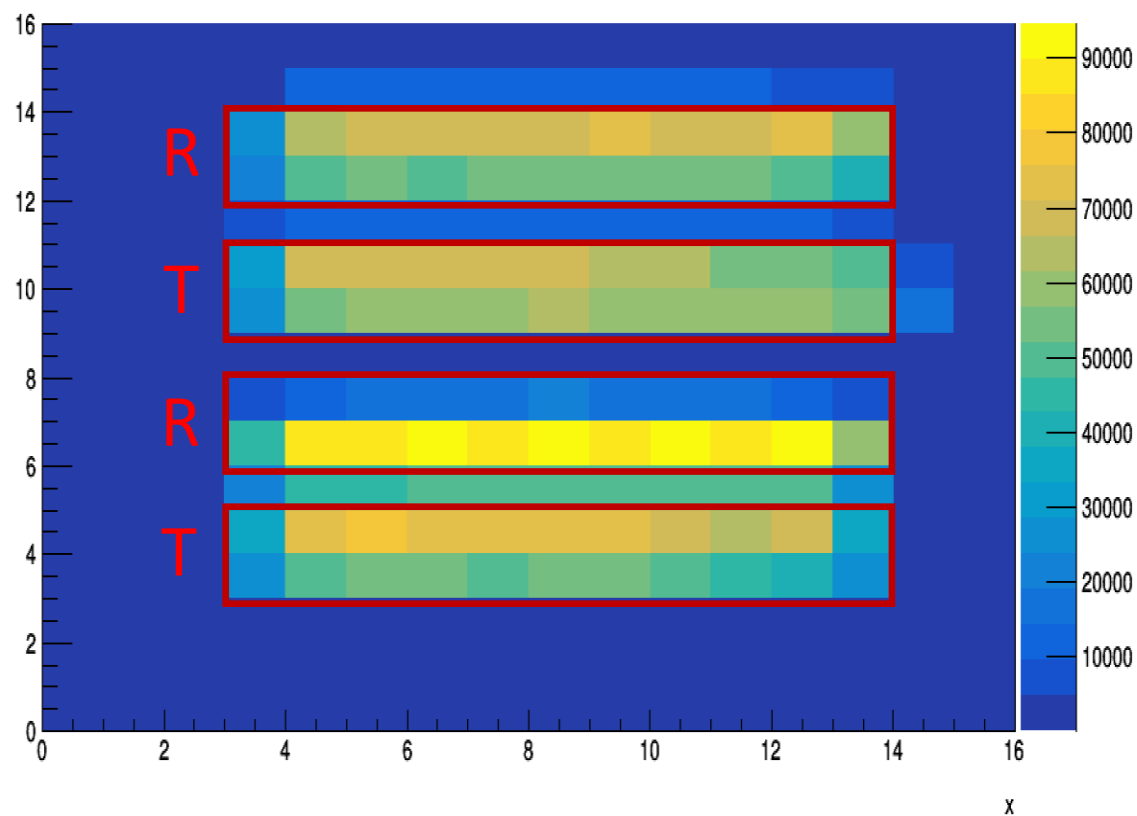


$B_0 = 125 \mu\text{T}$

2D (file 34)

	Bins X	Bins Y
UP ref	4-14	13-14
UP tra	4-14	10-11
DOWN ref	4-14	7-8
DOWN tra	4-14	4-5

$$A = \frac{R - T}{R + T}$$



$$A = \frac{R-T}{R+T}$$

$$\sigma_A^2 = \left(\frac{\delta A}{\delta R} \right)^2 \sigma_R^2 + \left(\frac{\delta A}{\delta T} \right)^2 \sigma_T^2 + 2 \frac{\delta A}{\delta R} \frac{\delta A}{\delta T} \sigma_{RT}$$

$$= \left(\frac{2T}{(R+T)^2} \right)^2 \sigma_R^2 + \left(-\frac{2R}{(R+T)^2} \right)^2 \sigma_T^2 + 2 \frac{\delta A}{\delta R} \frac{\delta A}{\delta T} \sigma_{RT}$$

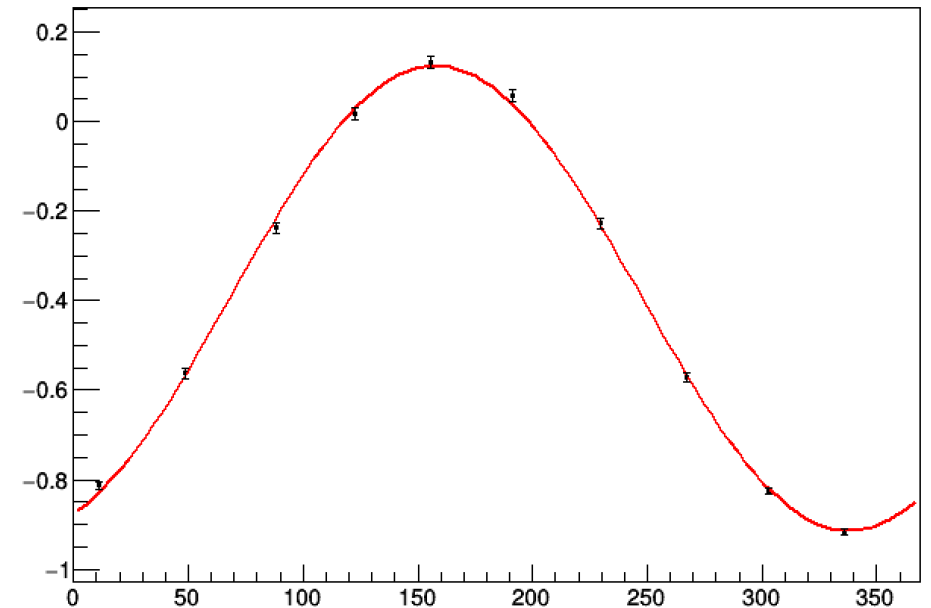
1) Assume

- Poissonian error
- No covariance

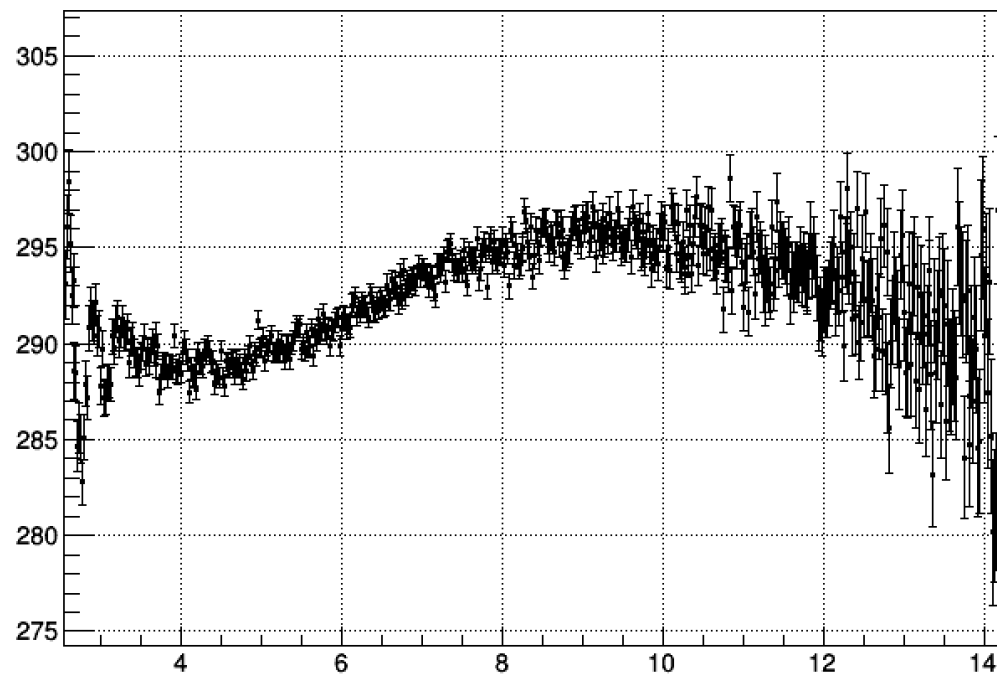
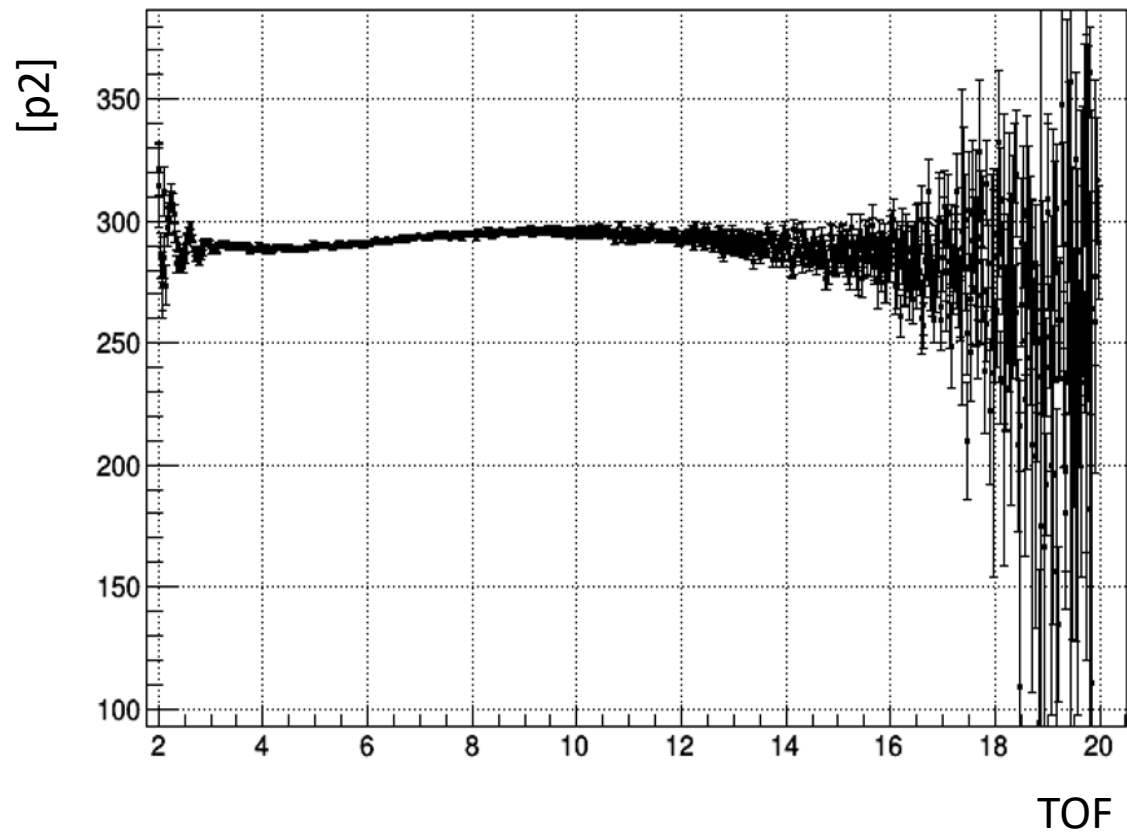
2) For each TOF bin fit asymmetry VS Φ_{SF} :

"[p0]+[p1]*sin(x*π/180.+[p2])"

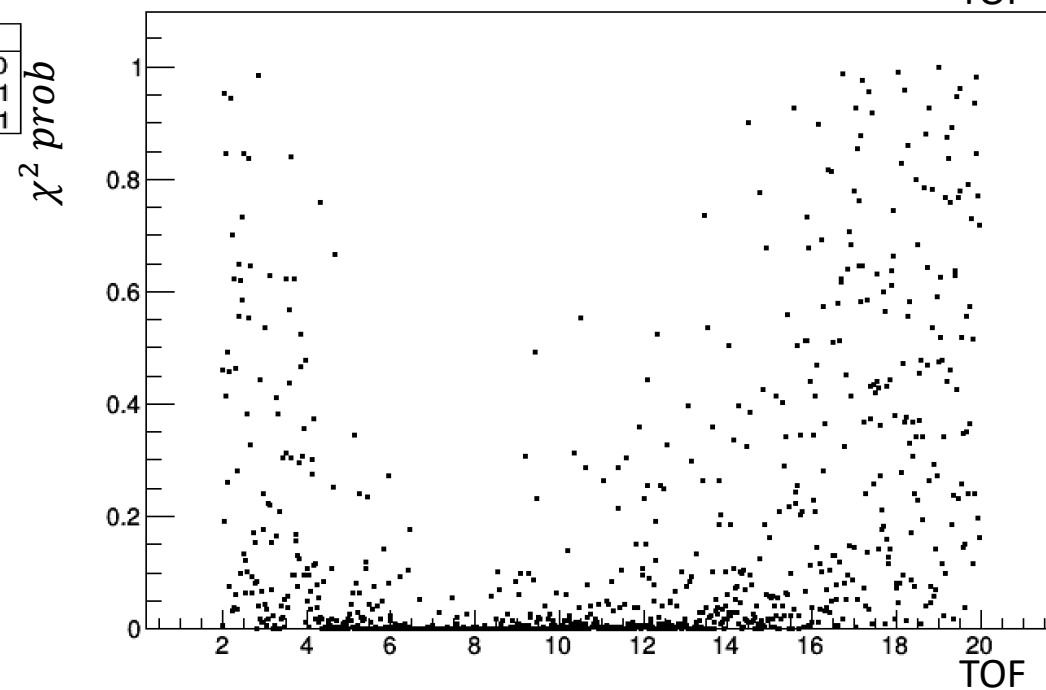
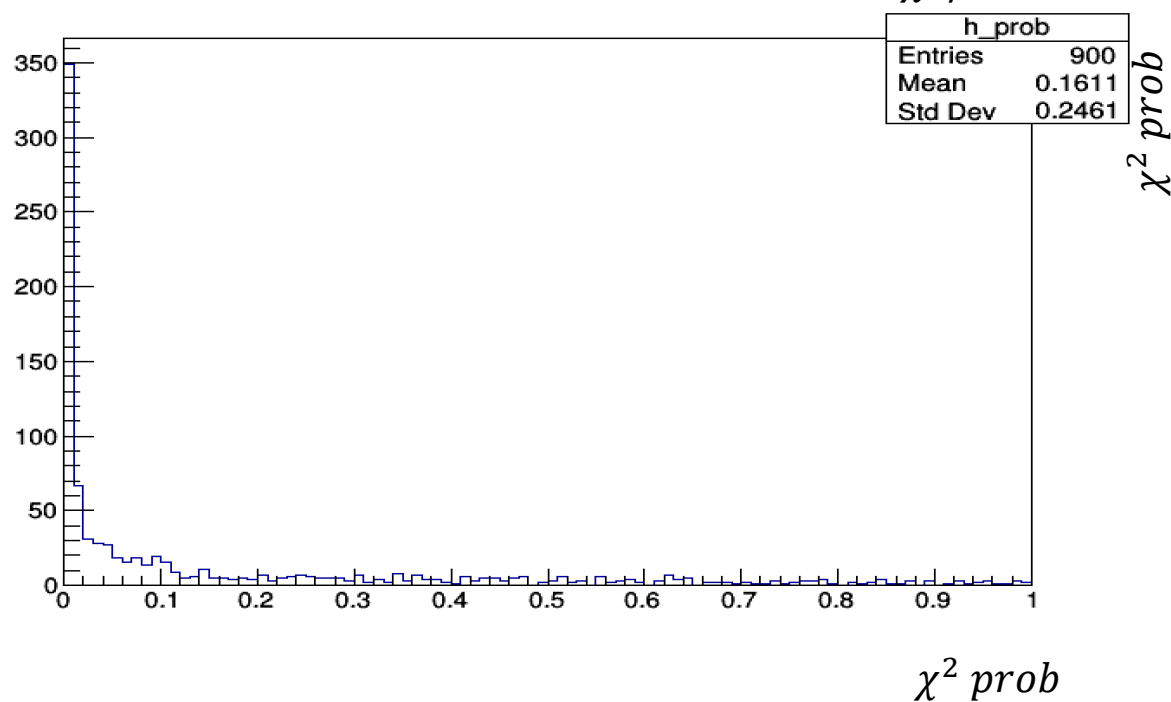
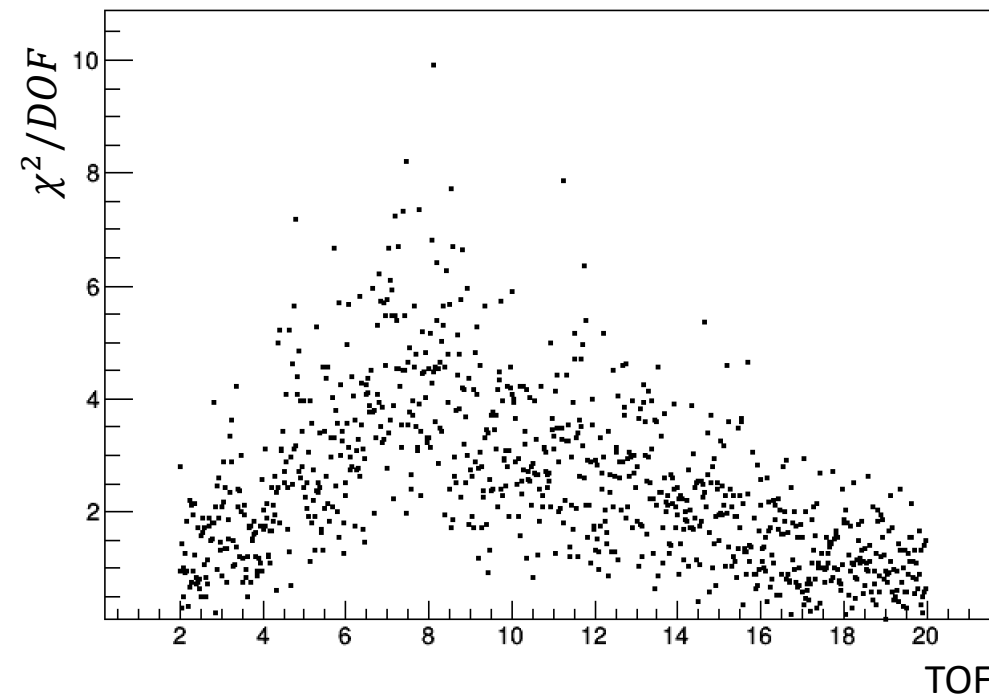
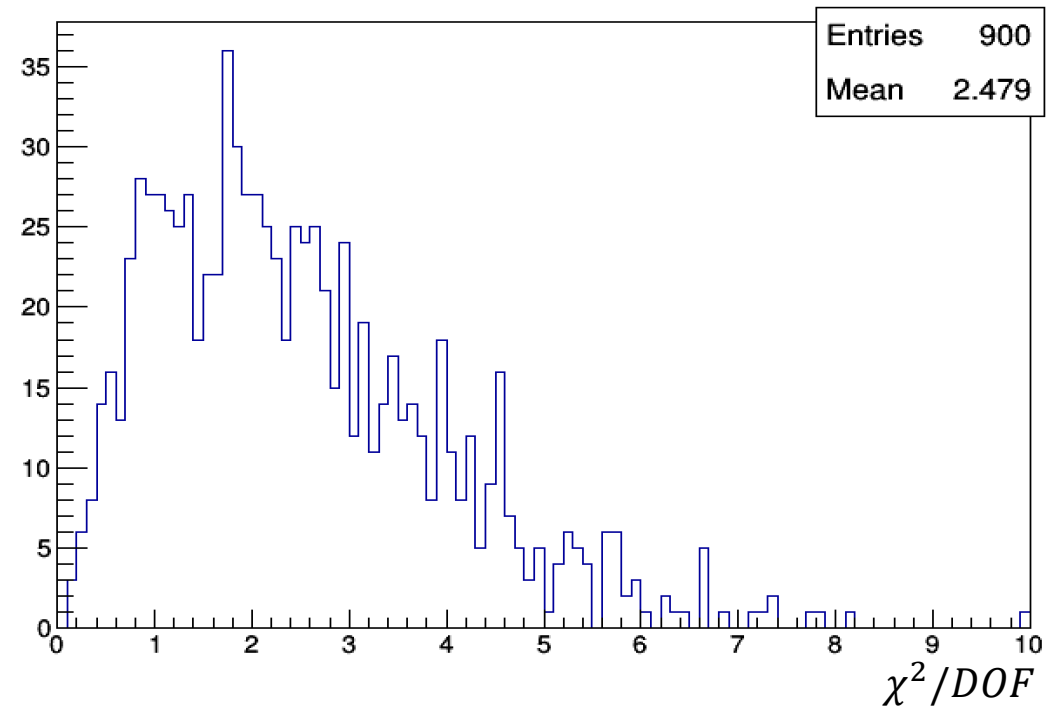
3) Plot [p2]*180./ π vs TOF

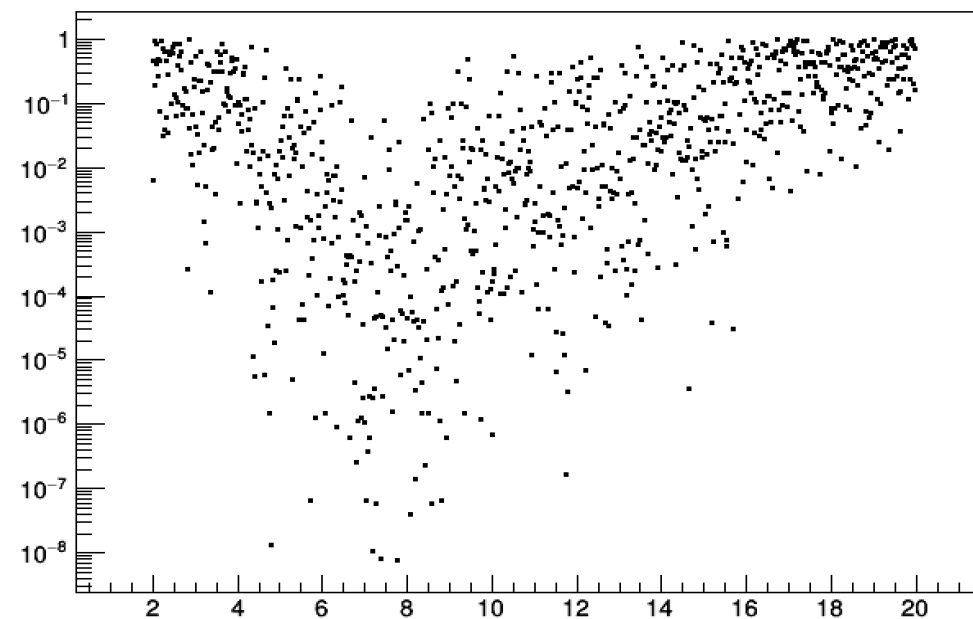
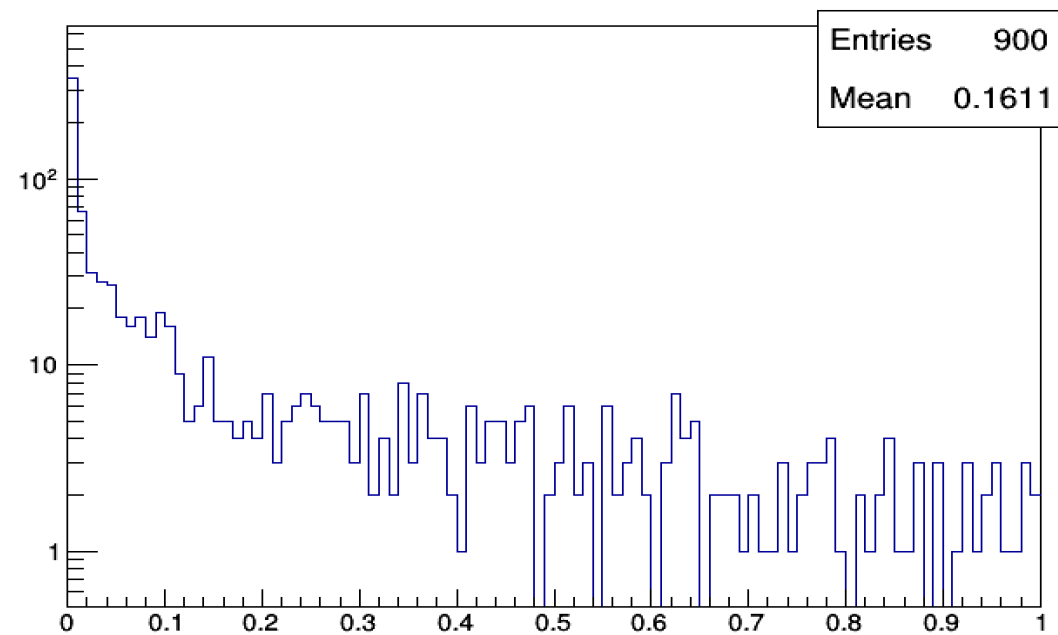


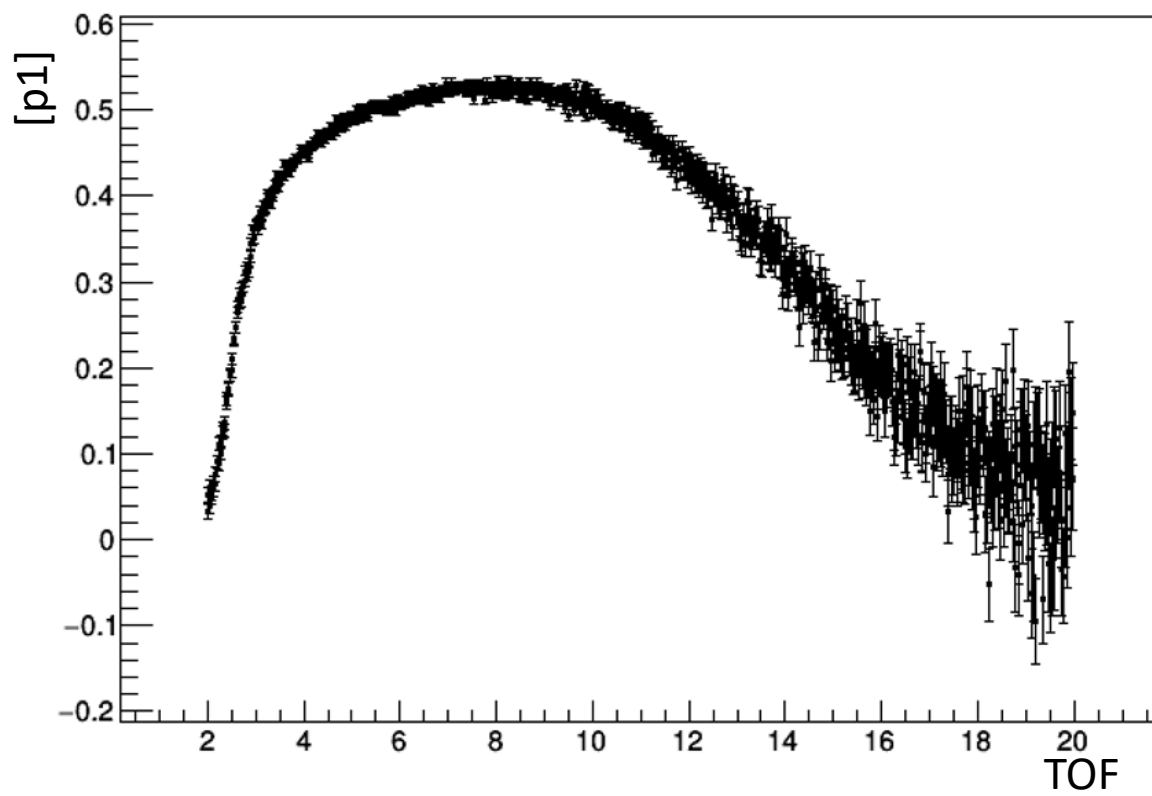
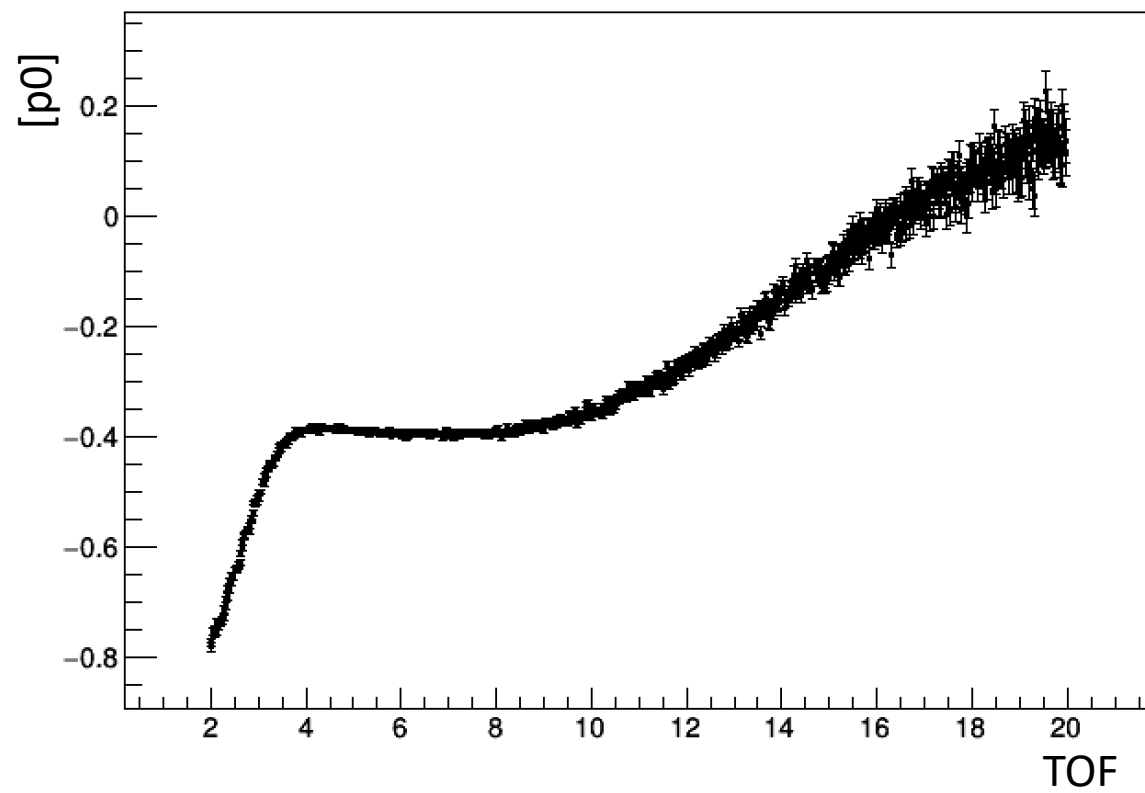
$B_0 = 125 \text{ uT}$ UP beam 900 bins (bin width is 20 μm)



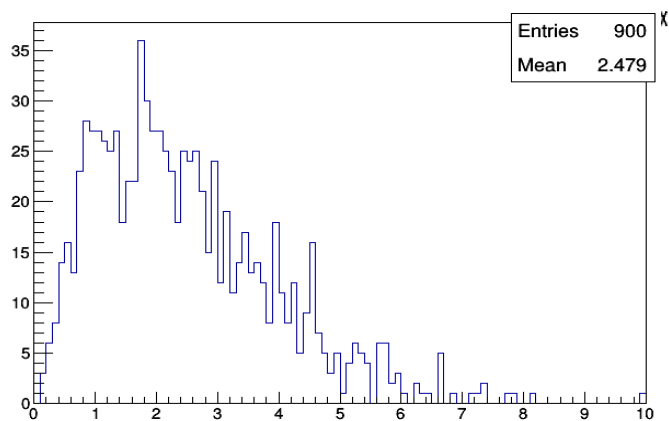
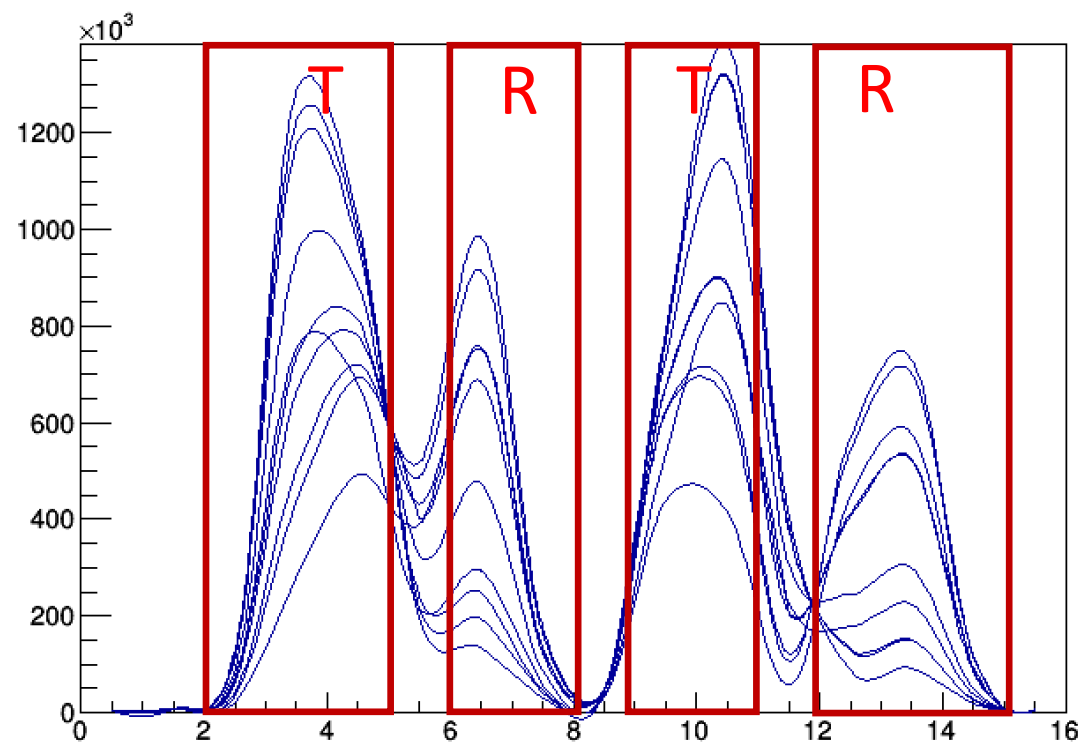
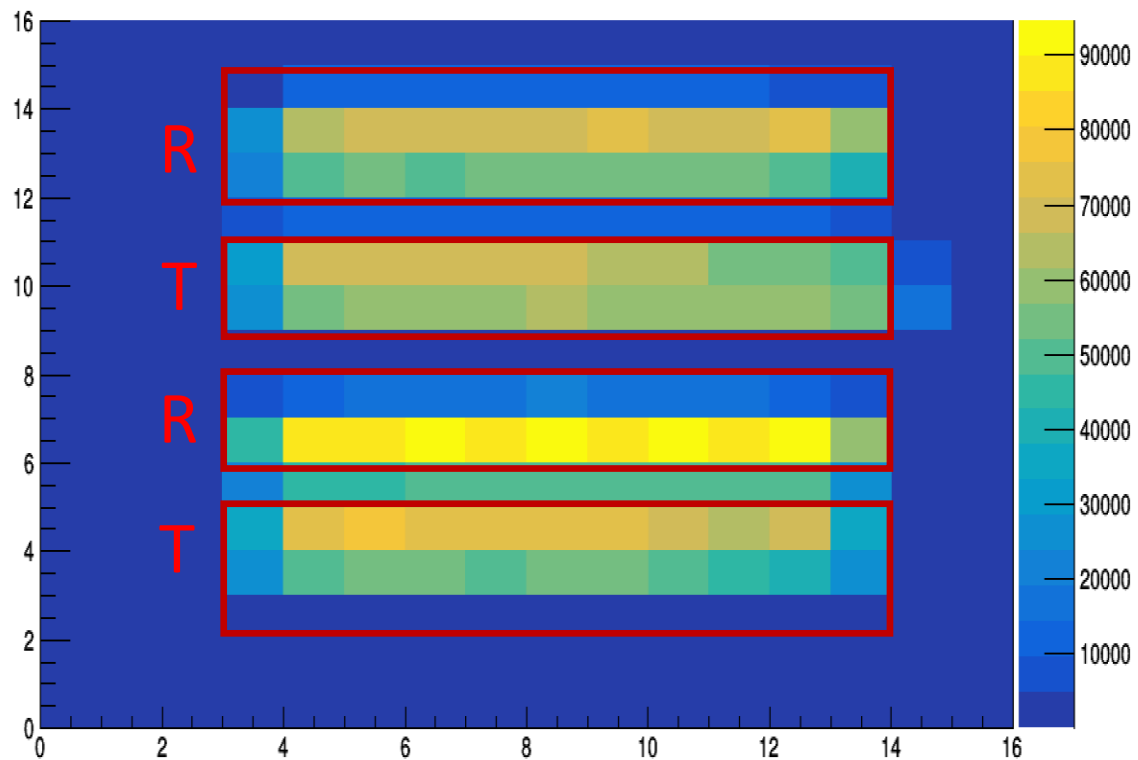
but...



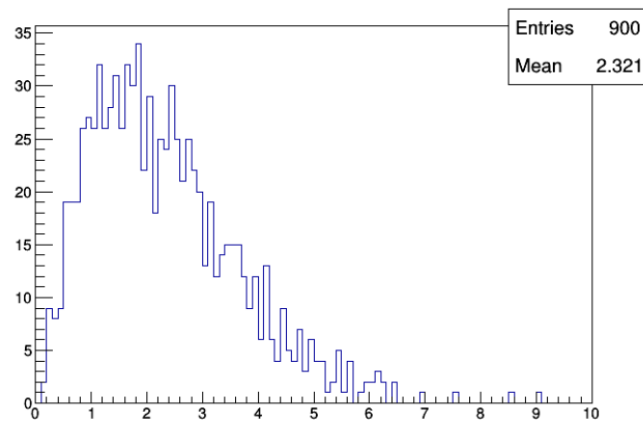




- Increase R_{up} and T_{down} area



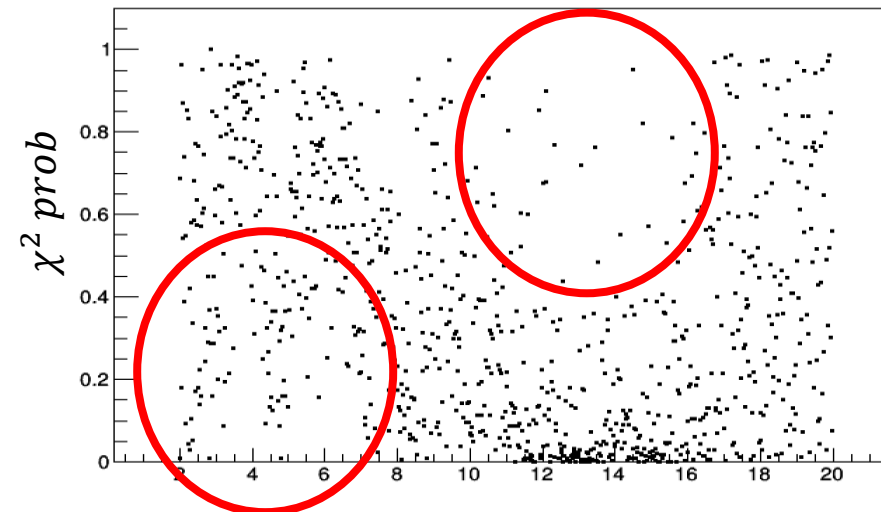
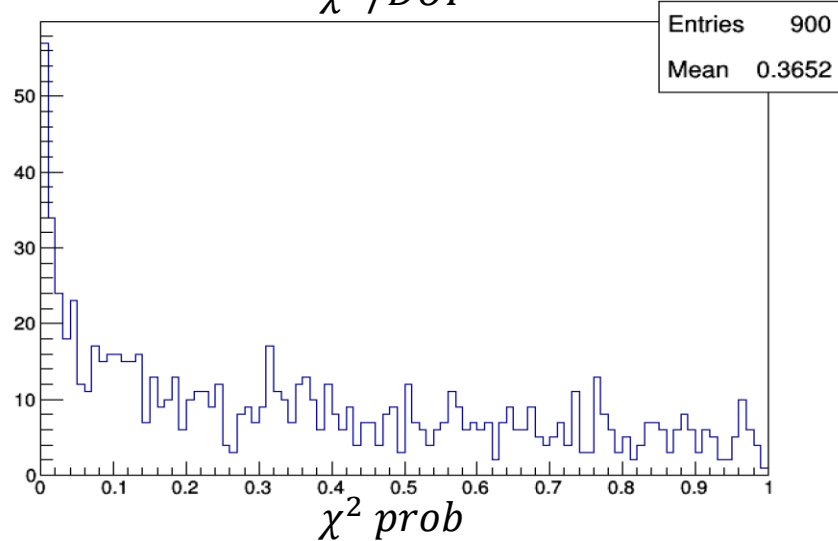
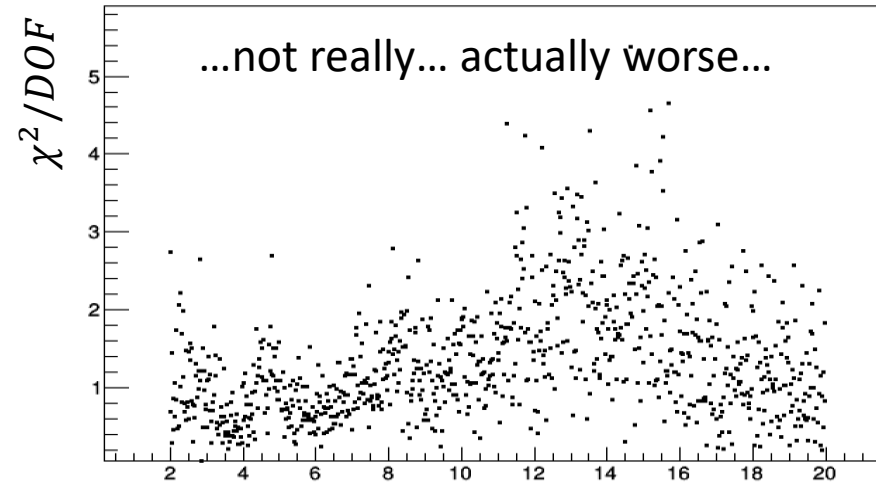
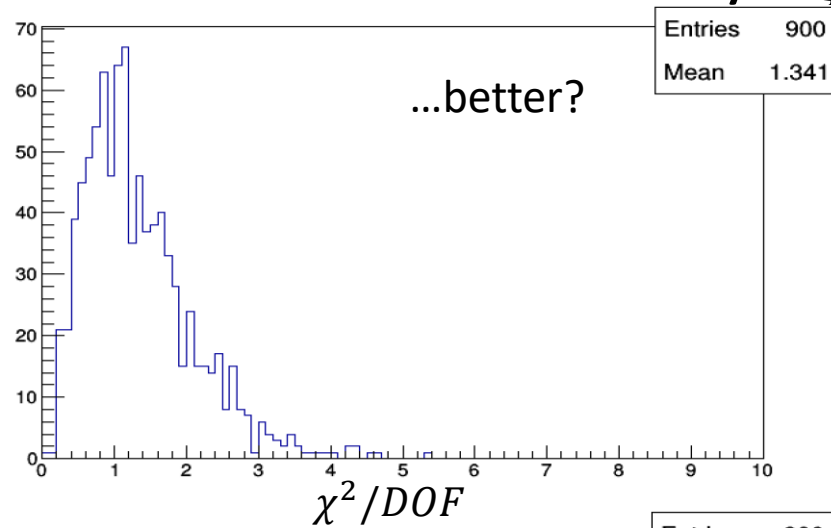
χ^2 / DOF



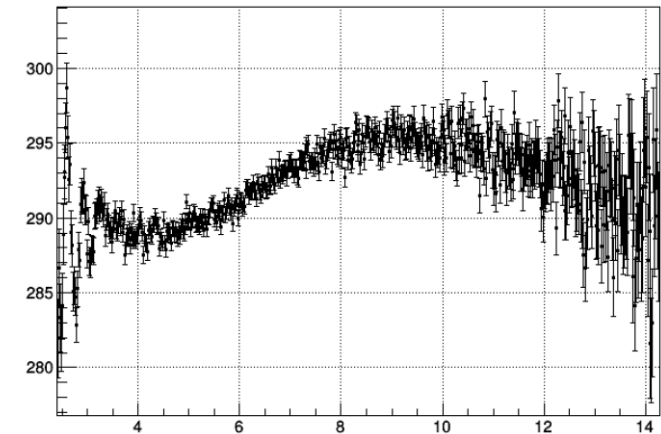
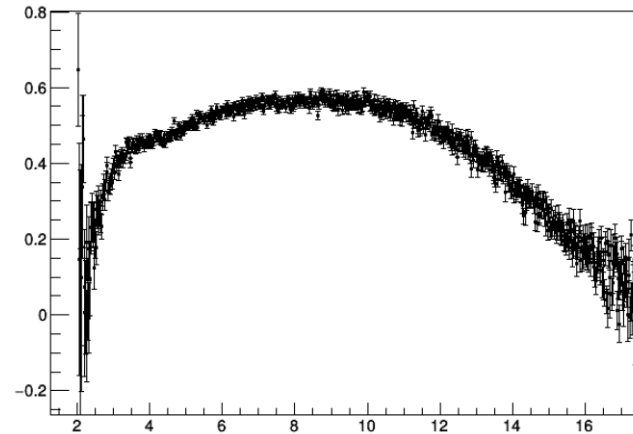
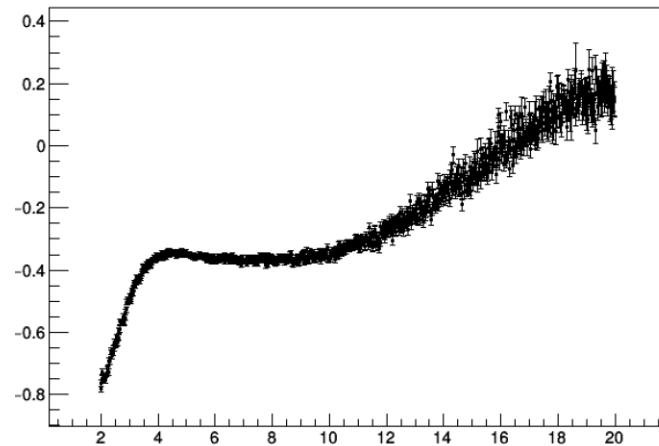
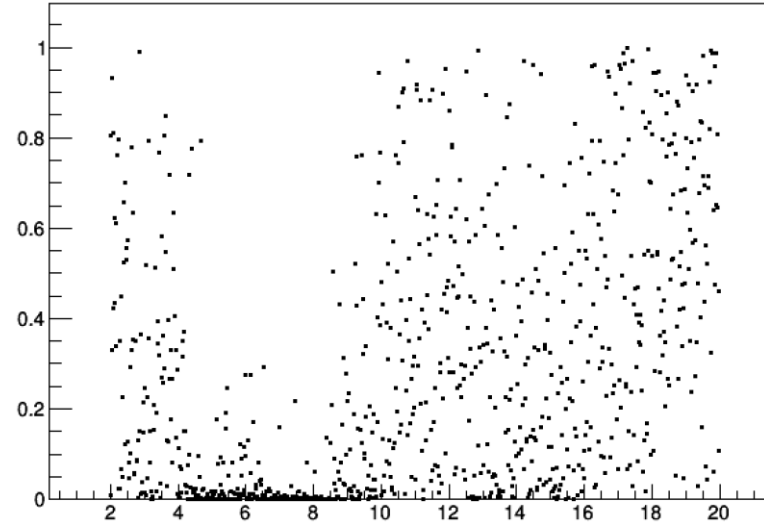
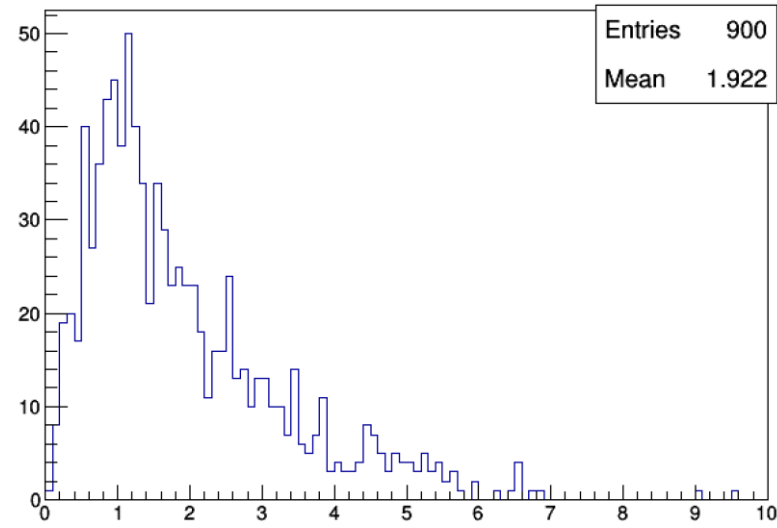
- Introduce Φ_{SF} error : $\sigma_{\Phi_{SF}} = 0.15^\circ$ (observed RMS)

➡ no substantial changes in χ^2/DOF distribution

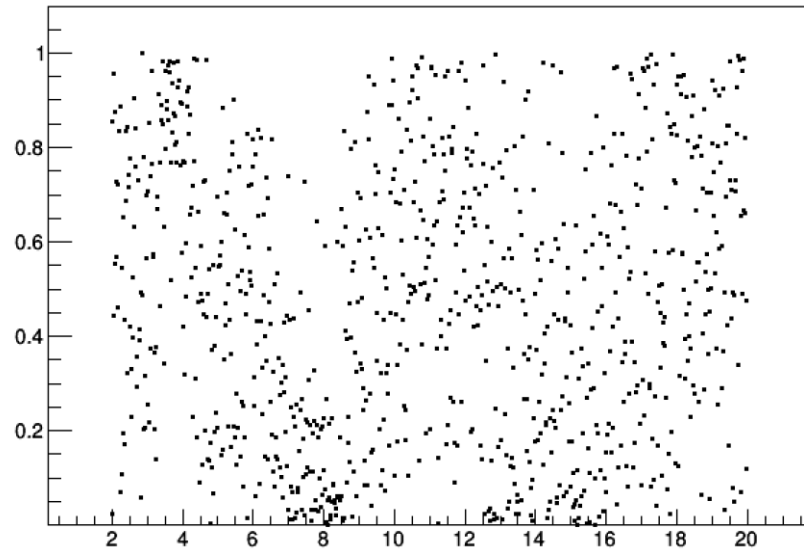
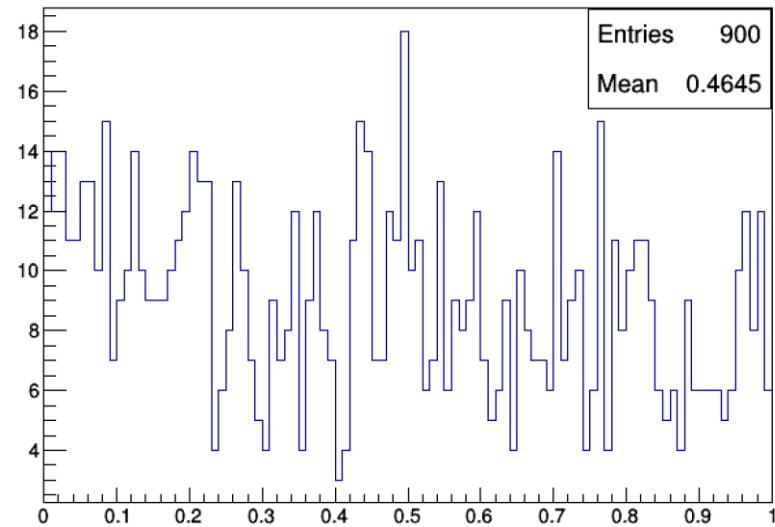
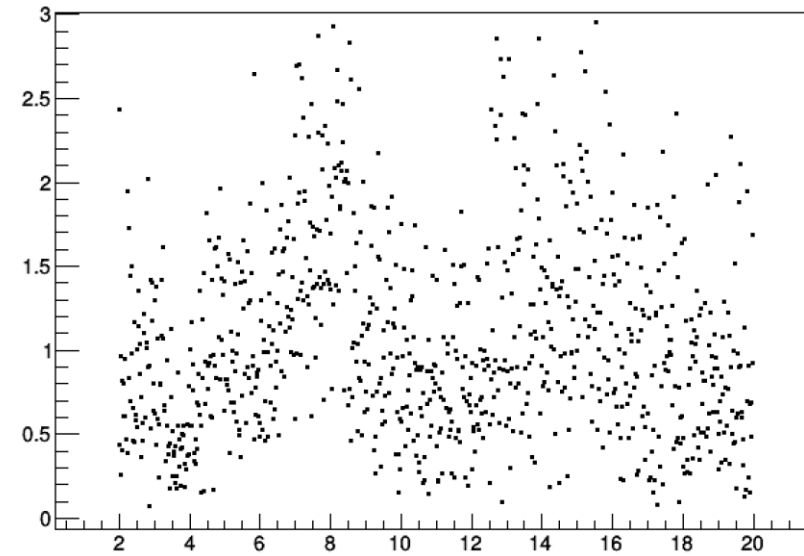
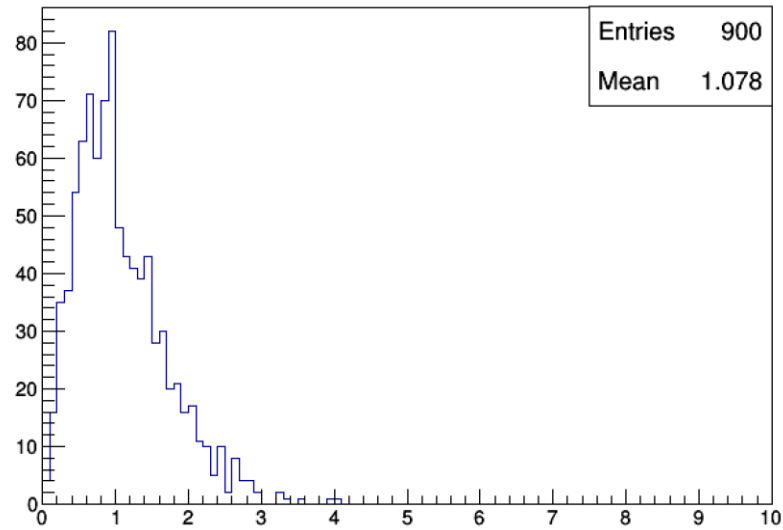
- What if I inflate arbitrarily $\sigma_{\Phi_{SF}}$ (ex. = 3°)?



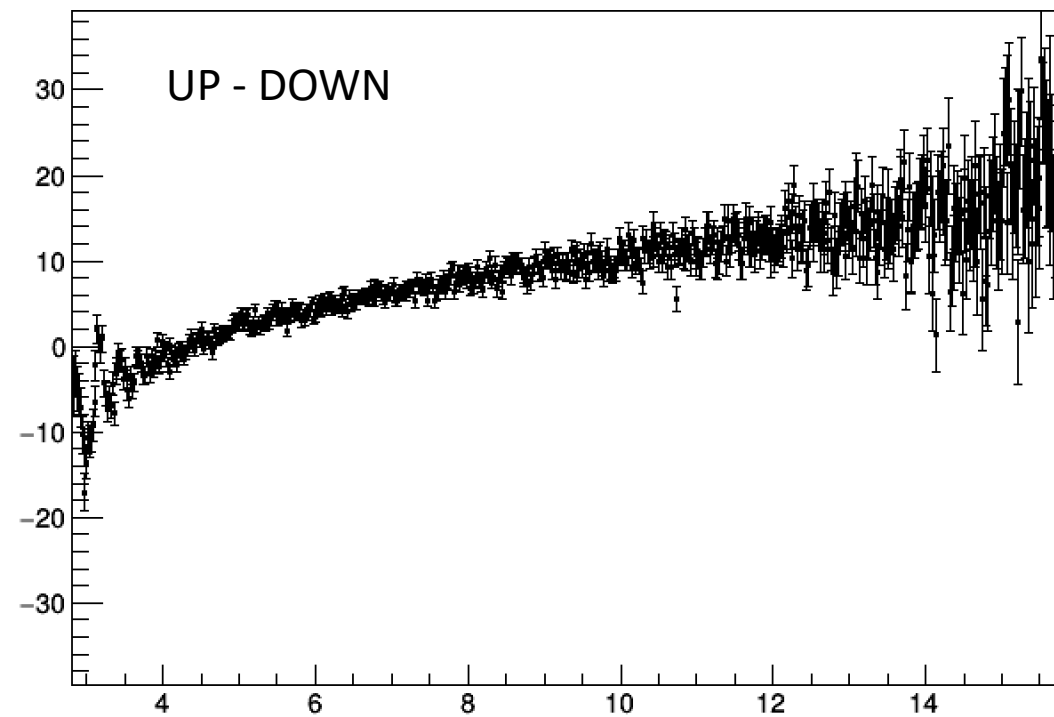
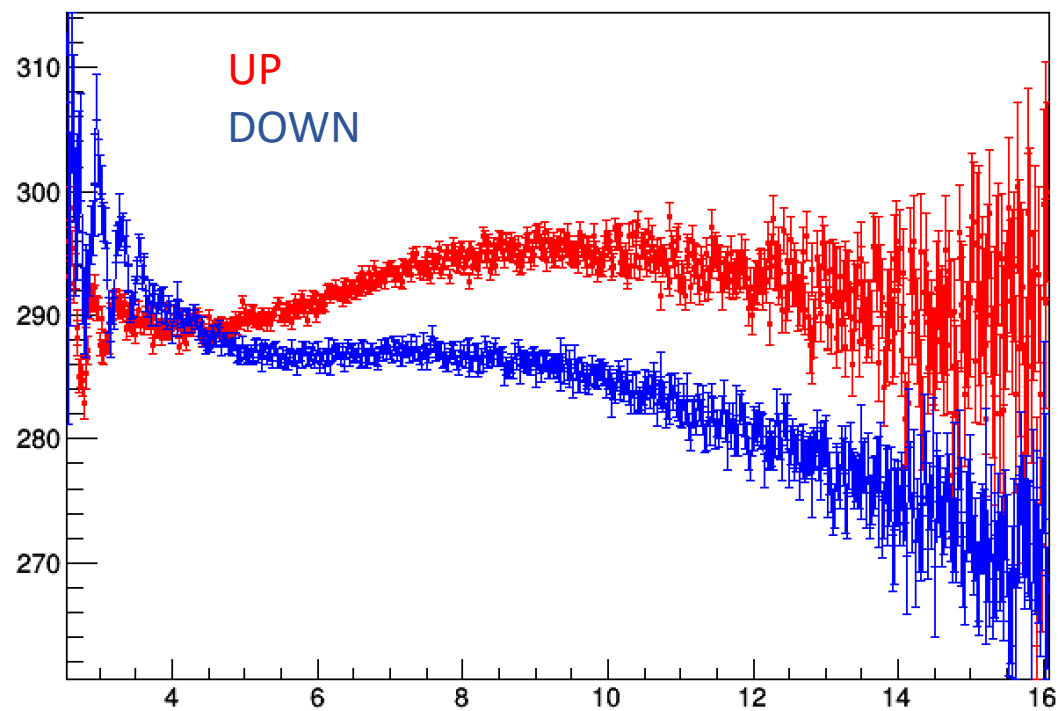
- Fit with $\frac{[p_0] + [p_1] \sin\left(x \cdot \frac{\pi}{180} + [p_2]\right)}{1 + [p_3] \sin\left(x \cdot \frac{\pi}{180} + [p_2]\right)}$



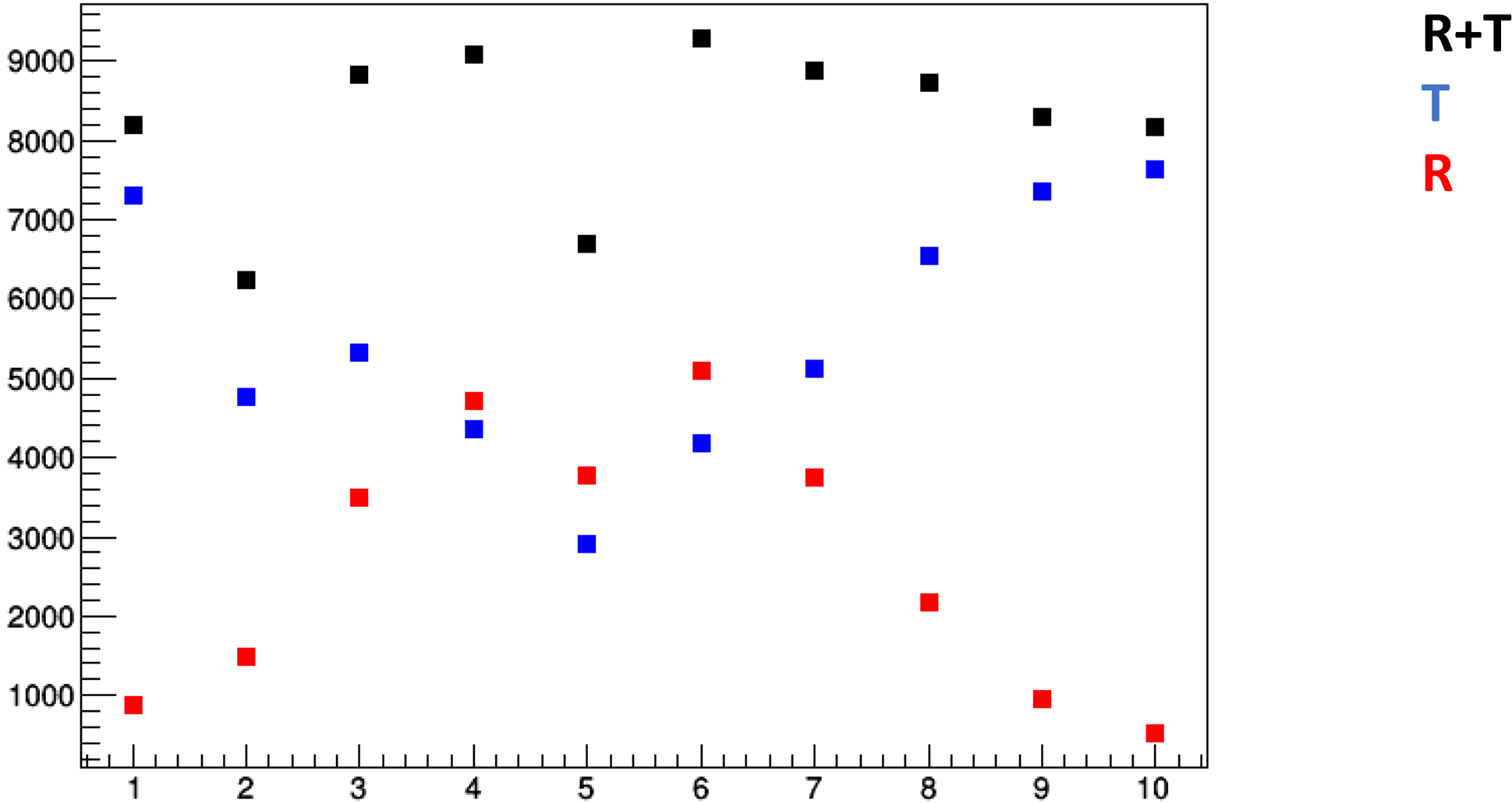
- Combine poissonian error on detector counts with a fixed 3% error

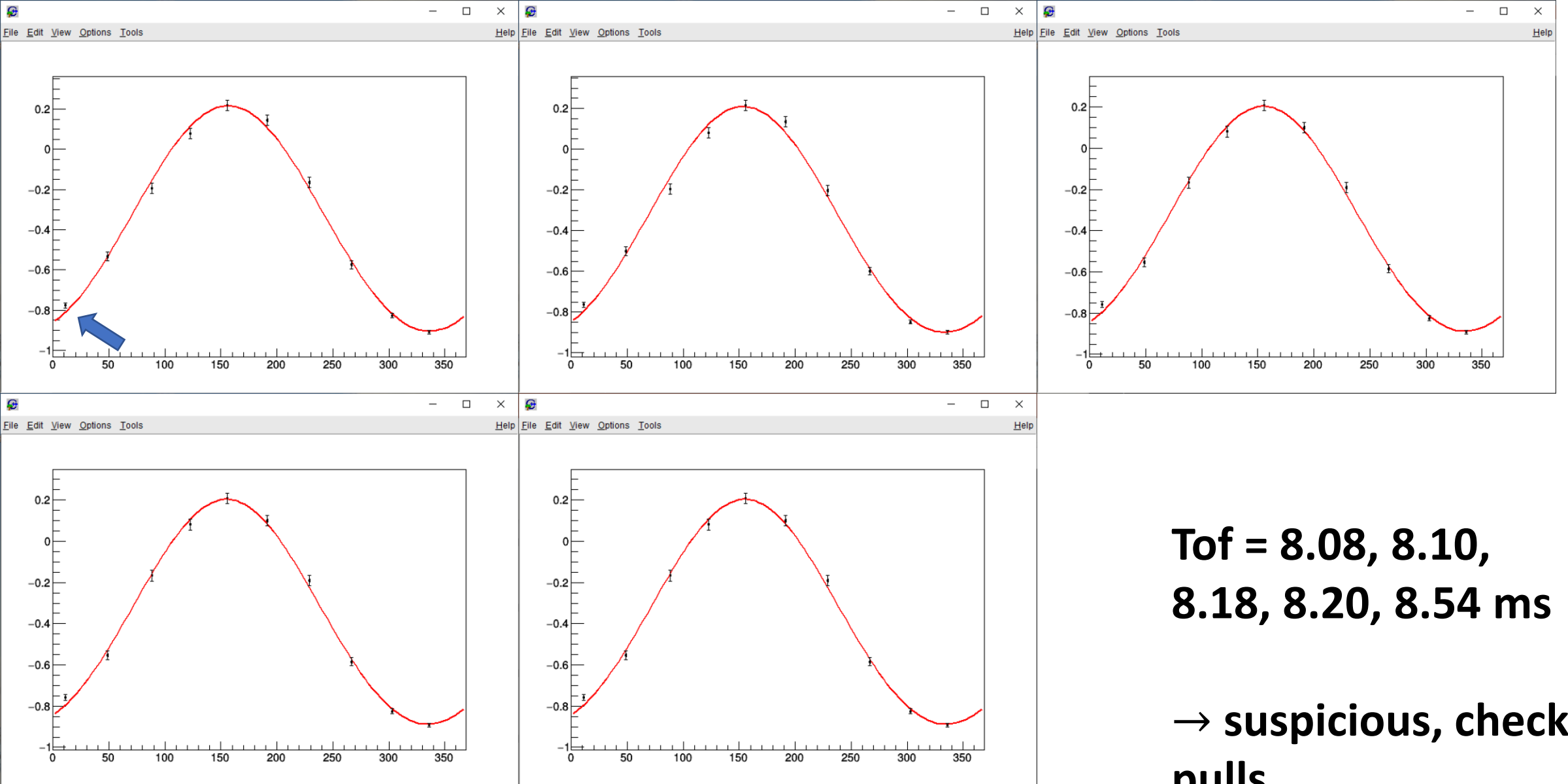


UP vs DOWN beams (125 μT)



Beam intensity variations (125 uT, tof = 5 ms, up)

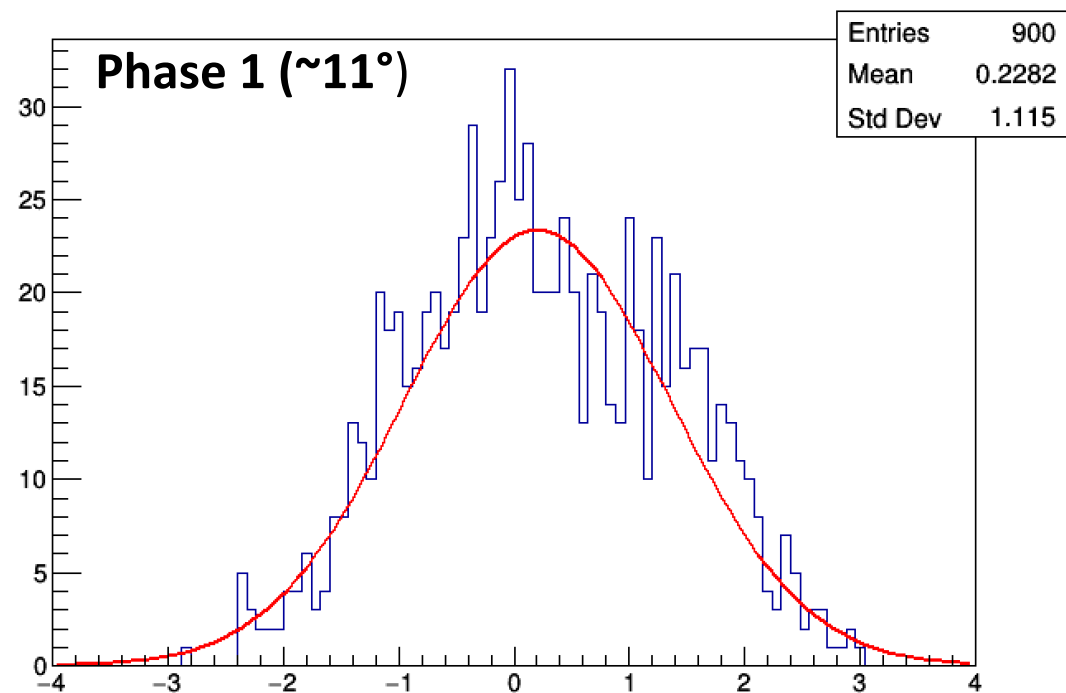




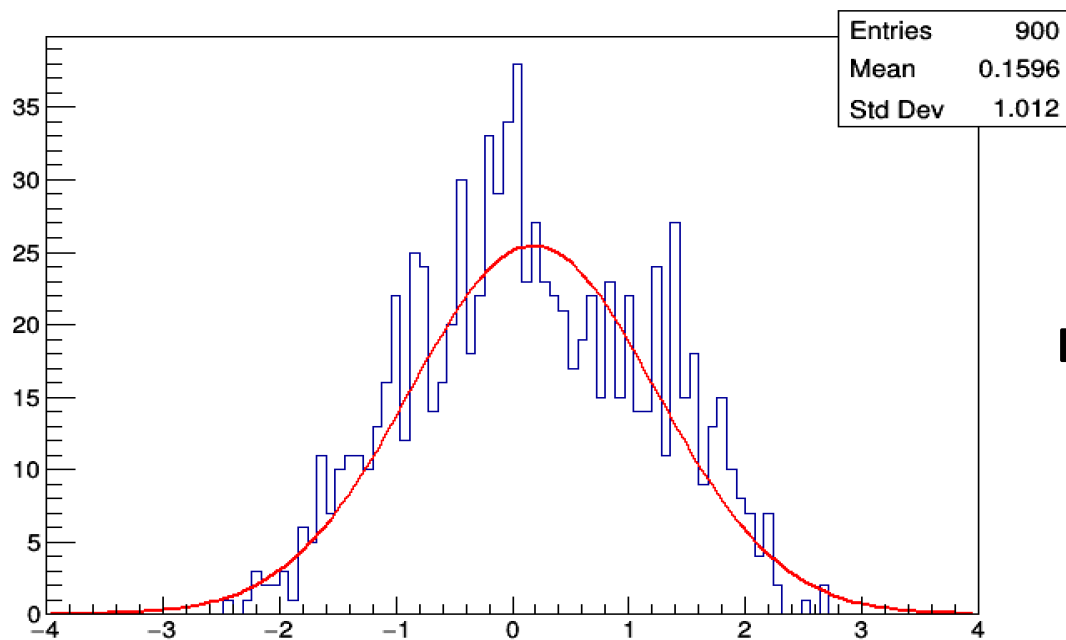
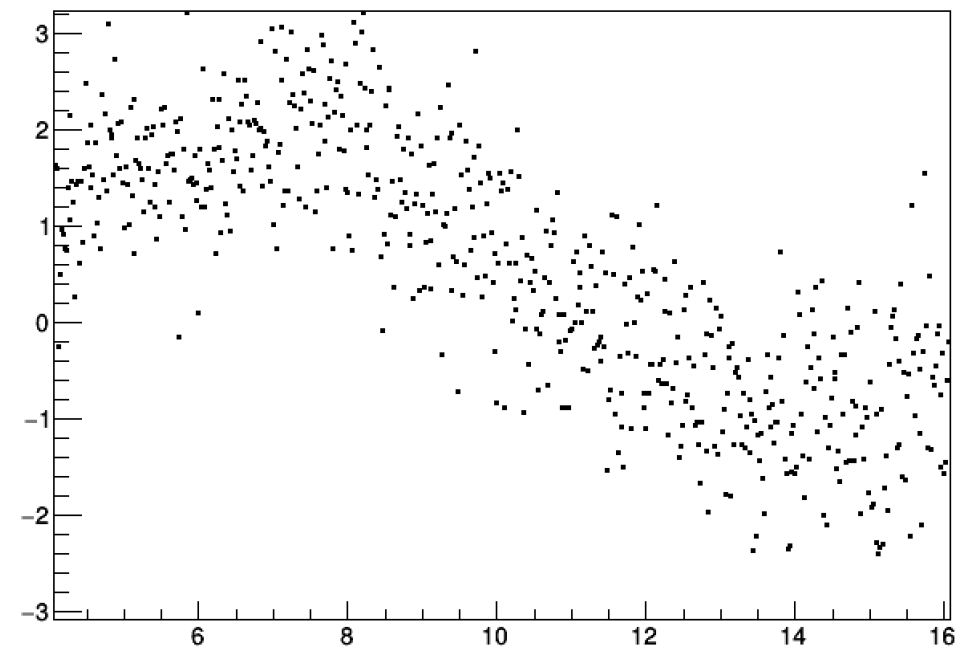
**Tof = 8.08, 8.10,
8.18, 8.20, 8.54 ms**

**→ suspicious, check
pulls**

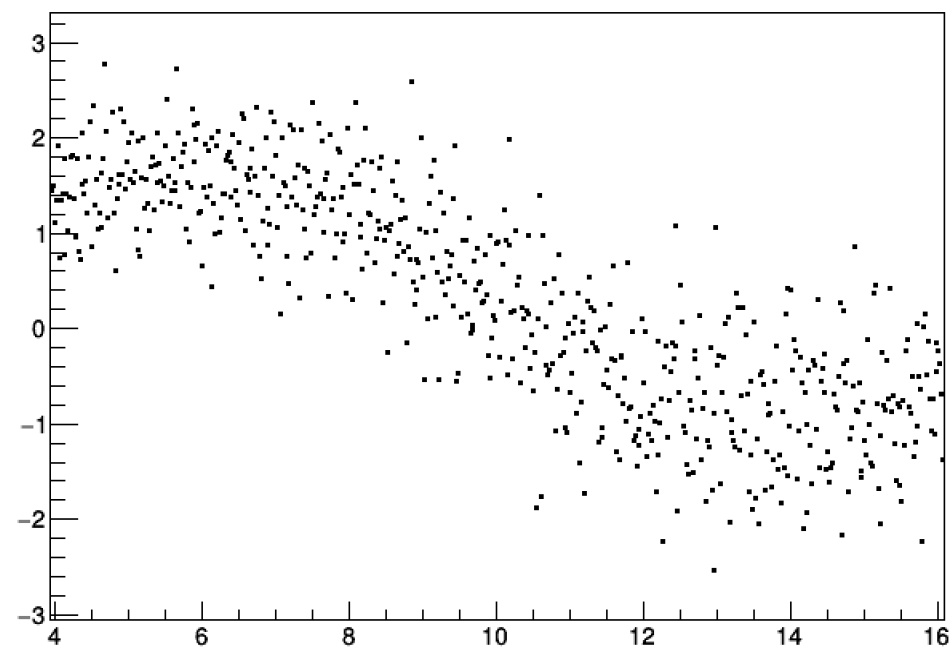
Pull distr.: $\frac{A_{obs} - A_{fit}}{\sigma_A}$ if OK, it's a gaussian with $\mu = 0$ and $\sigma = 1$

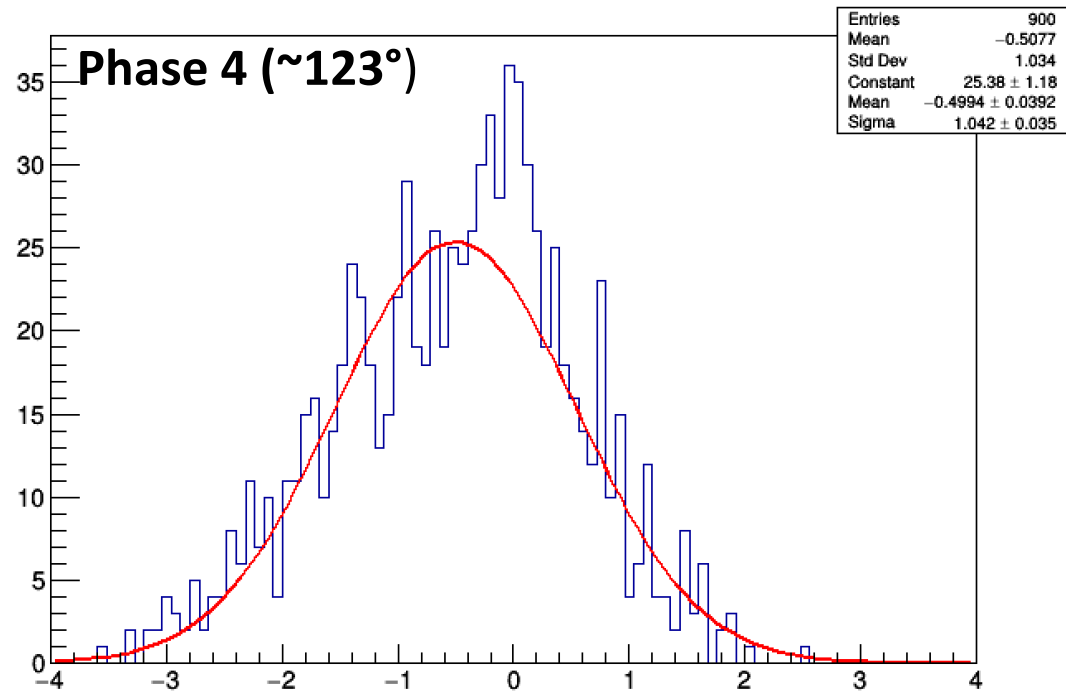


UP

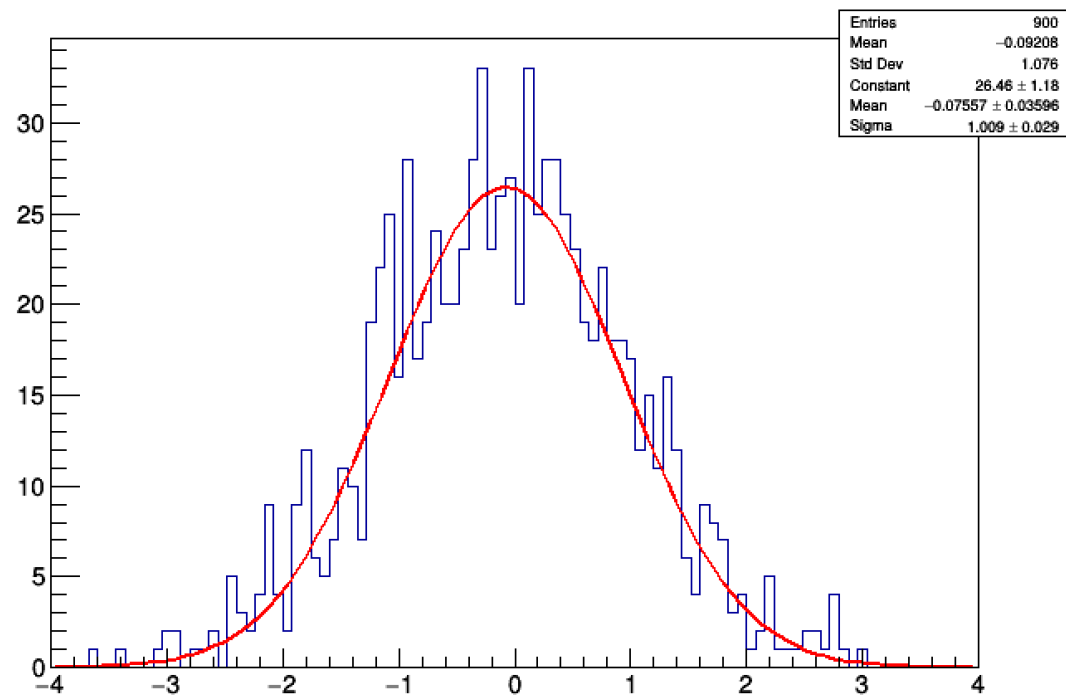
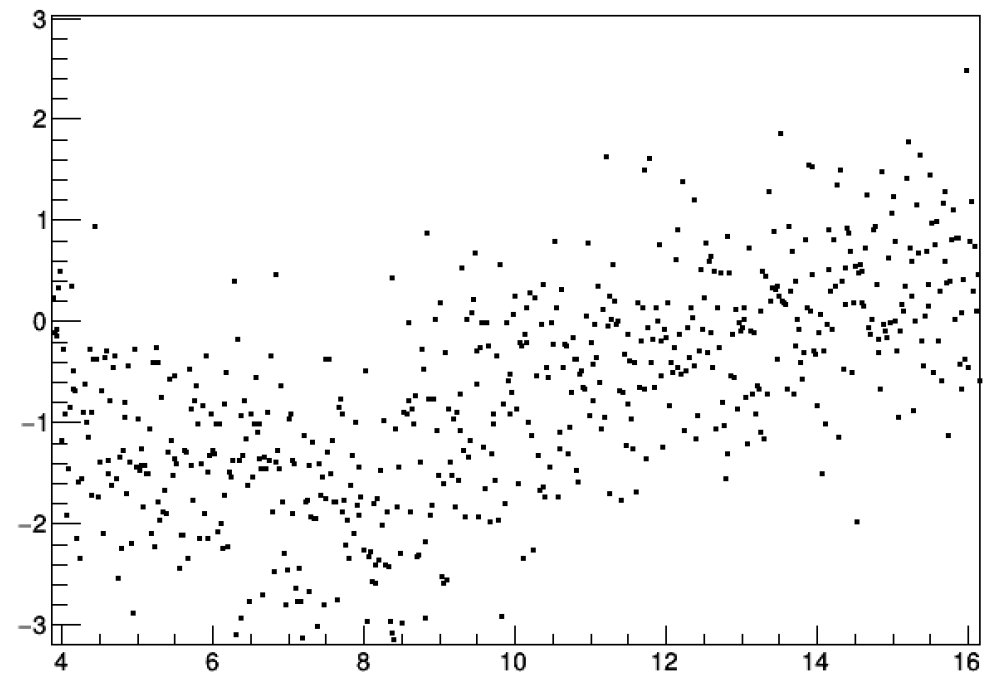


DOWN

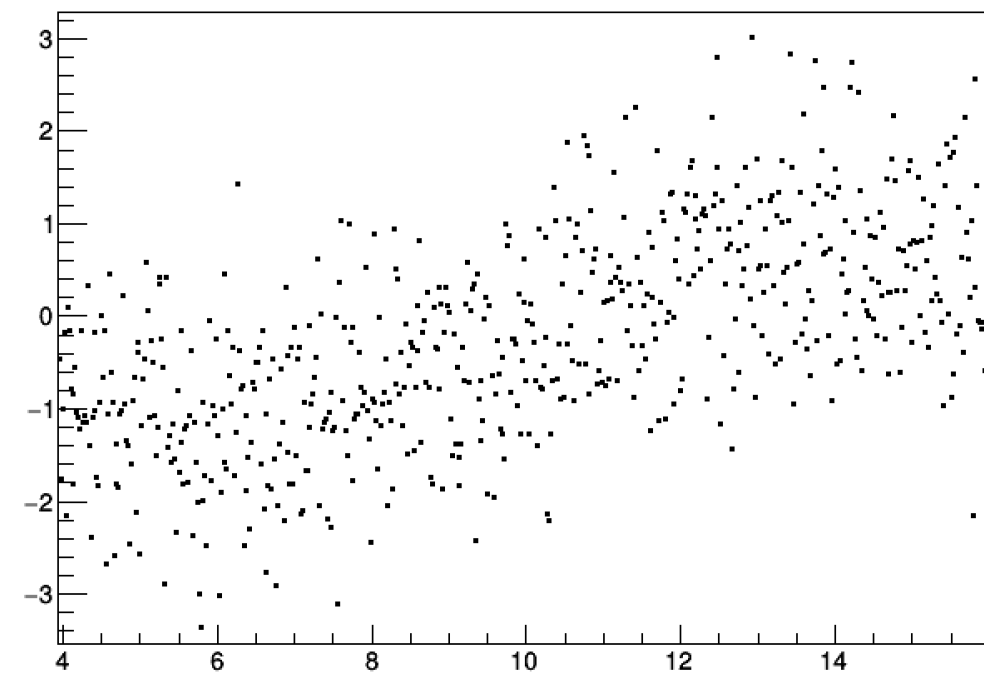


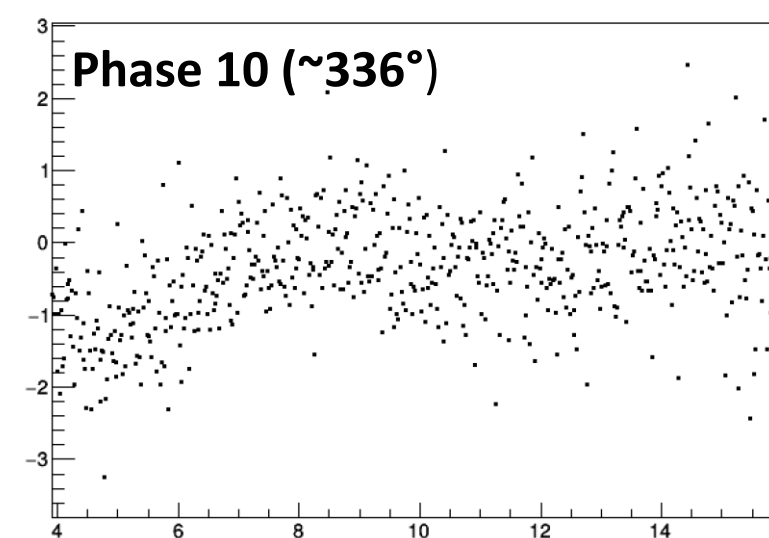
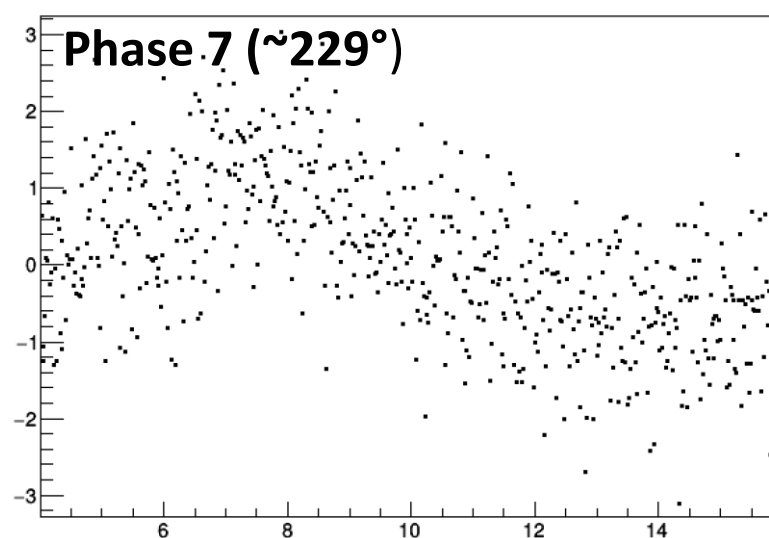
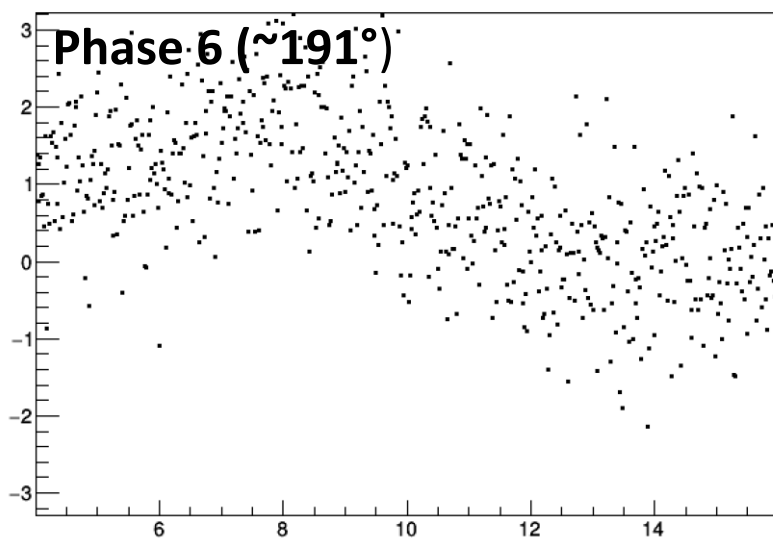
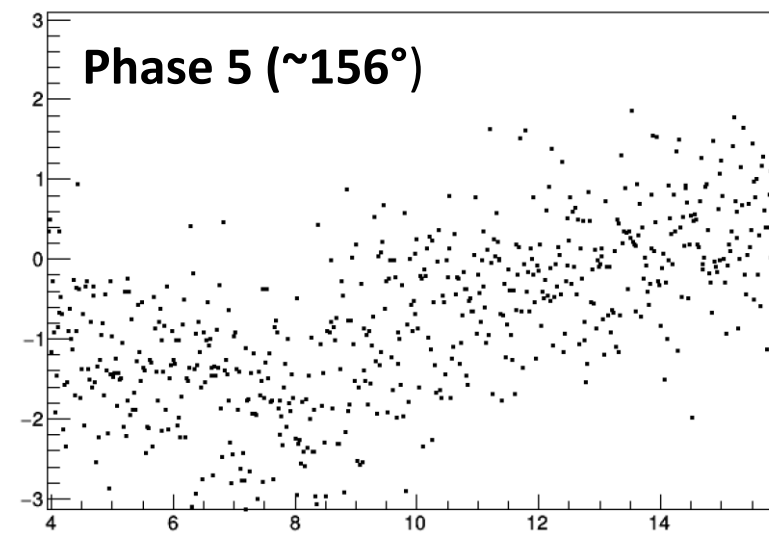
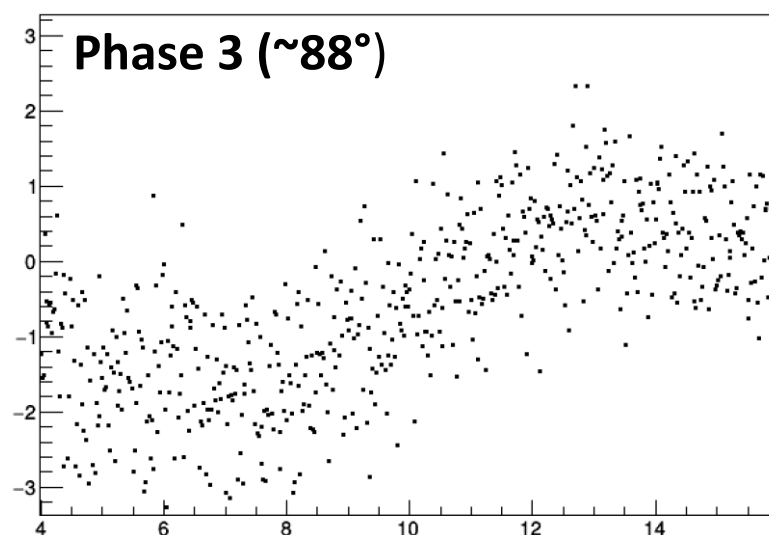
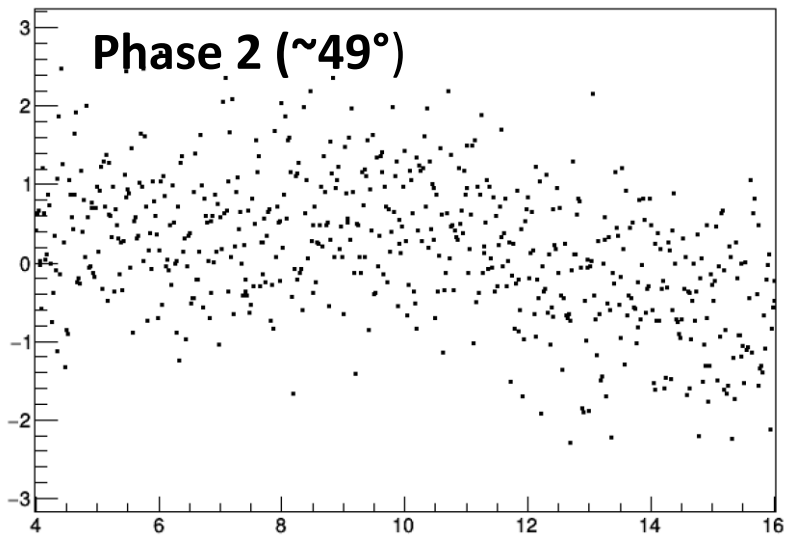


UP

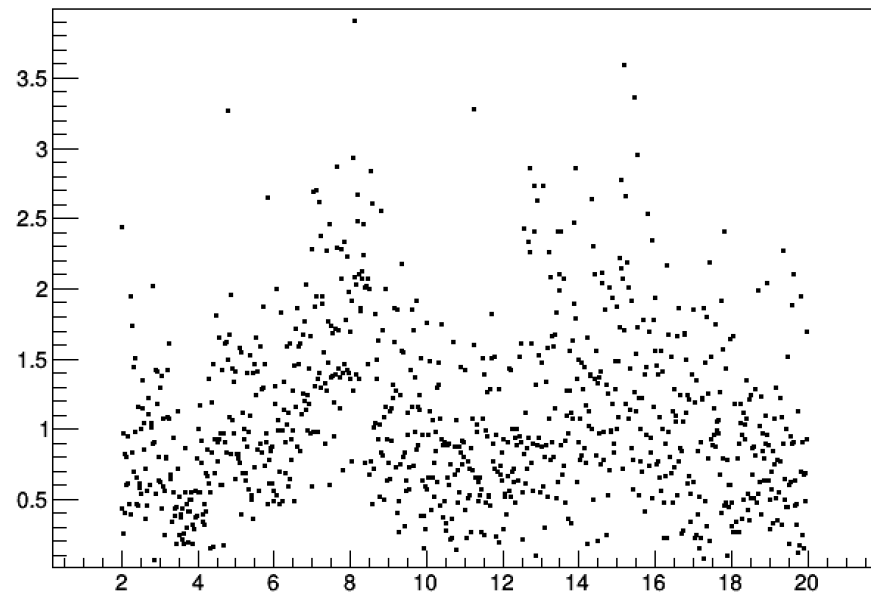


DOWN

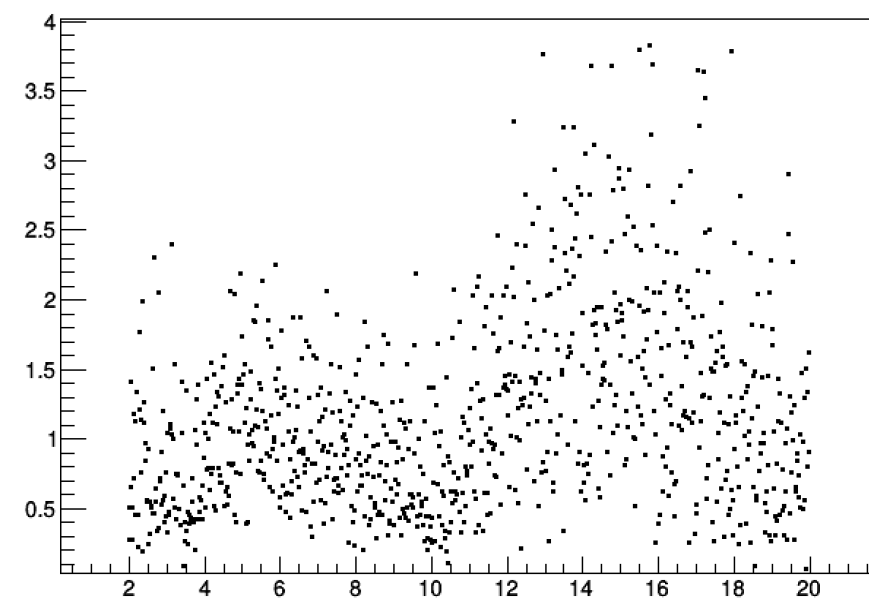




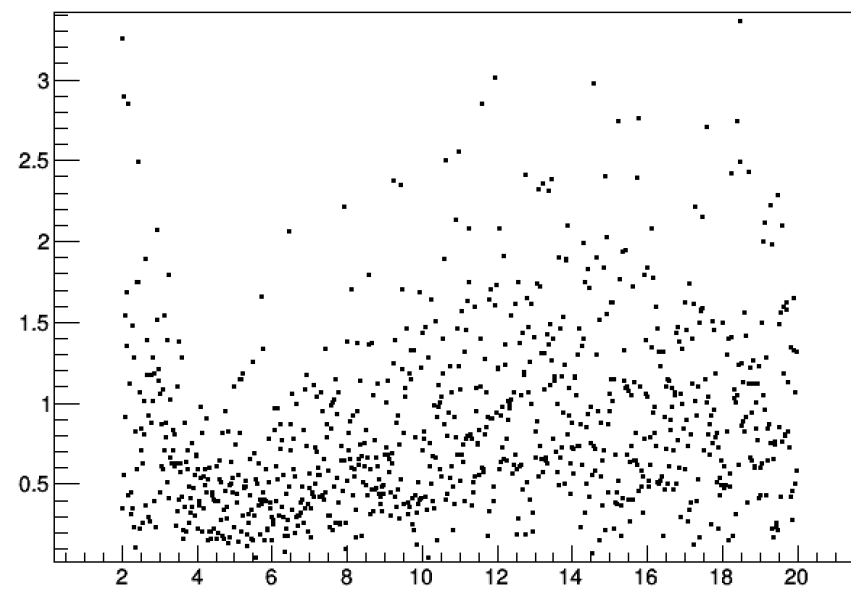
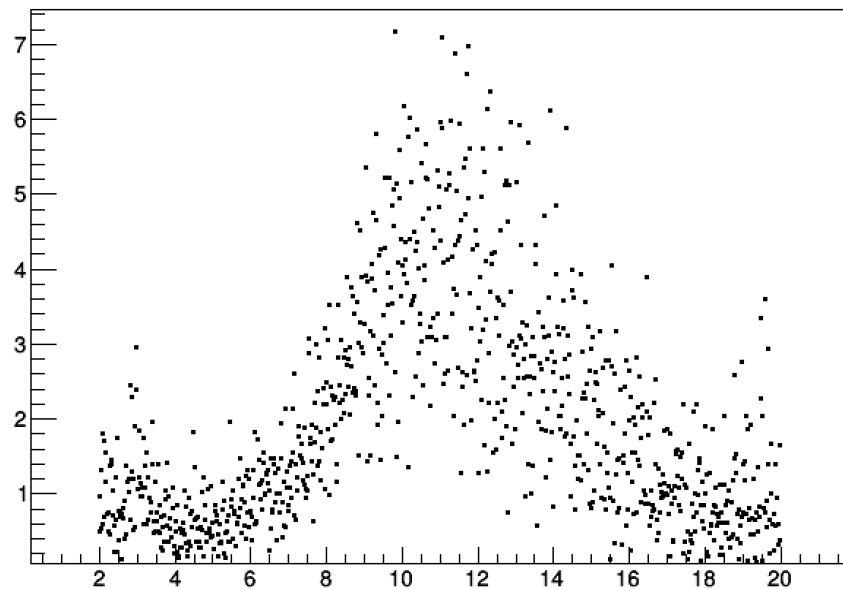
χ^2 UP vs. DOWN



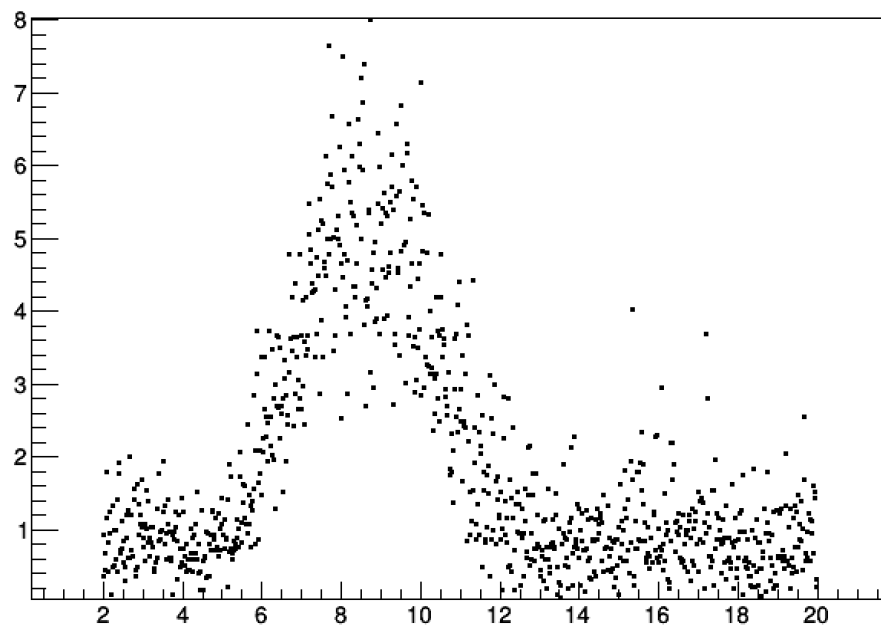
(125 μT)



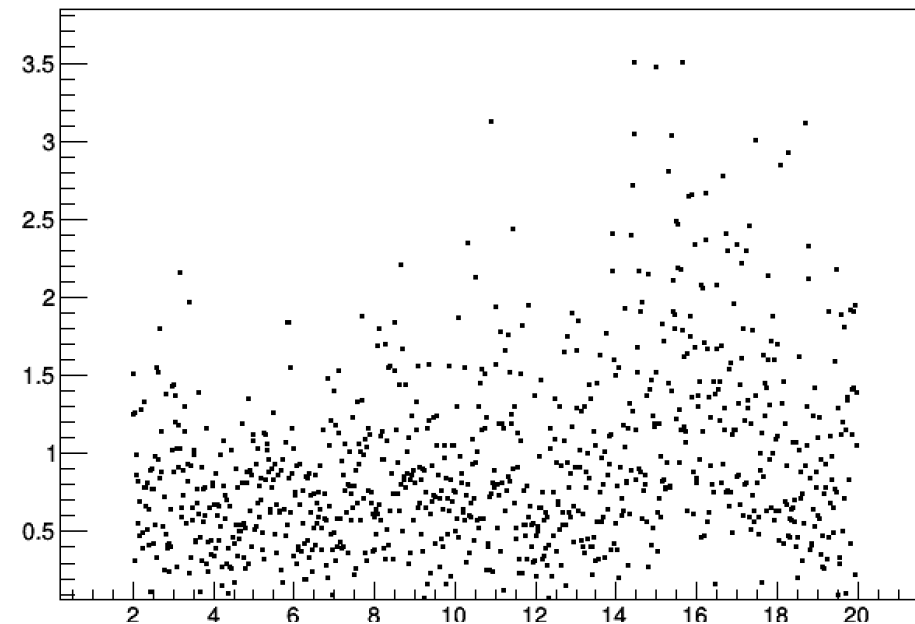
(124 μT)



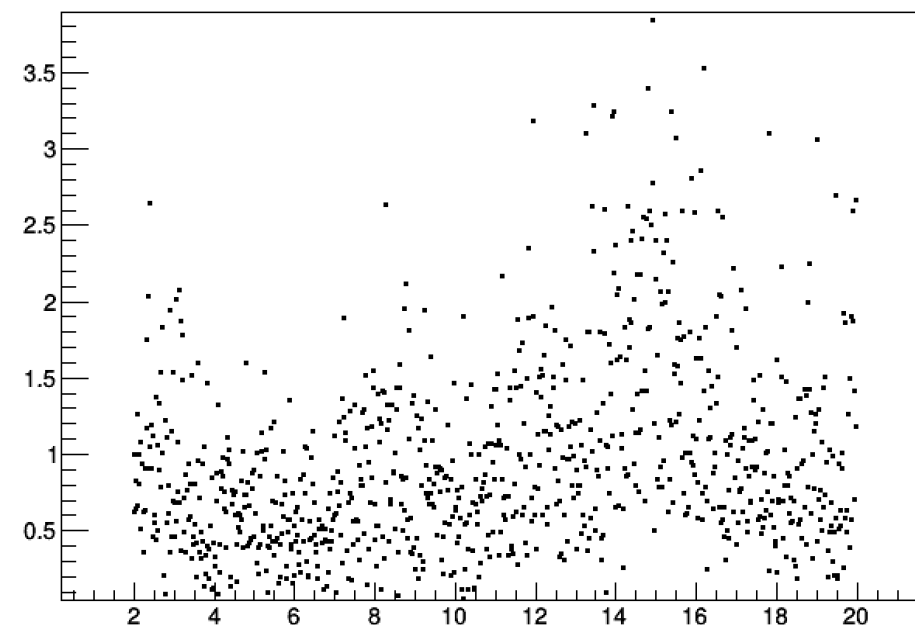
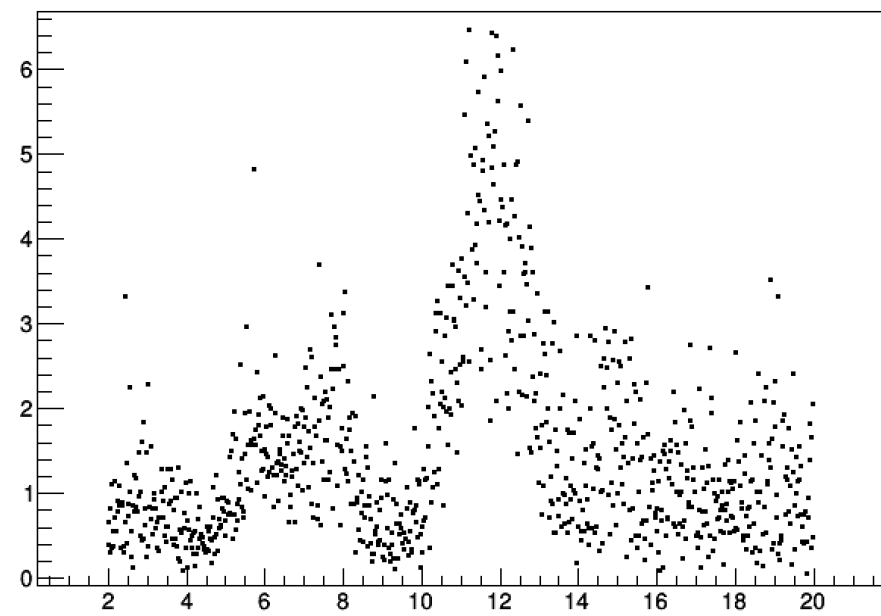
χ^2 UP vs. DOWN

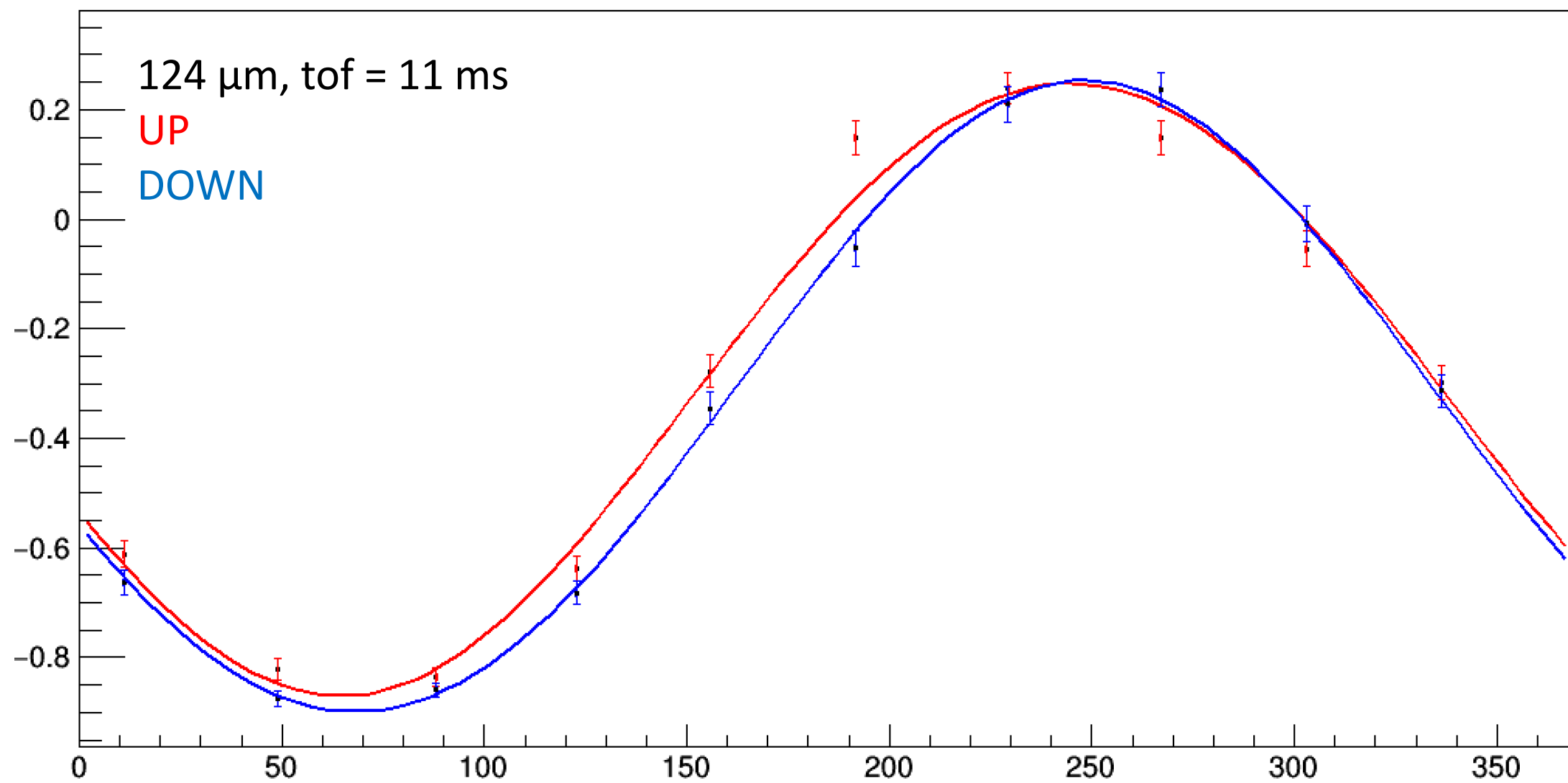


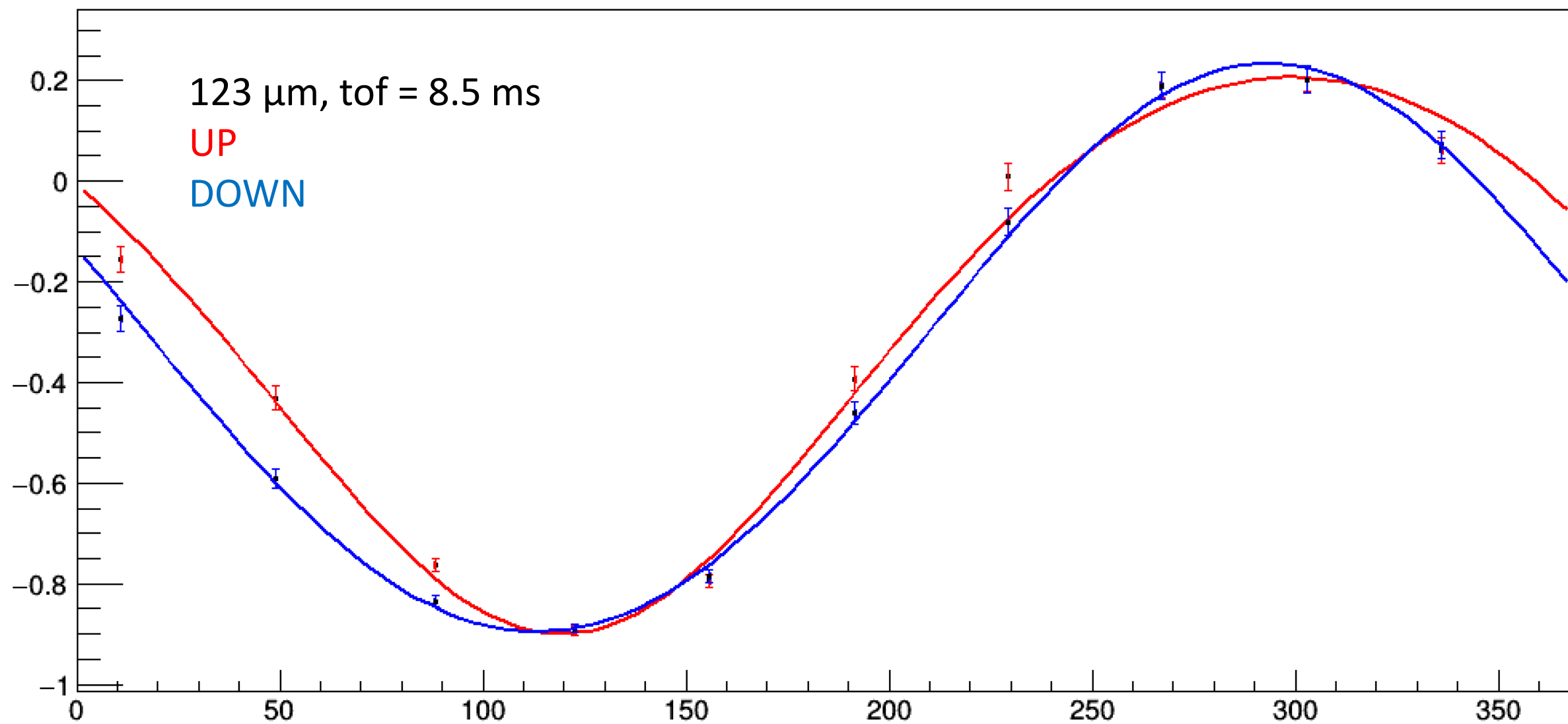
(123 μT)

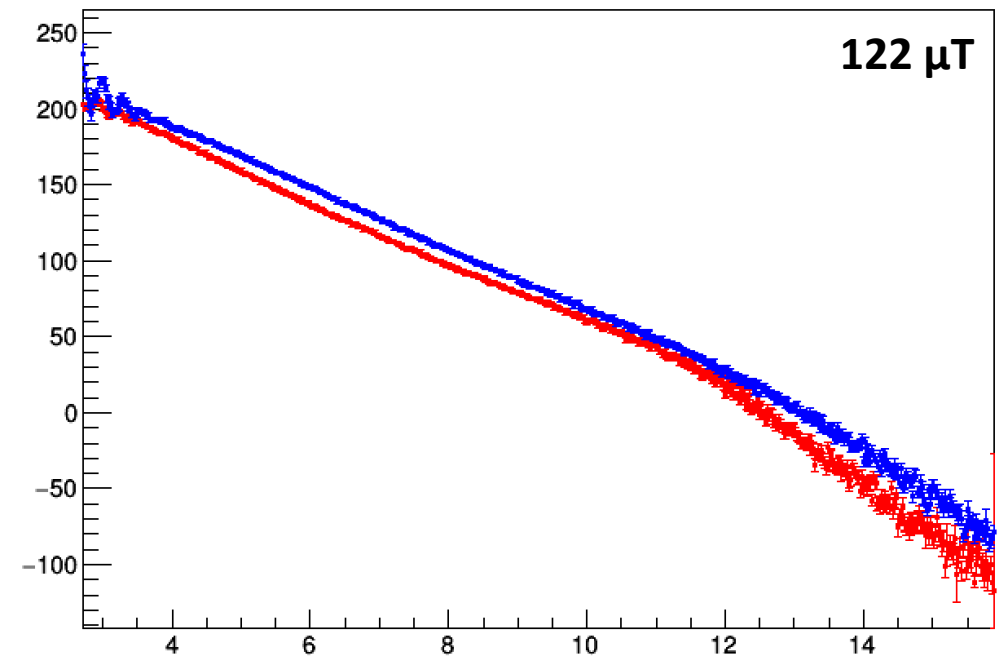
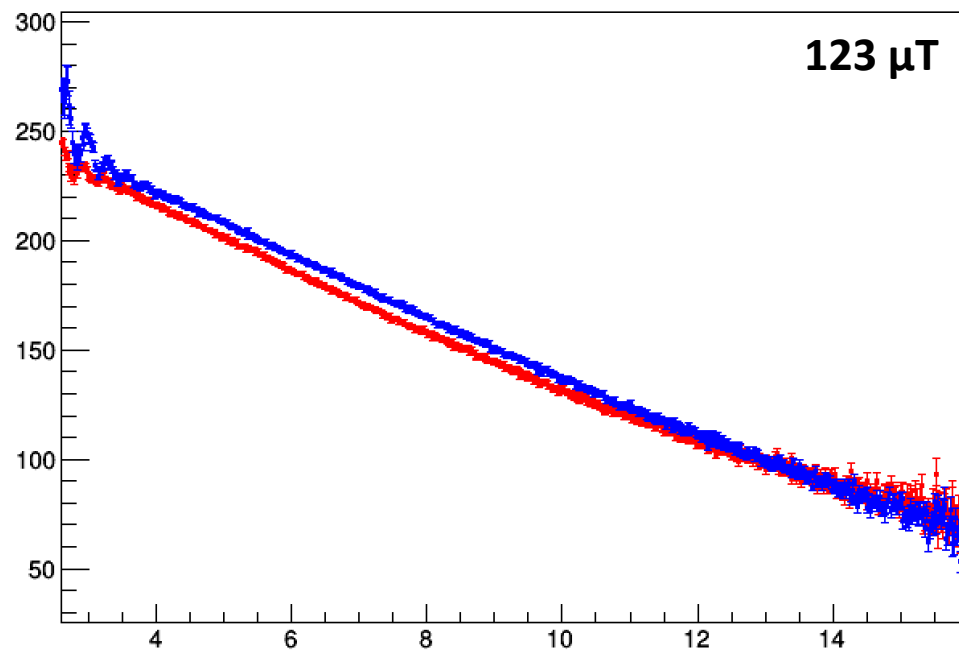
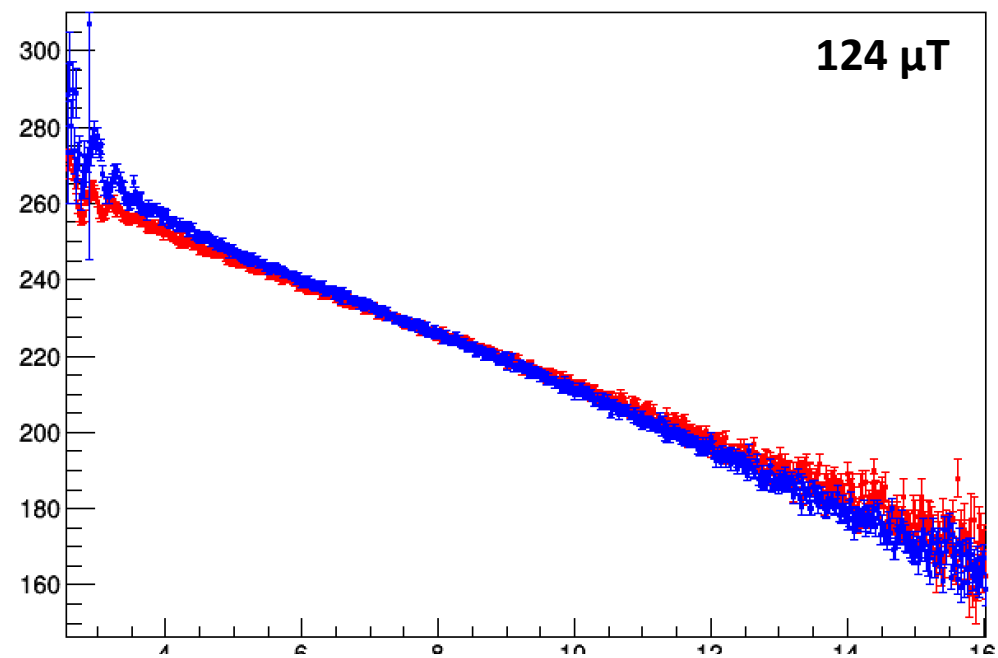
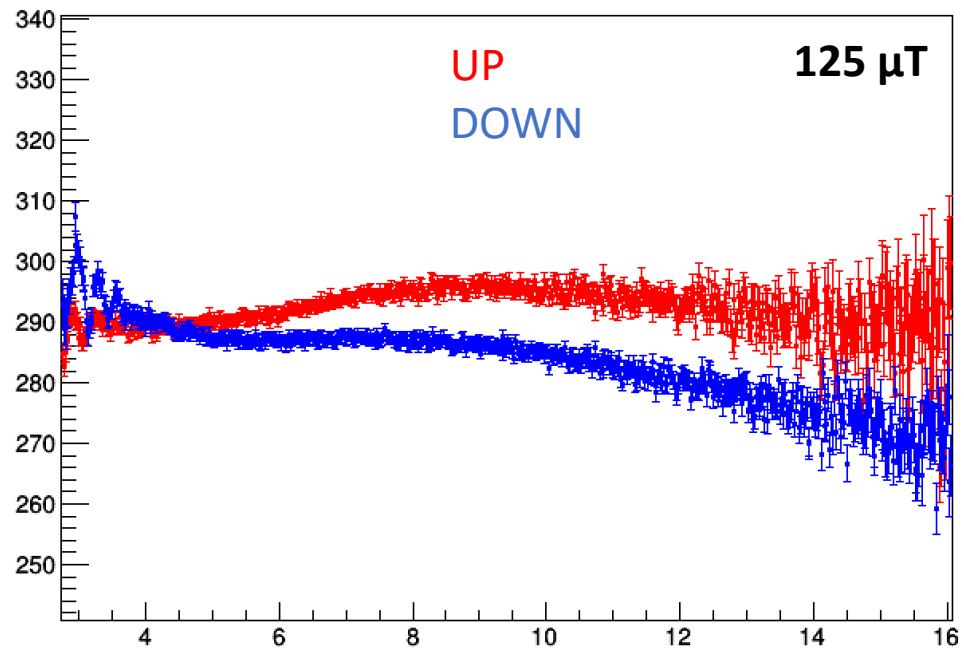


(122 μT)

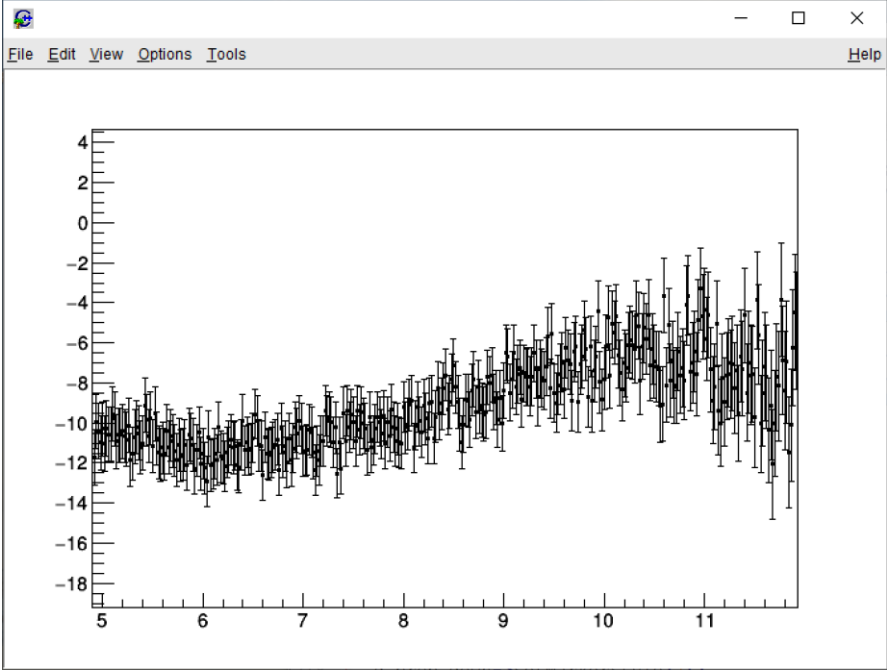
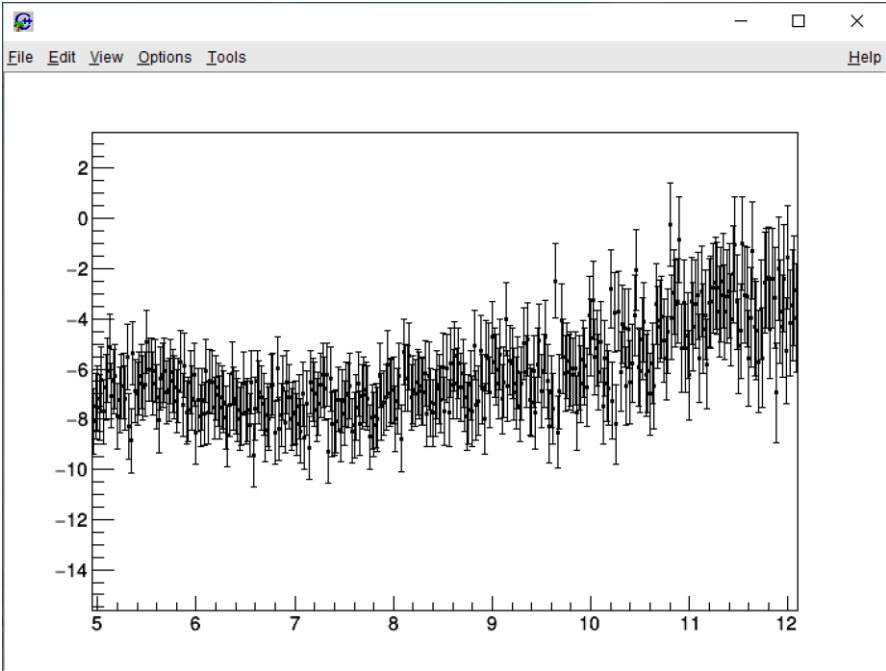
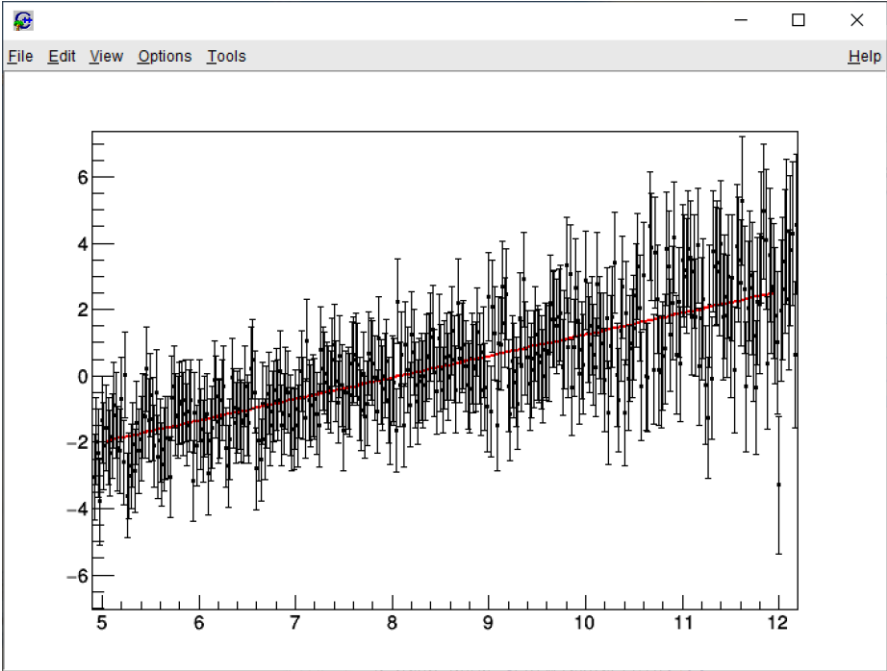
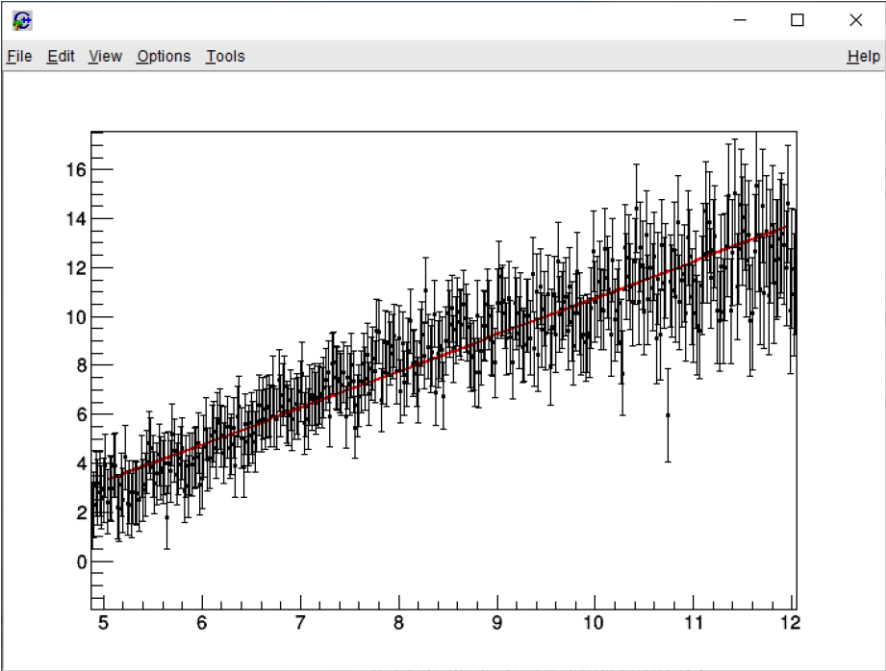








UP - DOWN



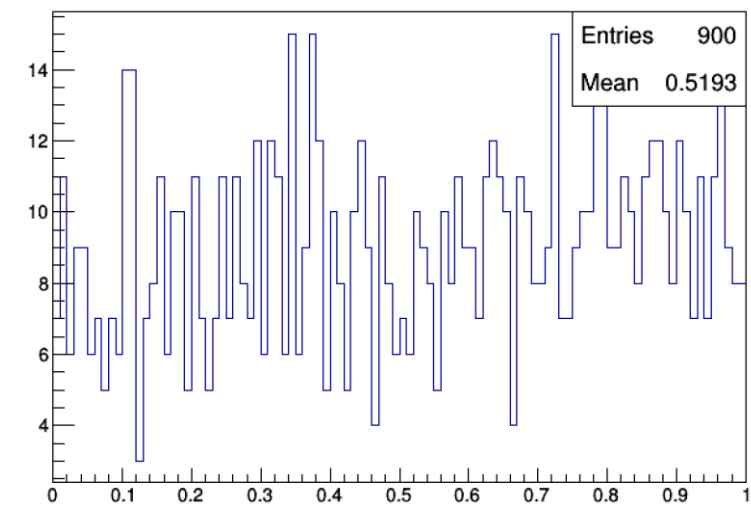
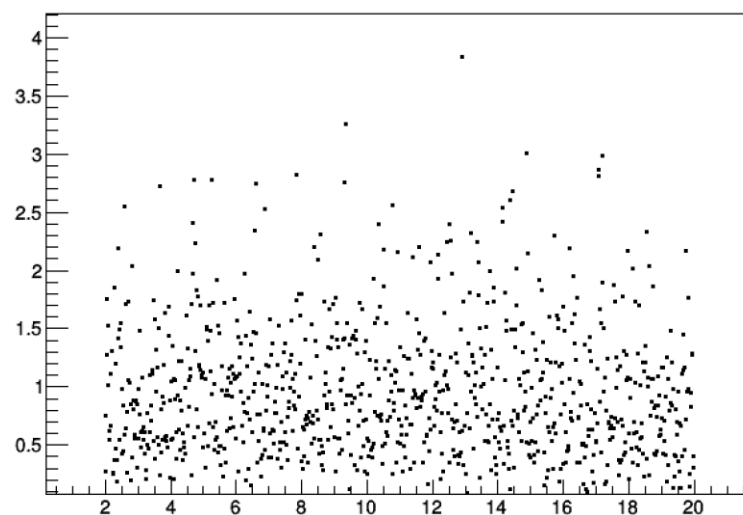
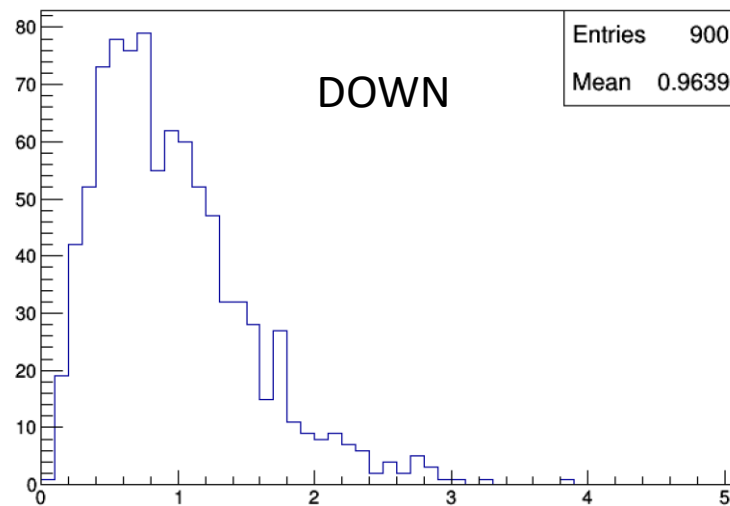
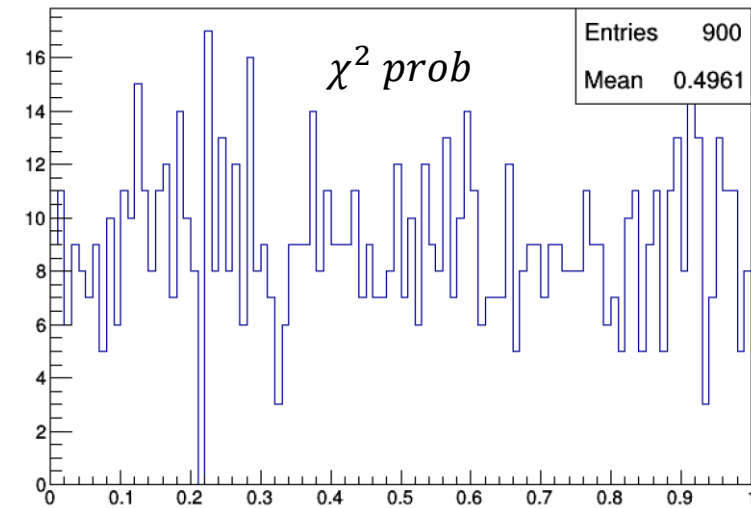
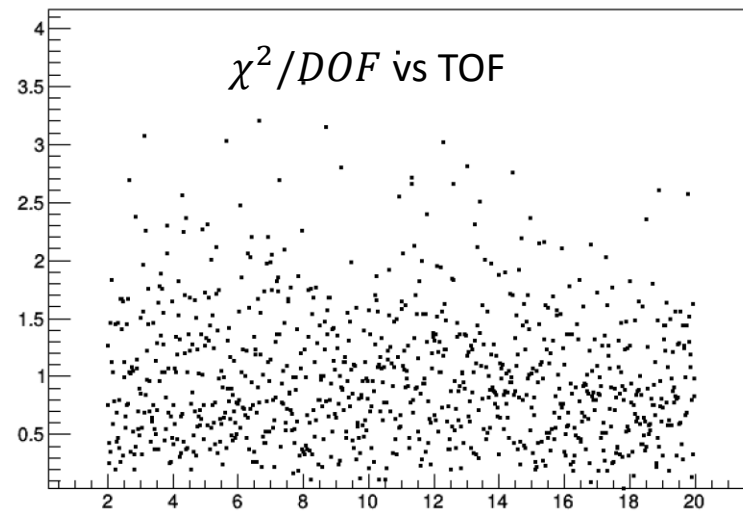
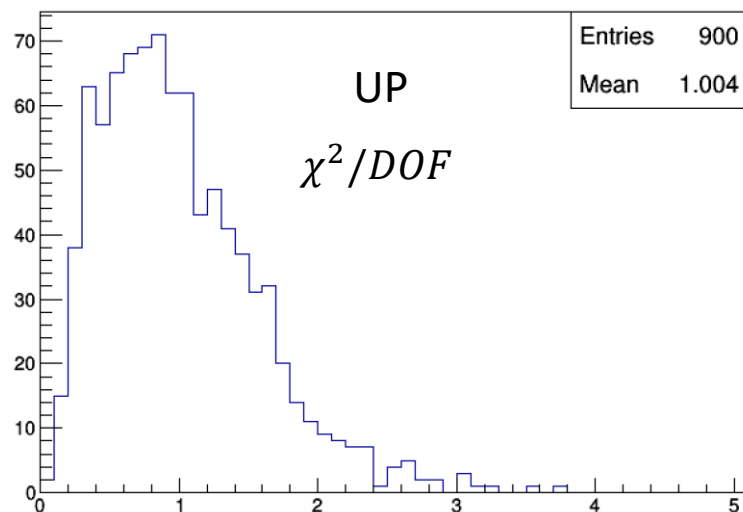
Phase scan analysis (sinusoidal signal)

Logbook: BOA_Logbook_Sept-2018 pages 39 ($B_0 = 125, 124, 123, 126, 127$ uT)

Data: T151018_phramsey-tof_0009.tof -> _0058.tof
Ramsey-1000004.dat-> ...8.dat

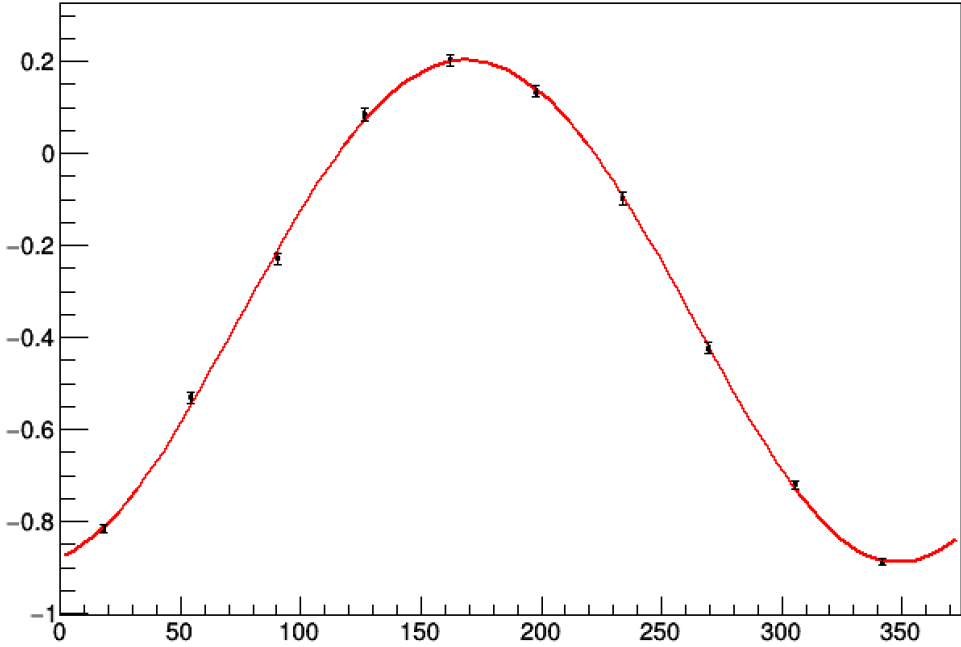
N.B: Assume detector data purely Poissonian (remove 3% correction)

125 μT

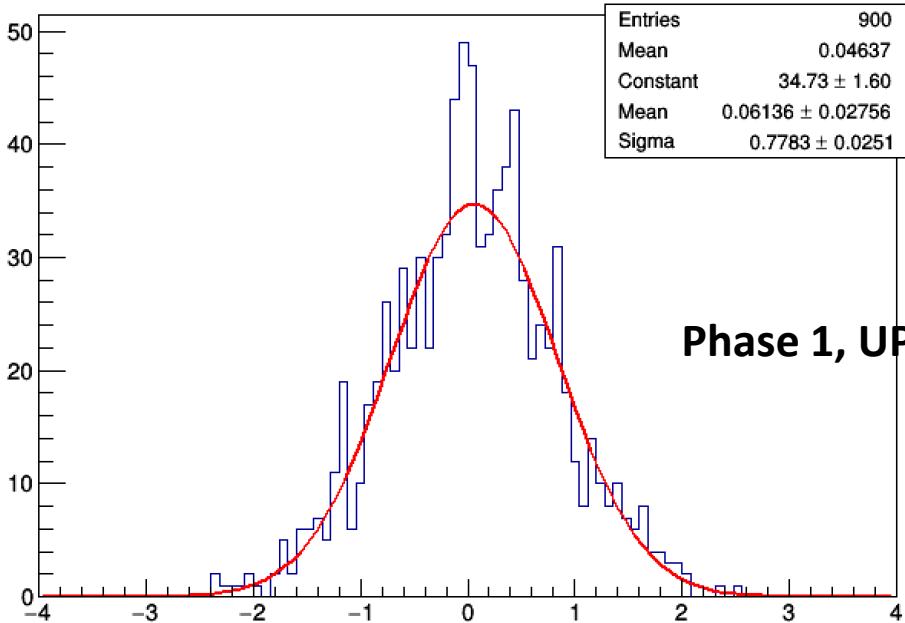


→ detector errors and fitting function OK

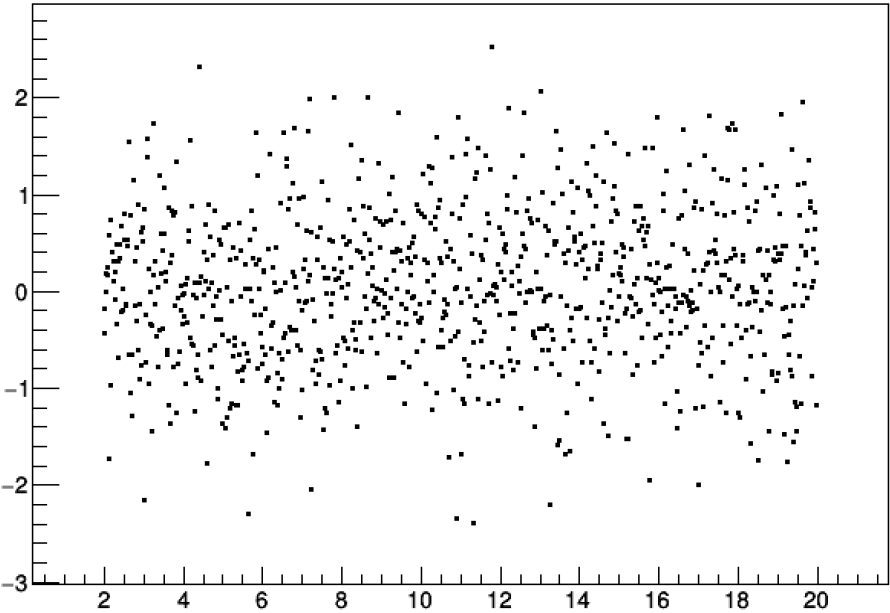
Pool distr.

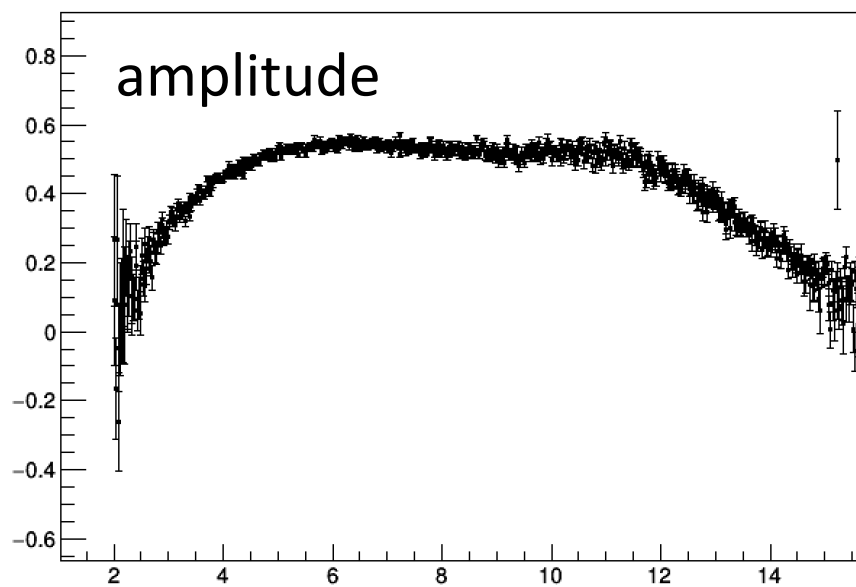
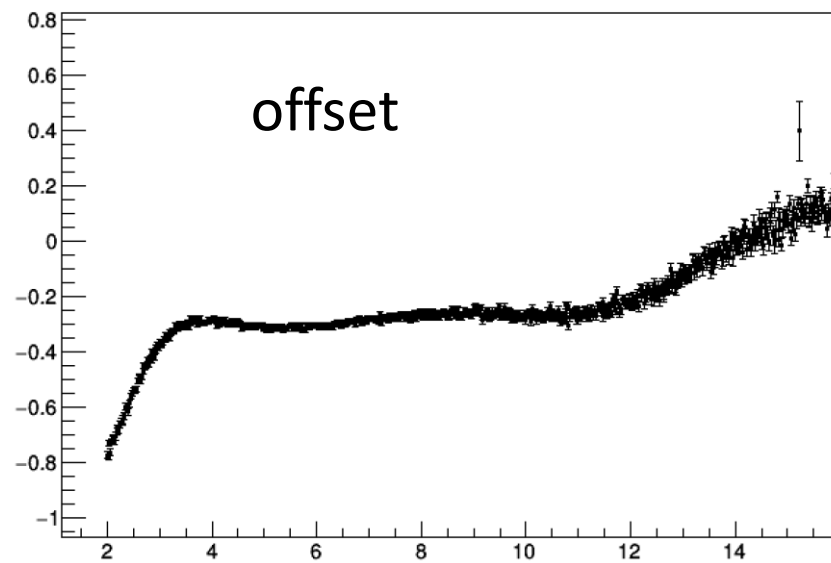
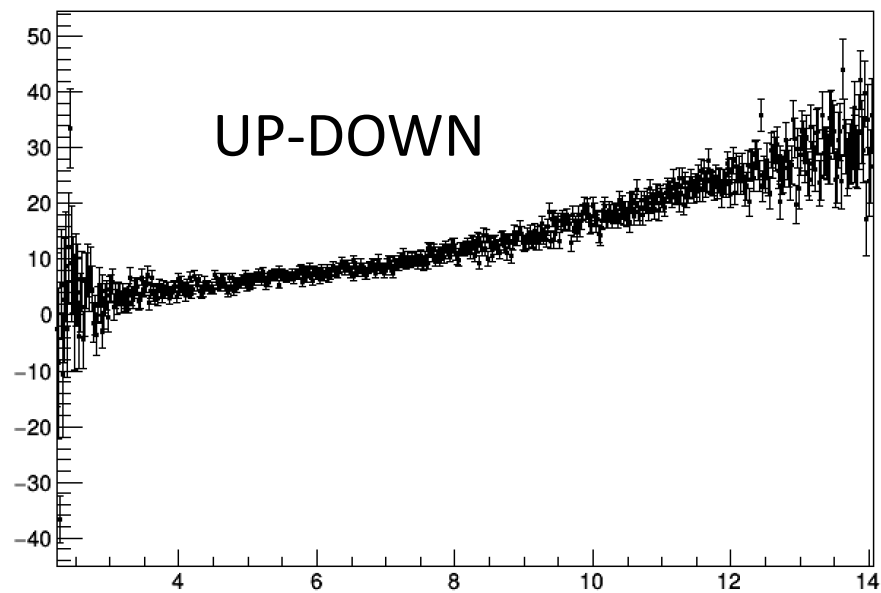
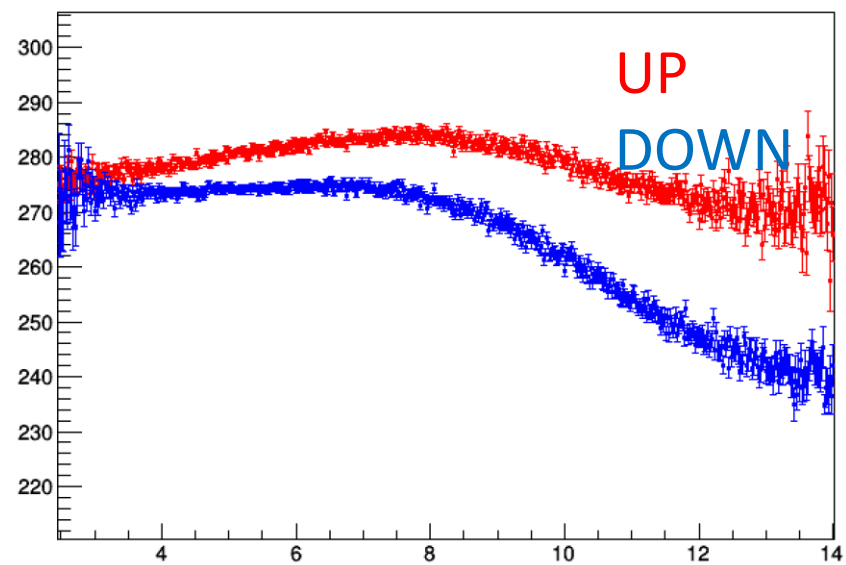


5 ms, up

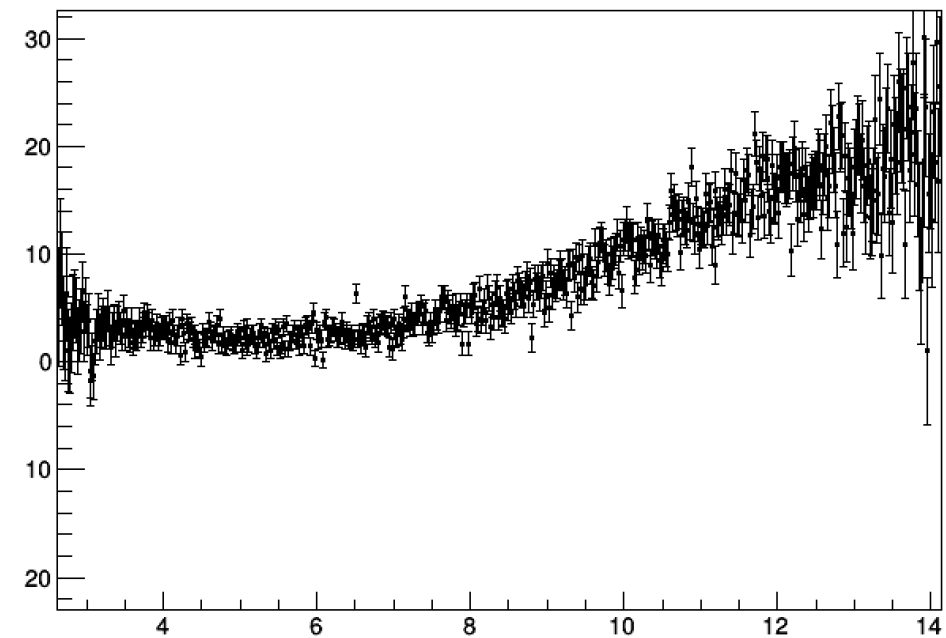
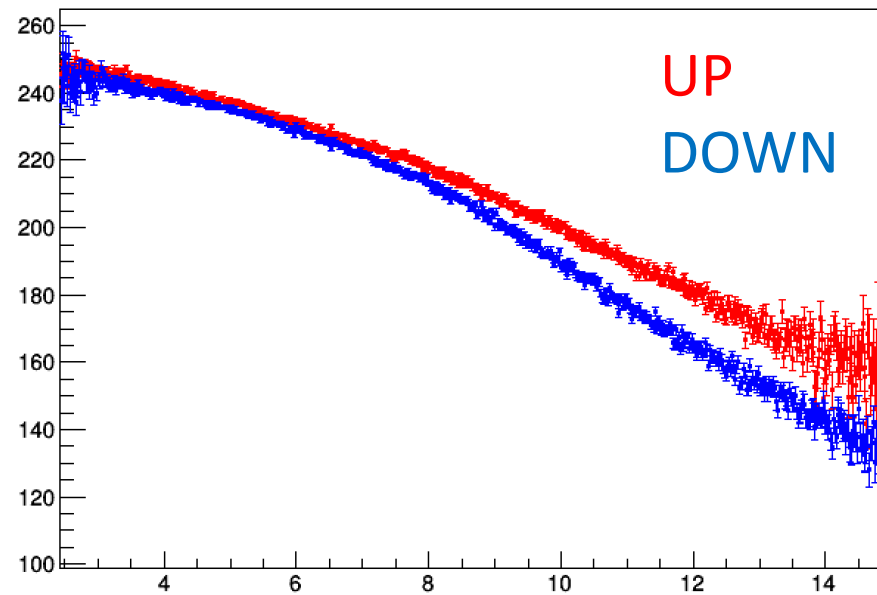


Phase 1, UP (~18°)

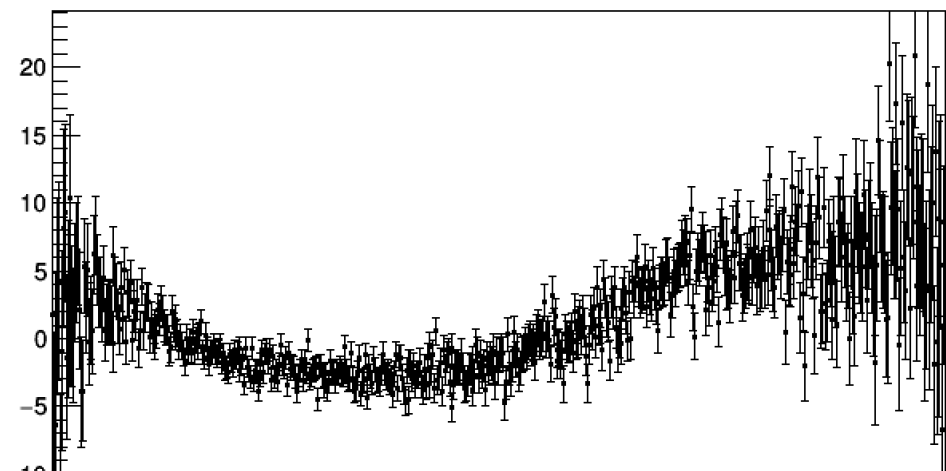
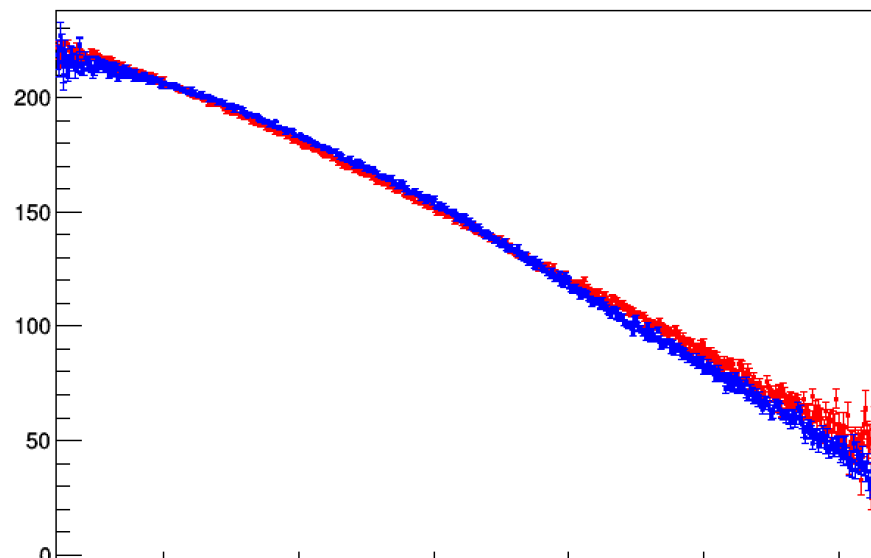


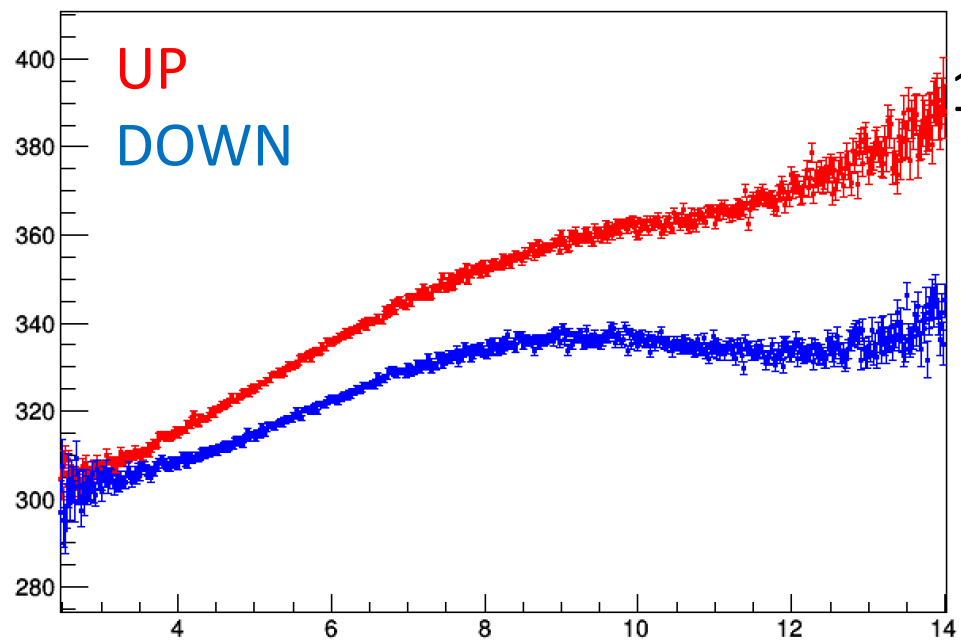


124 μT

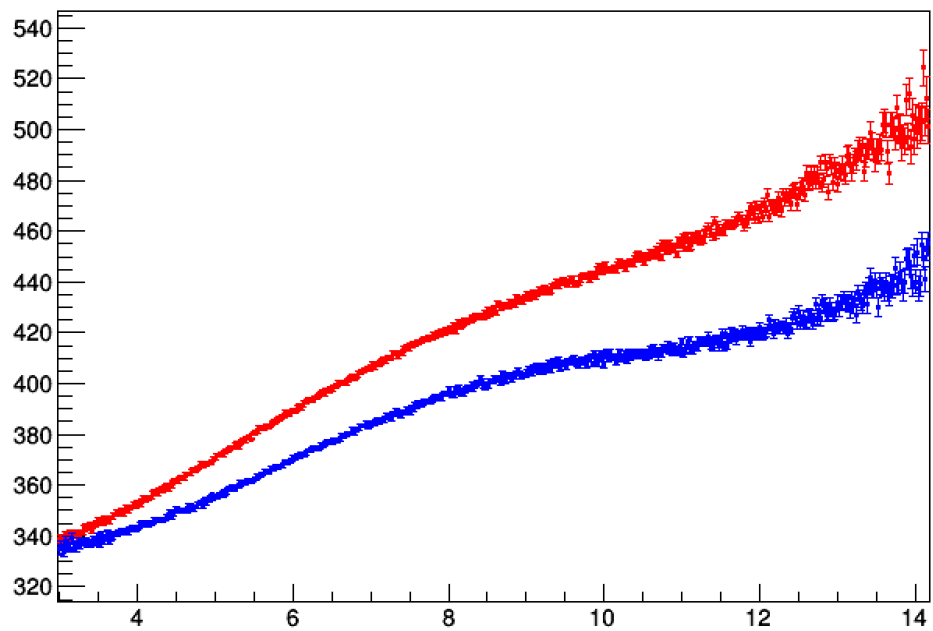
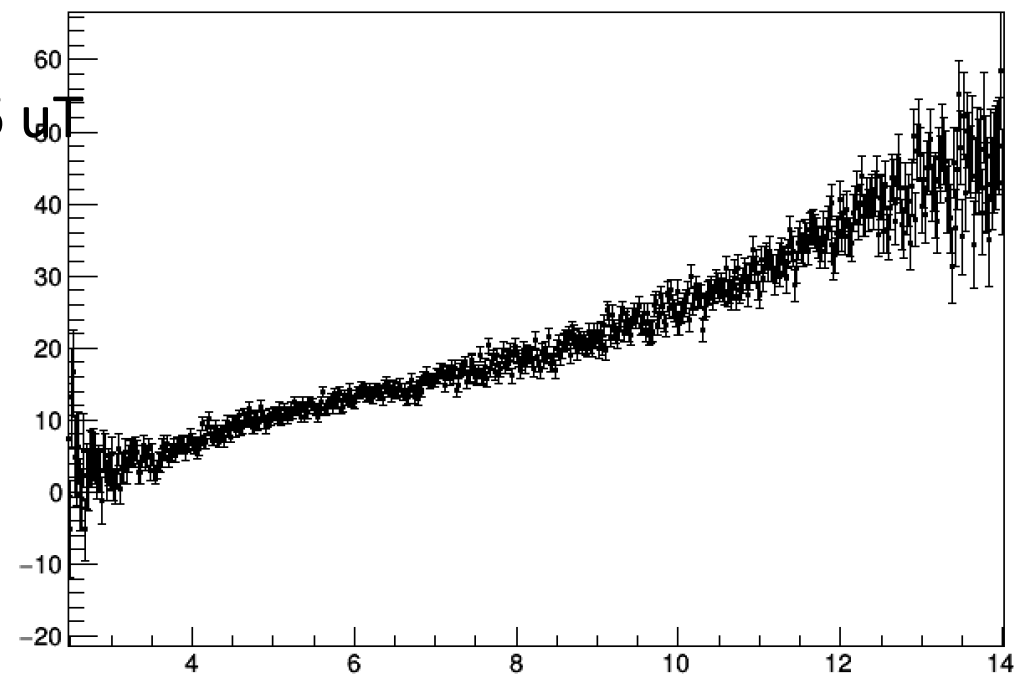


123 μT

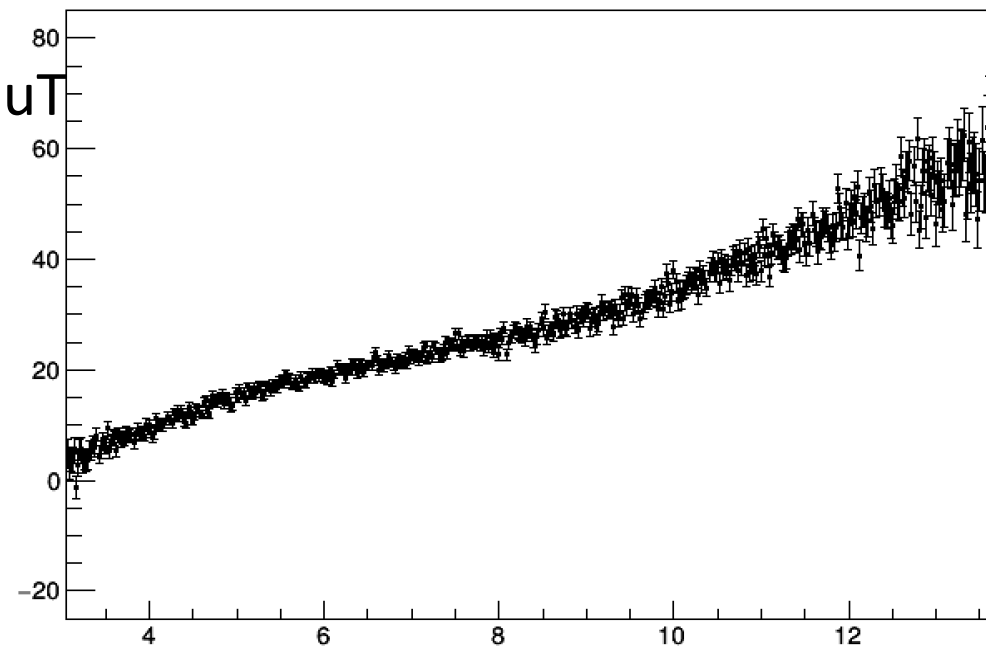




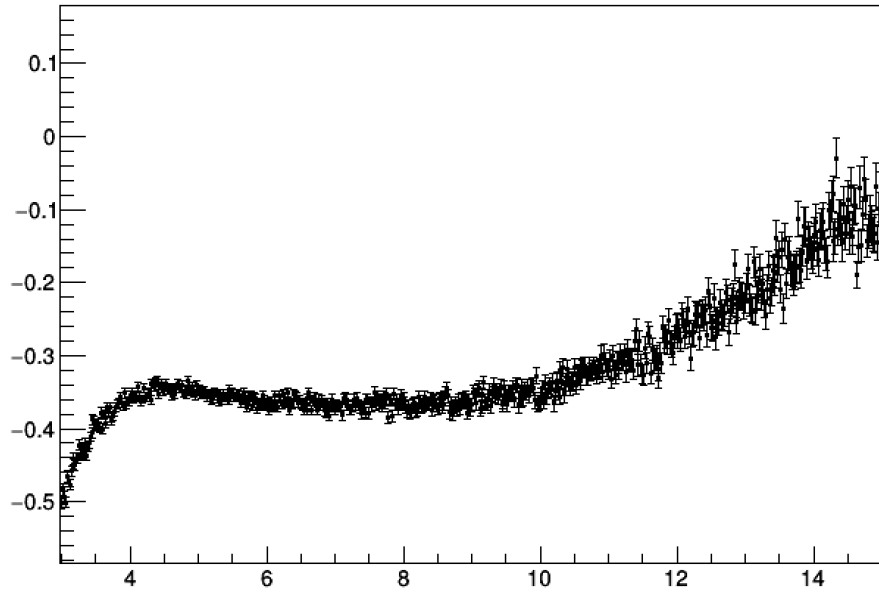
126 μT



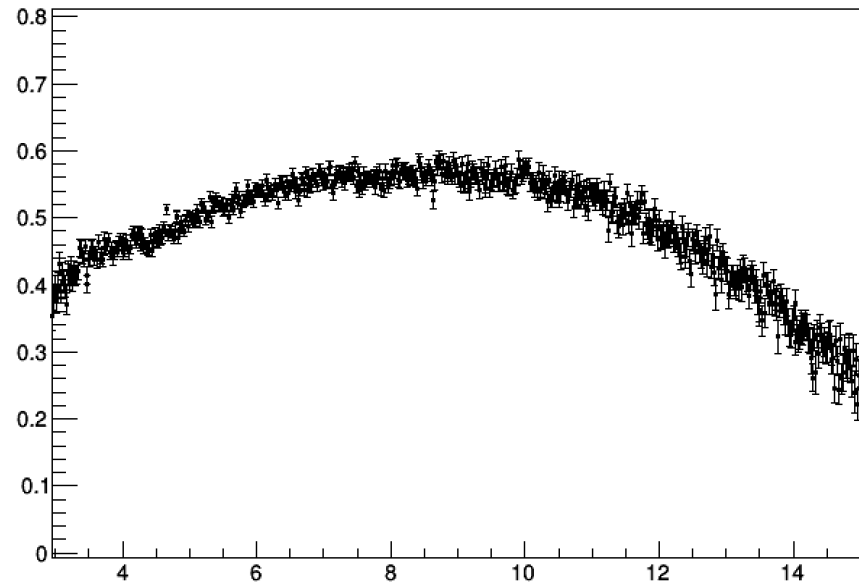
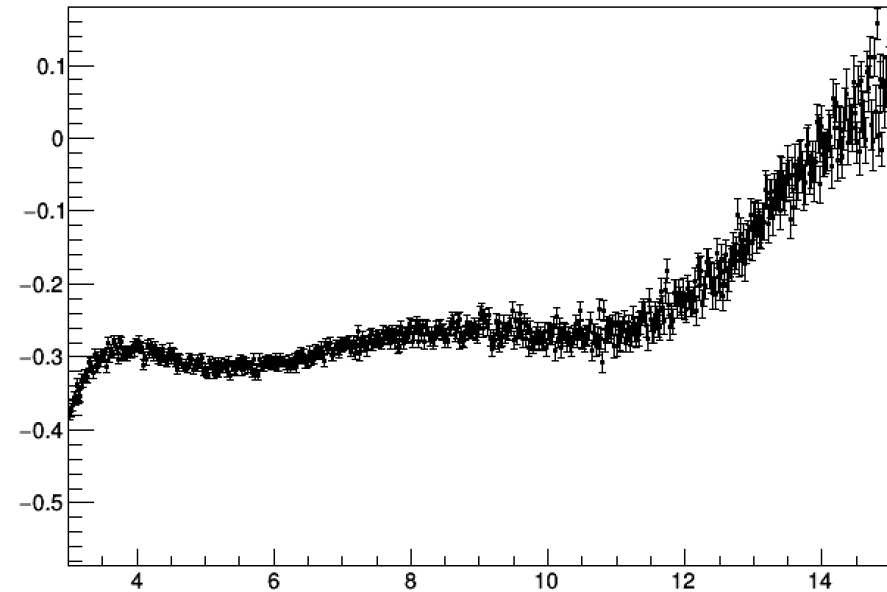
127 μT



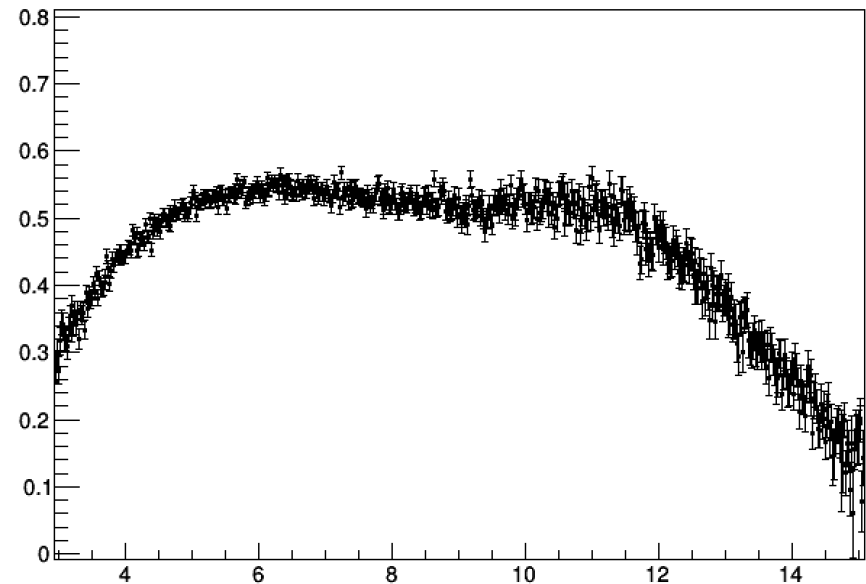
Modulated VS non modulated



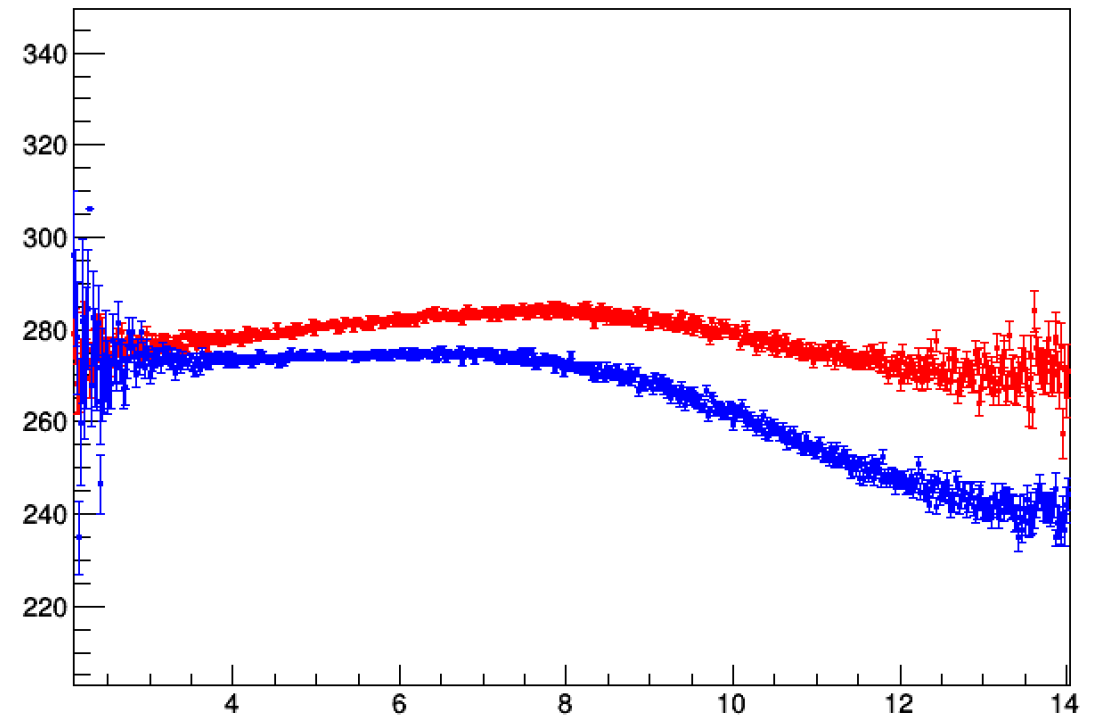
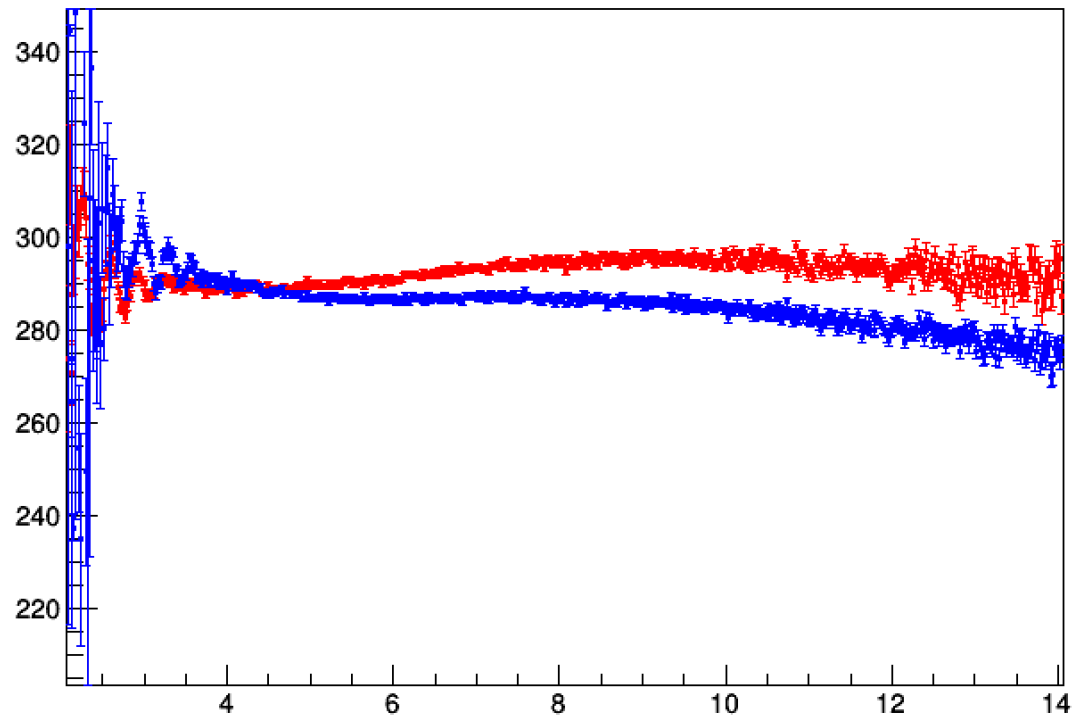
offset



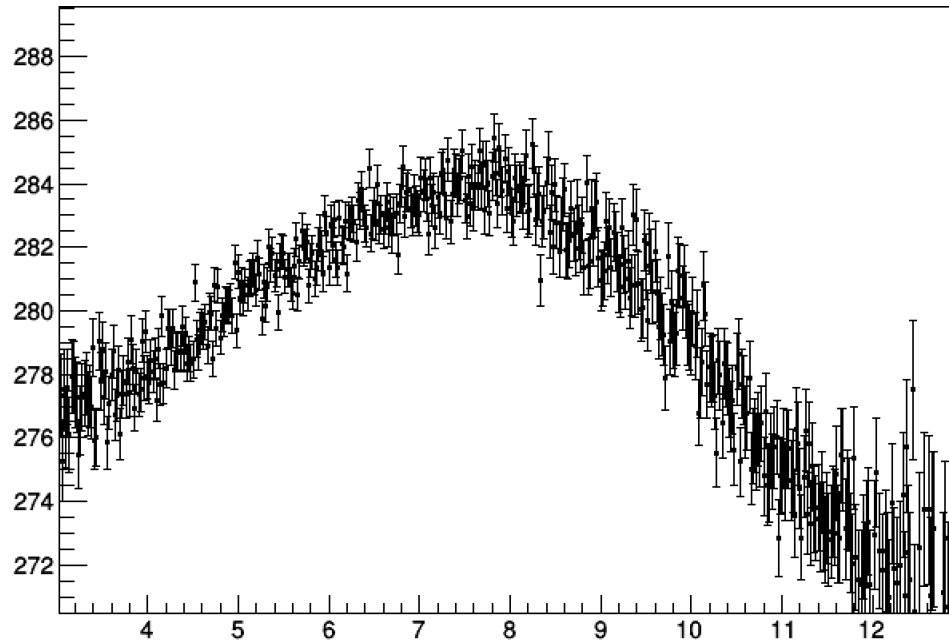
amplitude



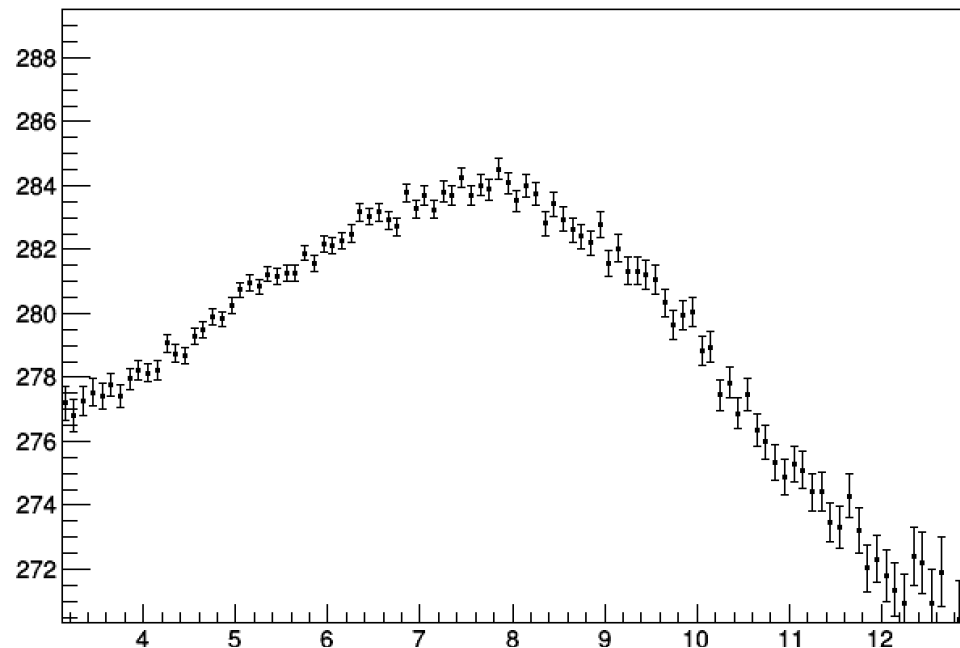
Modulated VS non modulated



Investigate binning effects (125 uT, non mod., up)



Time bin = 20 μ s



Time bin = 100 μ s

→ no difference

Simulation (as from: Piegsa - NIM A 589 (2008) 318)



$$B_0(1) = 158 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 4608 \text{ Hz}\right)$$

$B_0(2) = \text{variable}$

$$B_0(3) = 110 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3208 \text{ Hz}\right)$$

$$B_1(1) = B_1(3) = 25 \mu\text{T}$$

$\omega = \text{variable}$

$$B_0 (1) = 158 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 4608 \text{ Hz}\right)$$

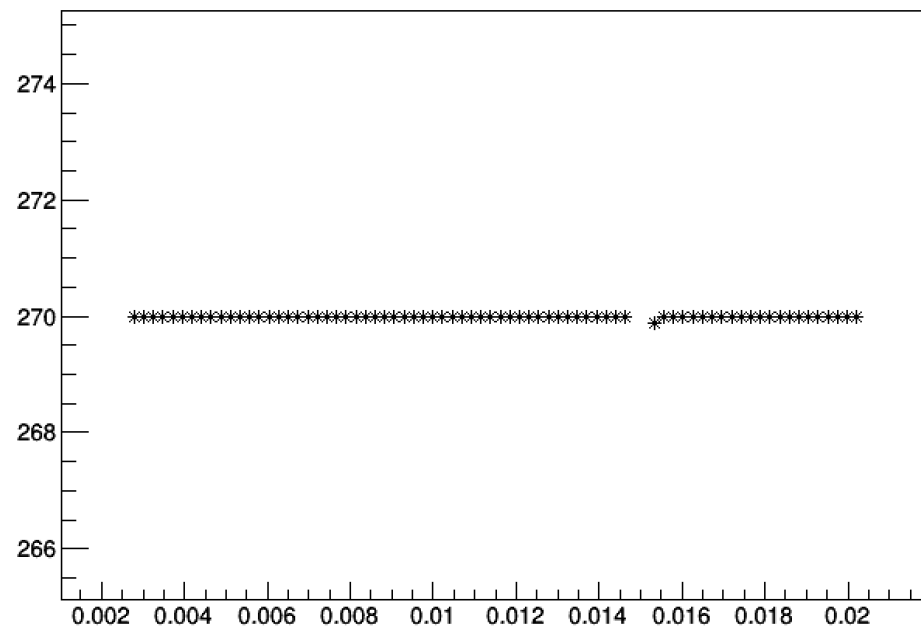
$$B_0 (2) = 134 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3908 \text{ Hz}\right)$$

$$B_0 (3) = 110 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3208 \text{ Hz}\right)$$

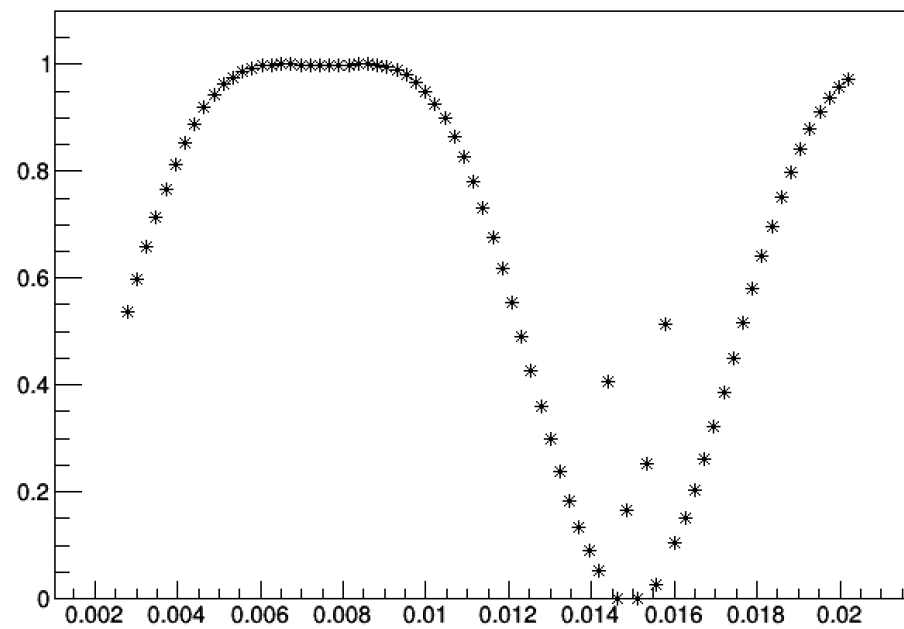
$$B_1 (1) = B_1 (3) = 25 \mu\text{T}$$

$$\omega = 3908 * 2\pi$$

phase



amplitude



$$B_0(1) = 158 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 4608 \text{ Hz}\right)$$

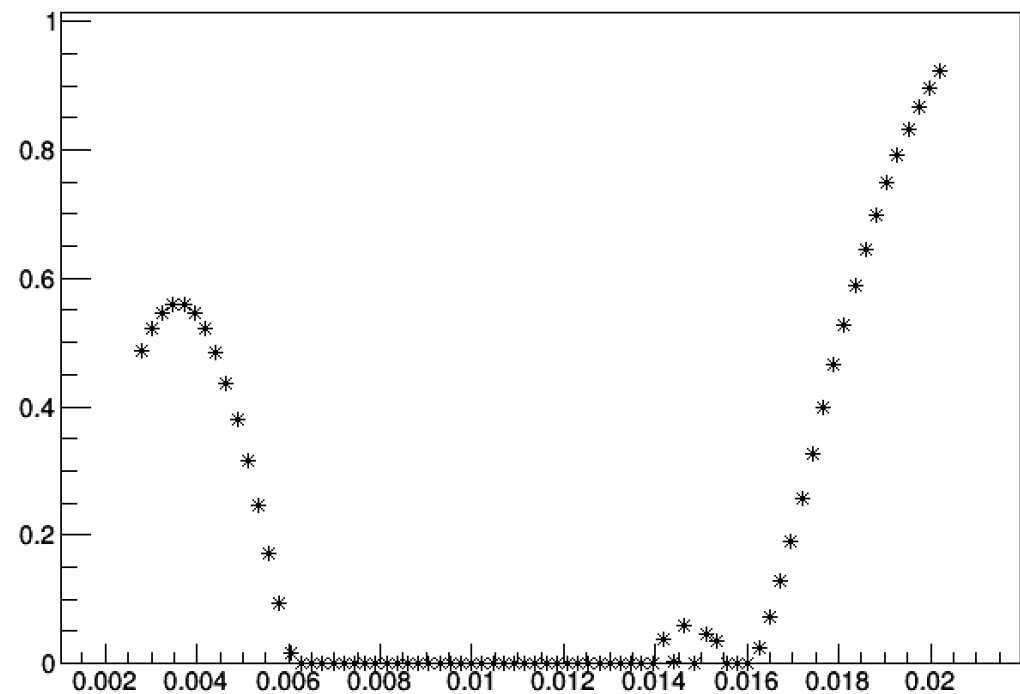
$$B_0(2) = 134 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3908 \text{ Hz}\right)$$

$$B_0(3) = 110 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3208 \text{ Hz}\right)$$

$$B_1(1) = B_1(3) = 25 \mu\text{T}$$

$$\omega = 3800 * 2\pi$$

amplitude



$$B_0 (1) = 158 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 4608 \text{ Hz}\right)$$

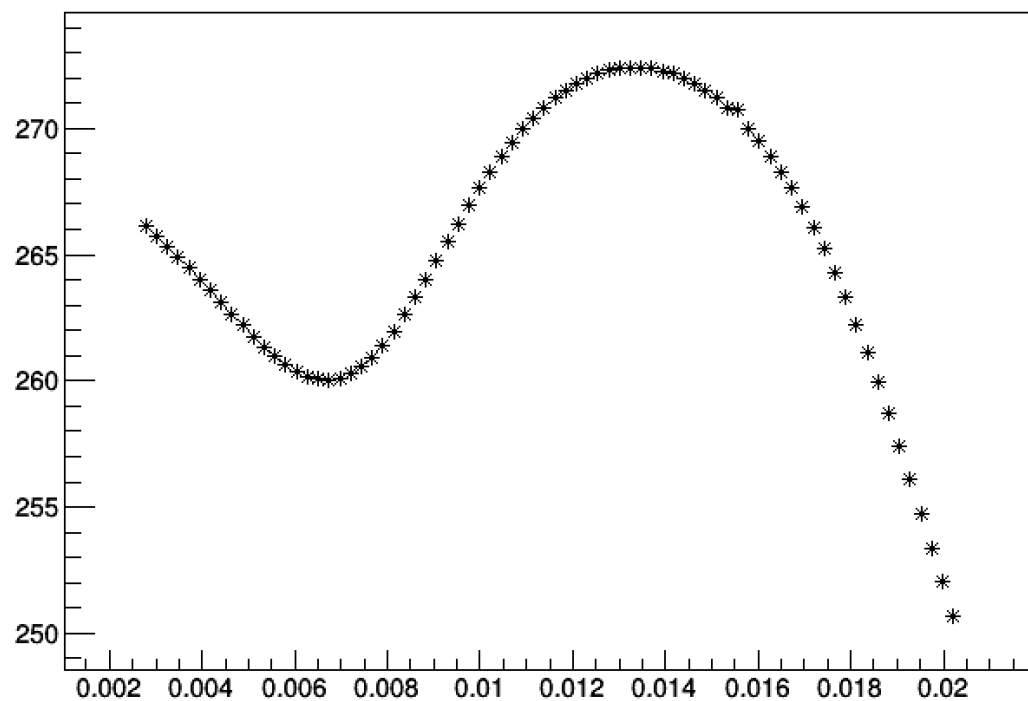
$$B_0 (2) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

$$B_0 (3) = 110 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3208 \text{ Hz}\right)$$

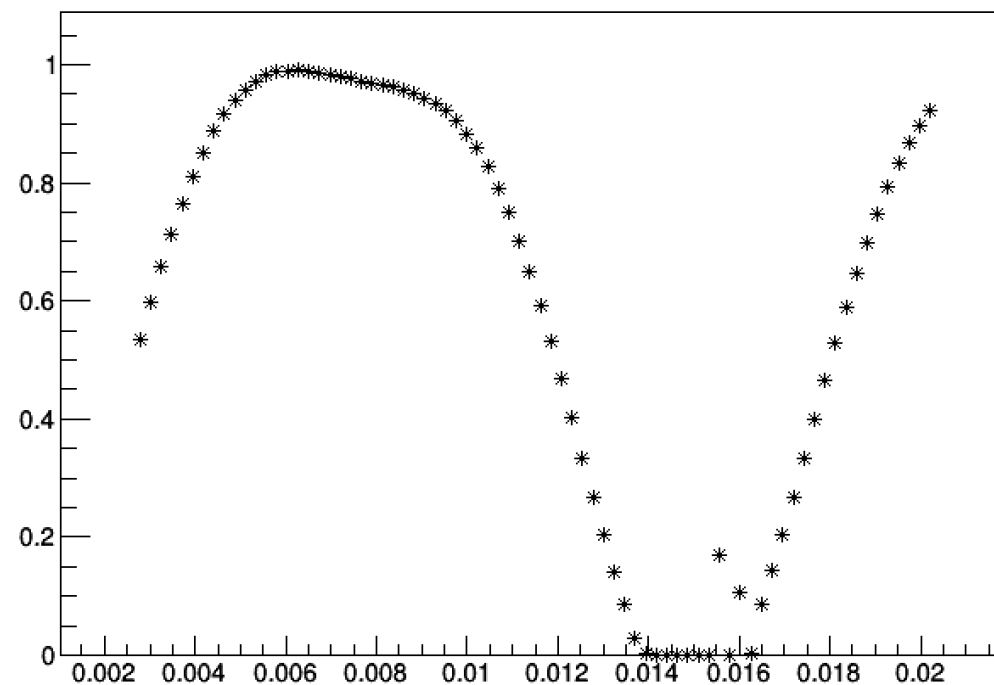
$$B_1 (1) = B_1 (3) = 25 \mu\text{T}$$

$$\omega = 3800 * 2\pi$$

phase



amplitude



$$B_0 (1) = 157 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 4579 \text{ Hz}\right)$$

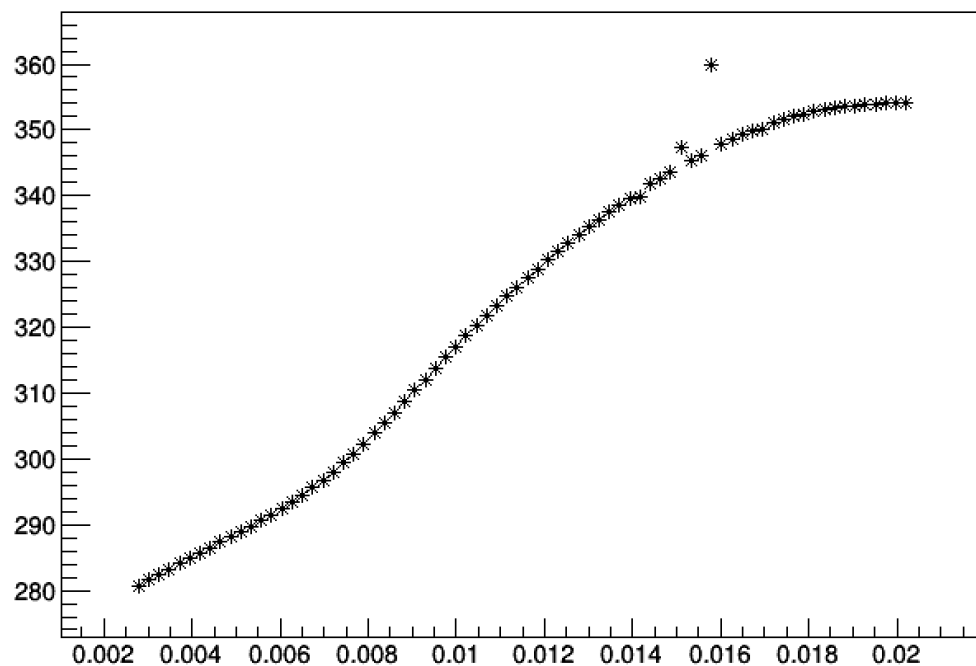
$$B_0 (2) = 129 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3762 \text{ Hz}\right)$$

$$B_0 (3) = 109 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3179 \text{ Hz}\right)$$

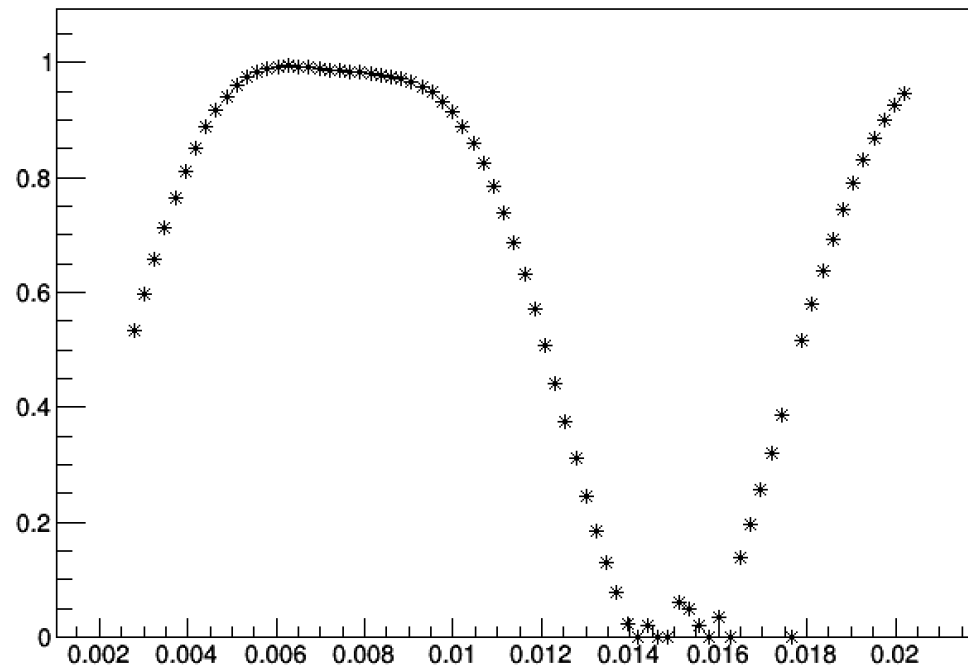
$$B_1 (1) = B_1 (3) = 25 \mu\text{T}$$

$$\omega = 3800 * 2\pi$$

phase



amplitude



$$B_0 (1) = 130.1 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3794 \text{ Hz}\right)$$

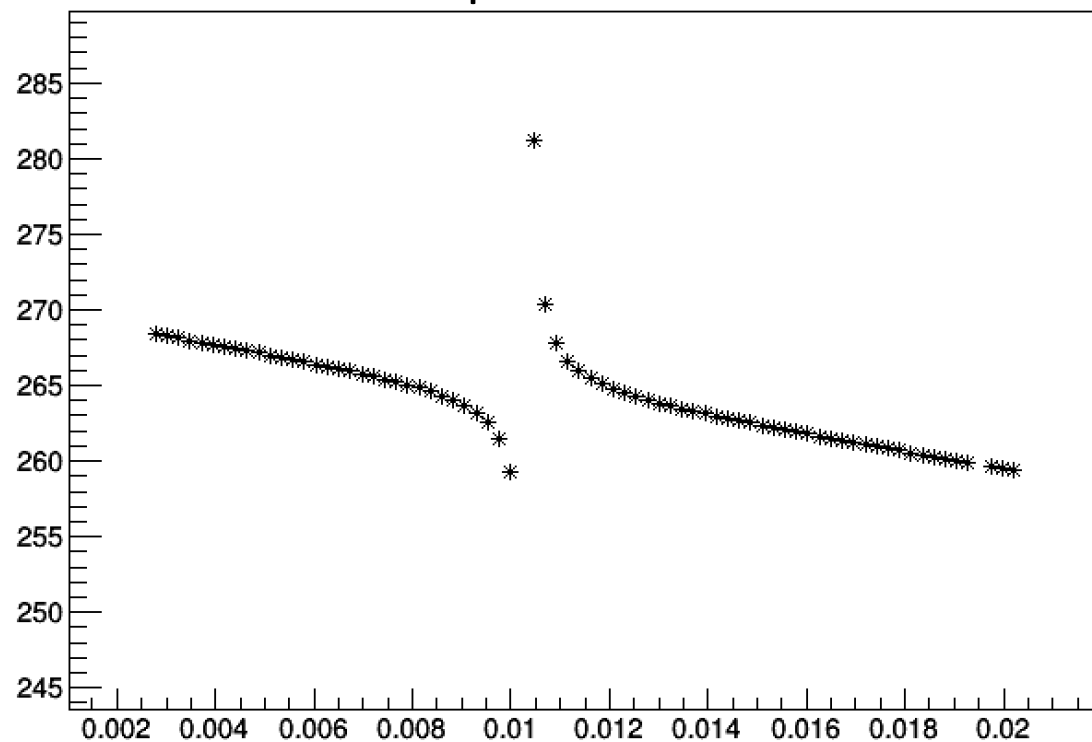
$$B_0 (2) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

$$B_0 (3) = 129.8 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3786 \text{ Hz}\right)$$

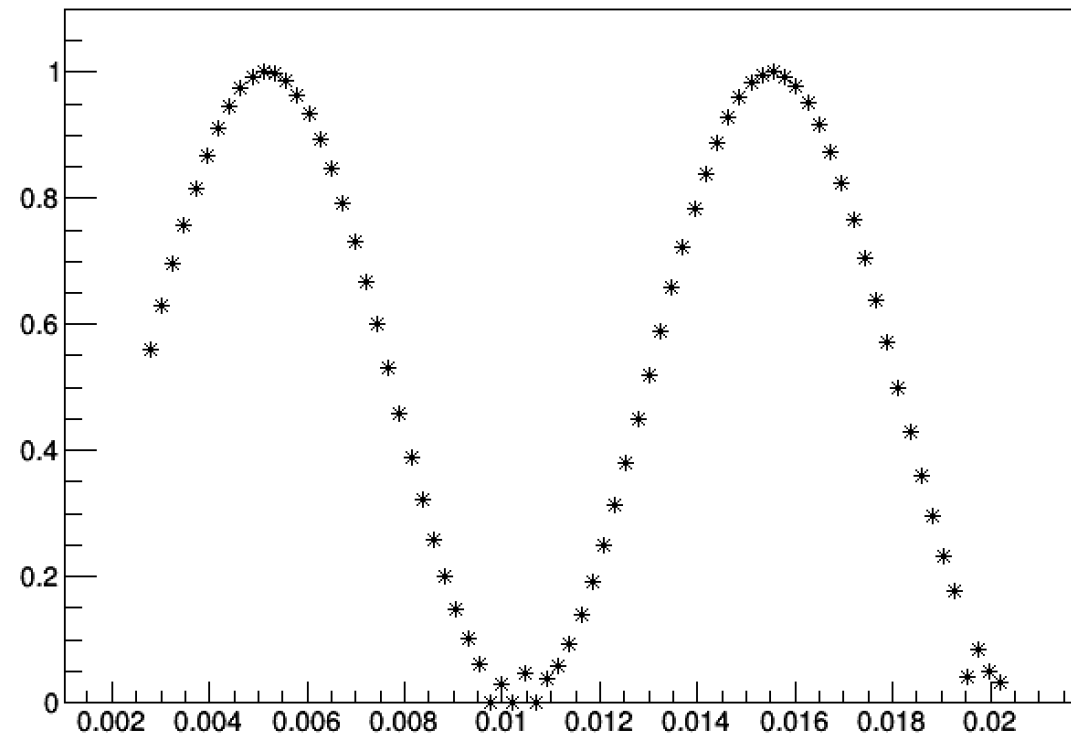
$$B_1 (1) = B_1 (3) = 25 \mu\text{T}$$

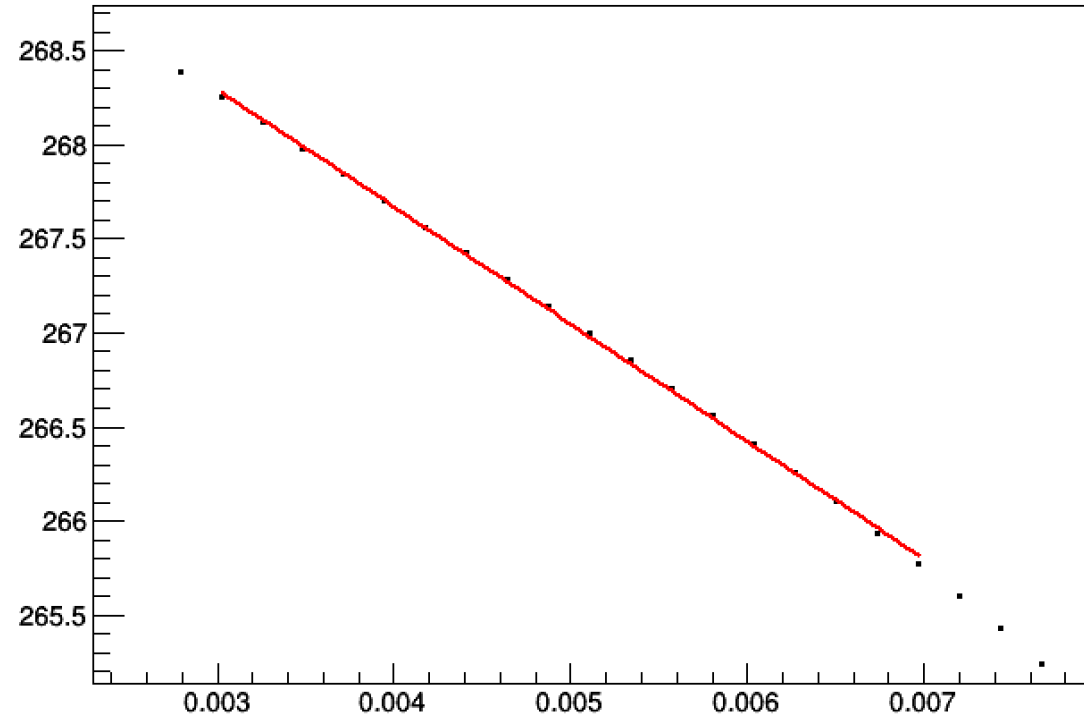
$$\omega = 3788 * 2\pi$$

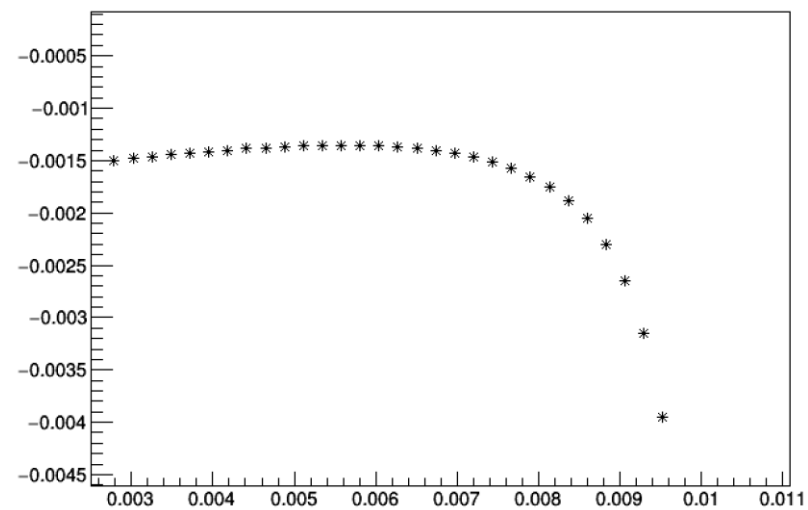
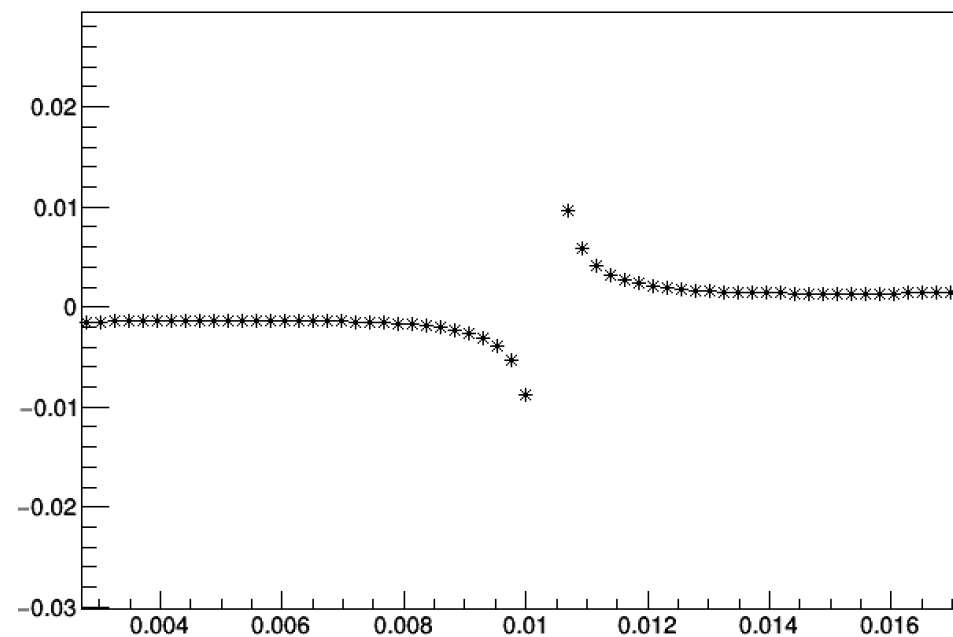
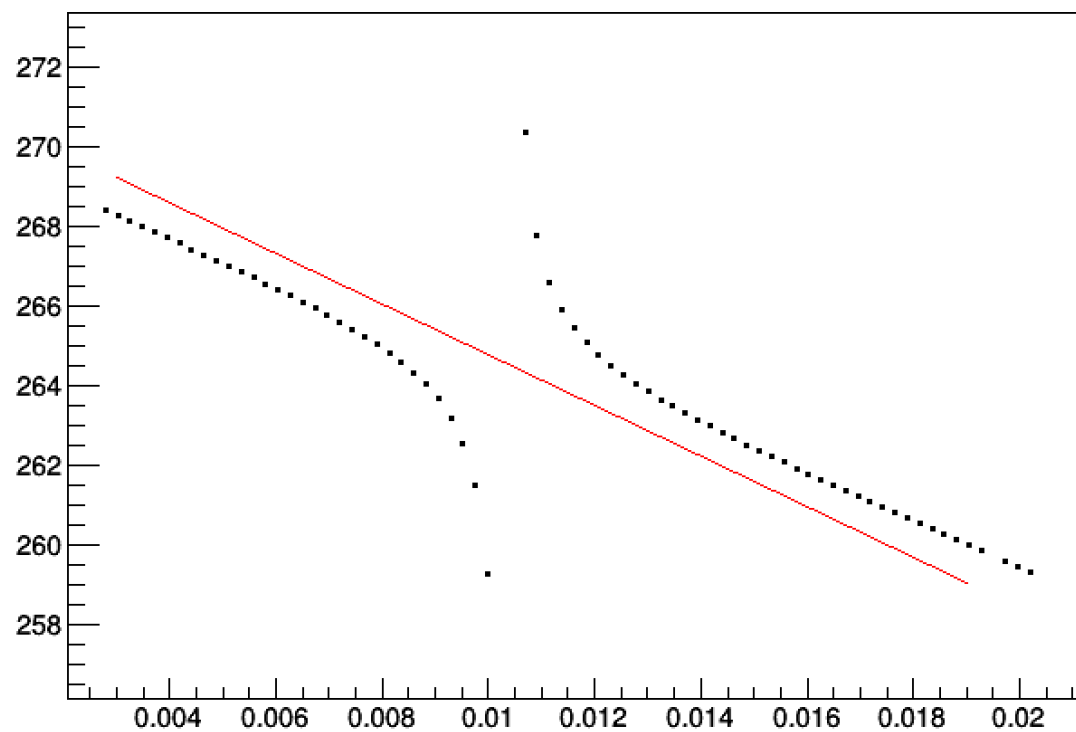
phase



amplitude







$$B_0 (1) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

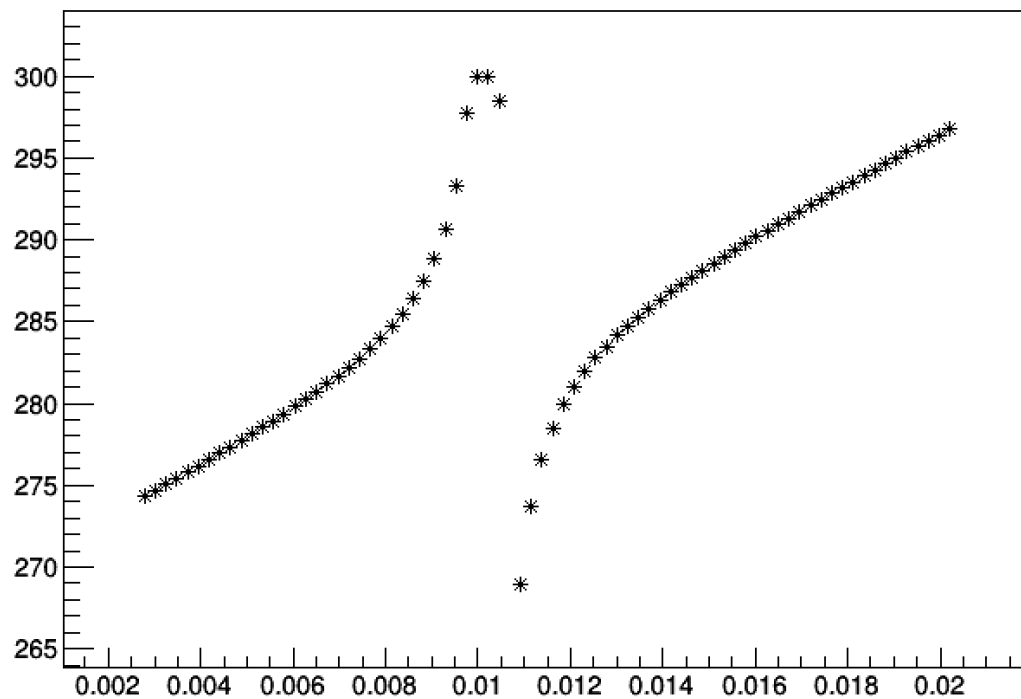
$$B_0 (2) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

$$B_0 (3) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

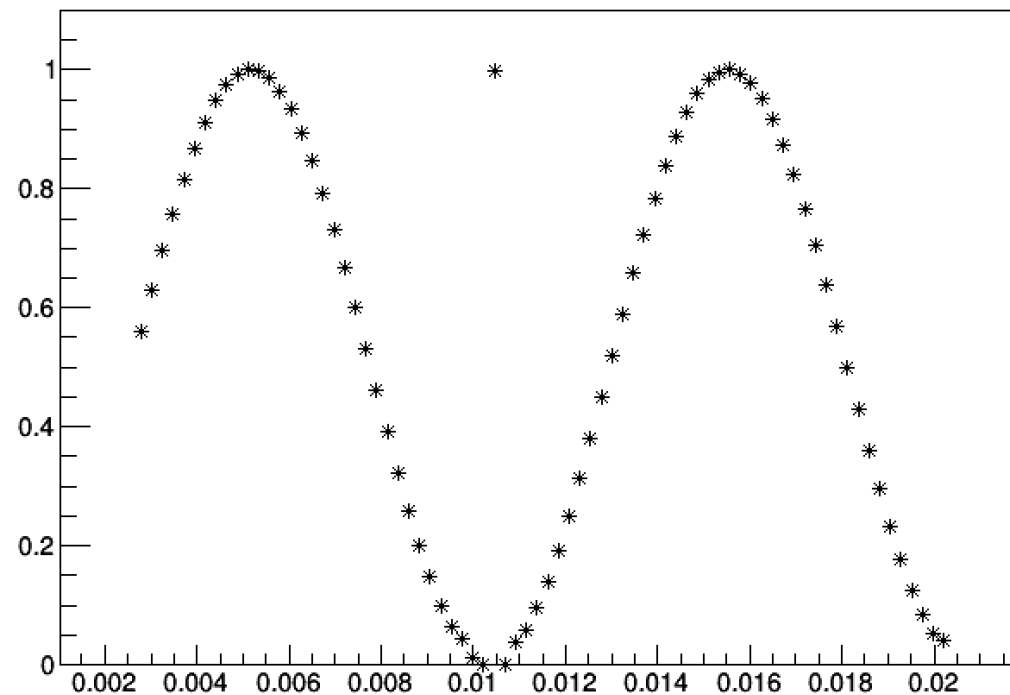
$$B_1 (1) = B_1 (3) = 25 \mu\text{T}$$

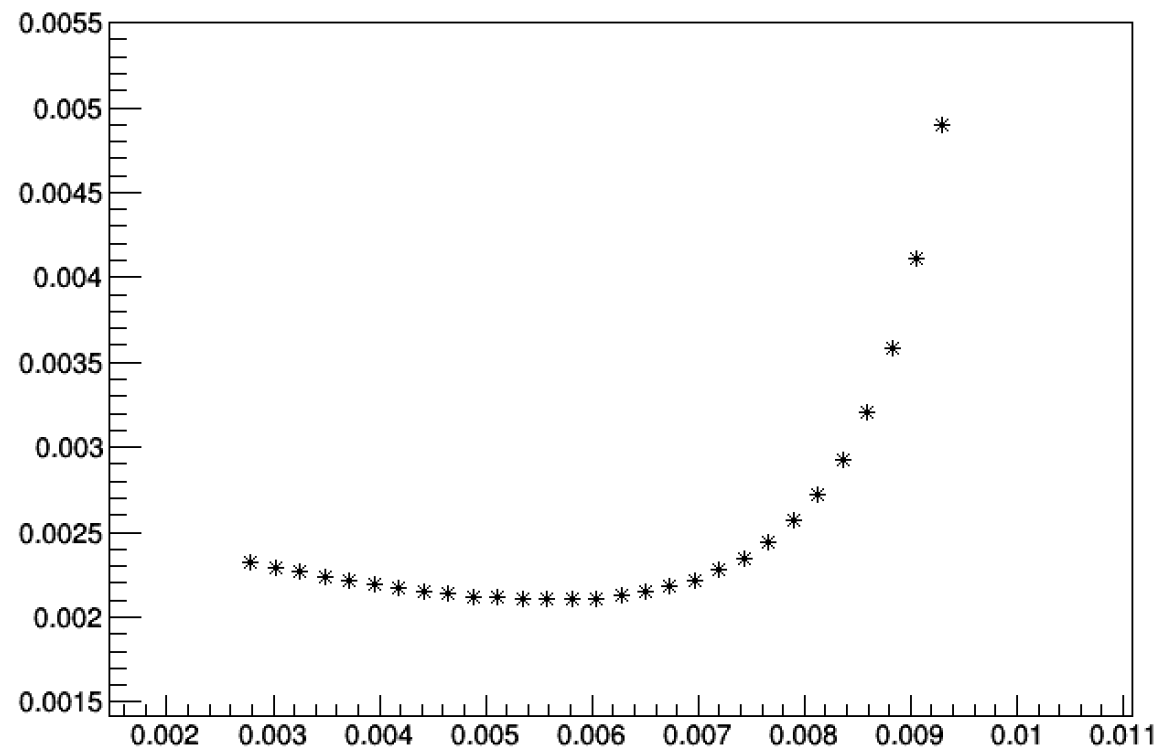
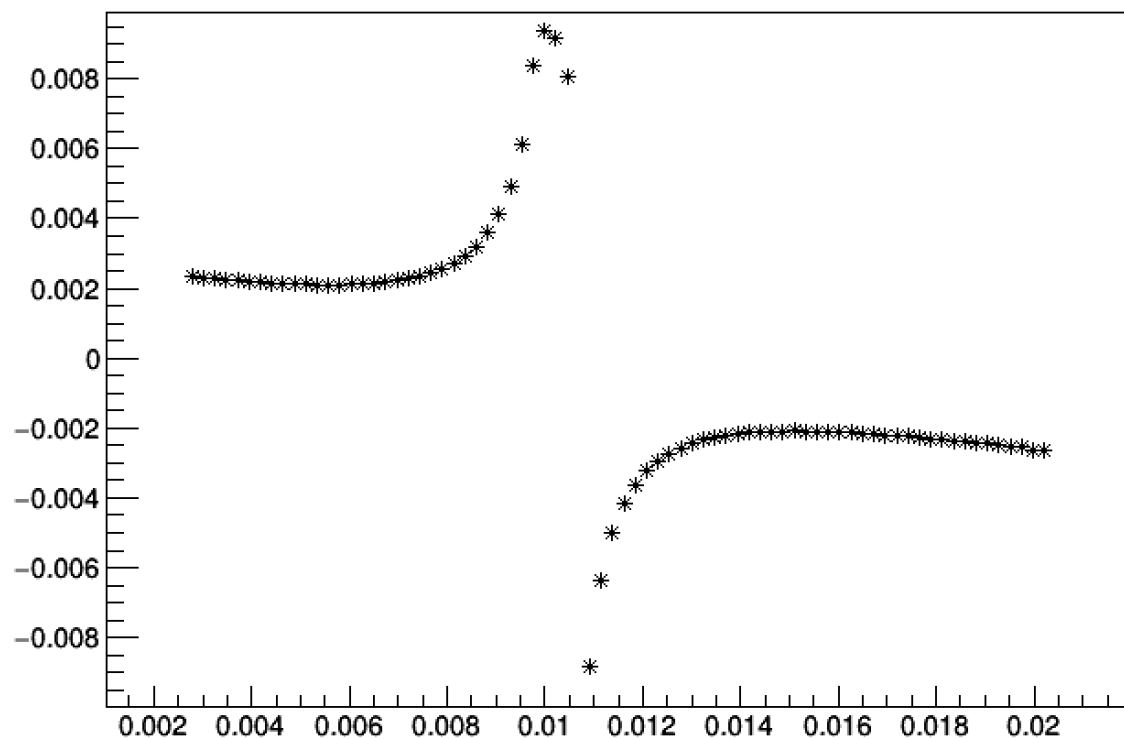
$$\omega = 3800 * 2\pi$$

phase



amplitude





$$B_0(1) = 1300 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37914 \text{ Hz}\right)$$

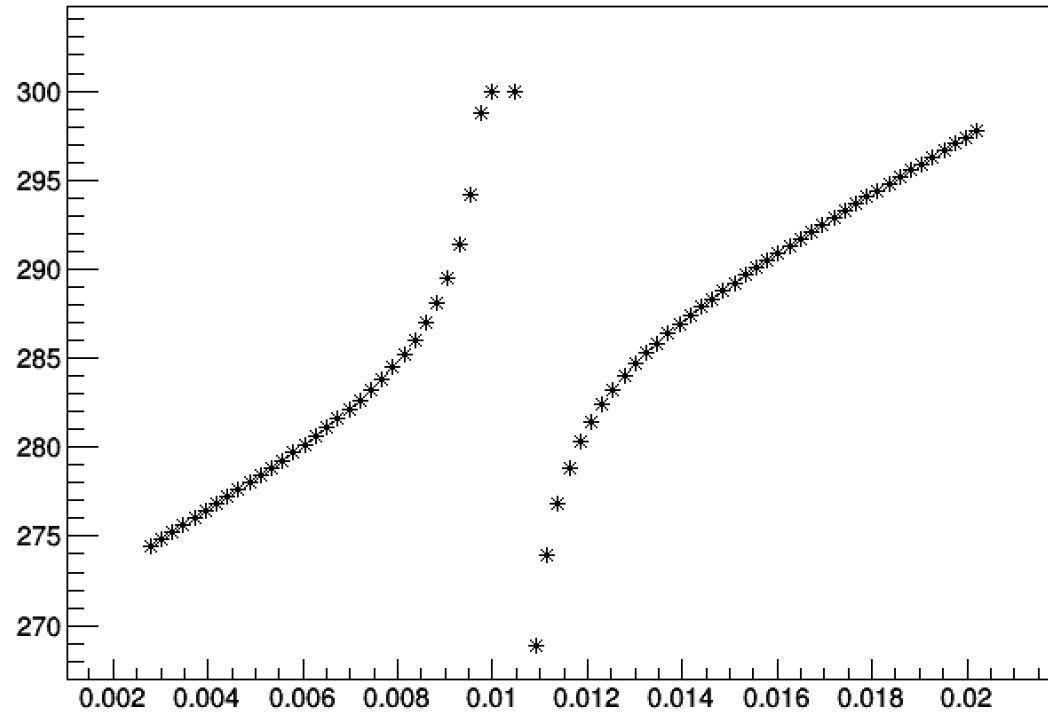
$$B_0(2) = 1300 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37914 \text{ Hz}\right)$$

$$B_0(3) = 1300 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37914 \text{ Hz}\right)$$

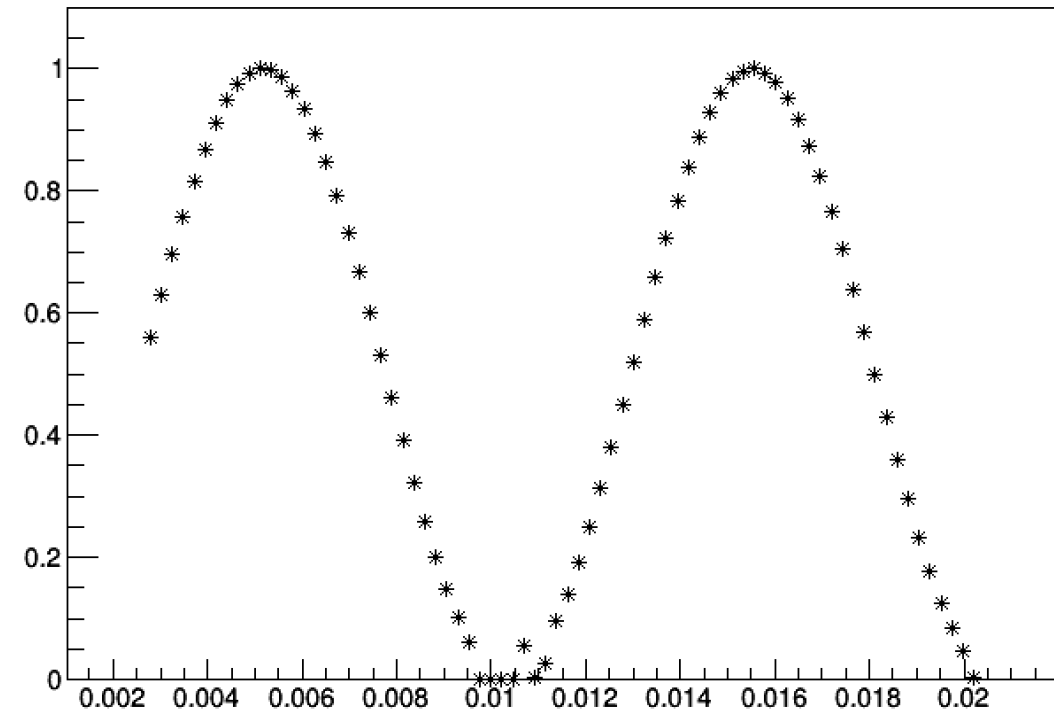
$$B_1(1) = B_1(3) = 25 \mu\text{T}$$

$$\omega = 37920 * 2\pi \quad (\text{same } \omega - \omega_0(2))$$

phase



amplitude



$$B_0(1) = 1300.1 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37917 \text{ Hz}\right) \quad (\text{same } \omega_0(1) - \omega_0(2))$$

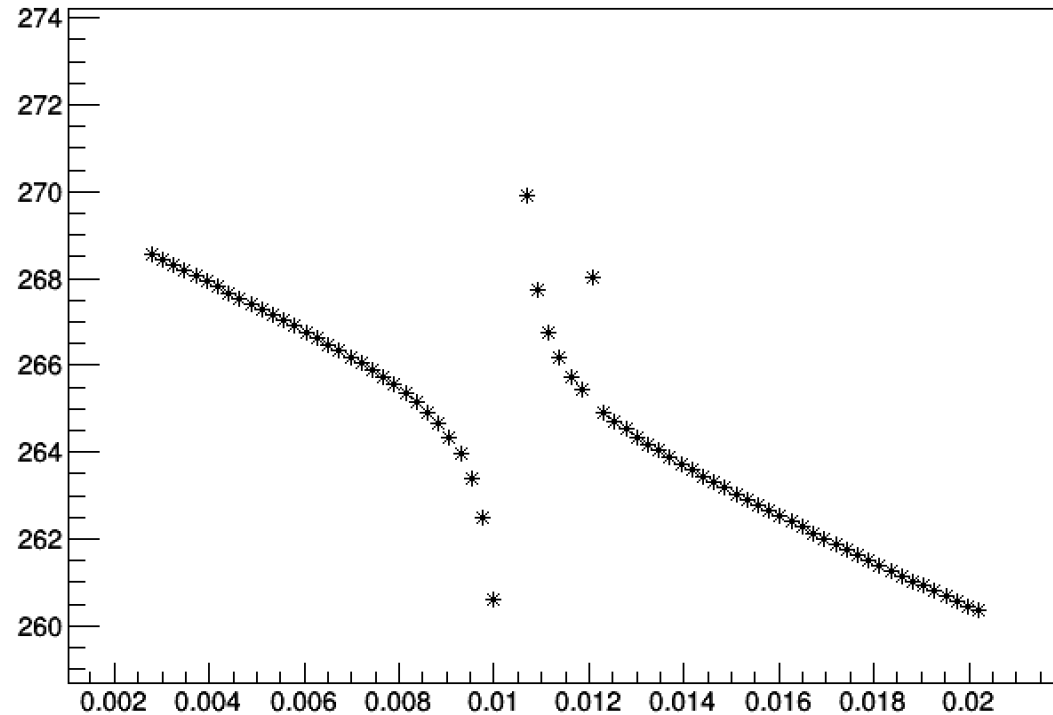
$$B_0(2) = 1300.0 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37914 \text{ Hz}\right)$$

$$B_0(3) = 1299.8 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37908 \text{ Hz}\right) \quad (\text{same } \omega_0(3) - \omega_0(2))$$

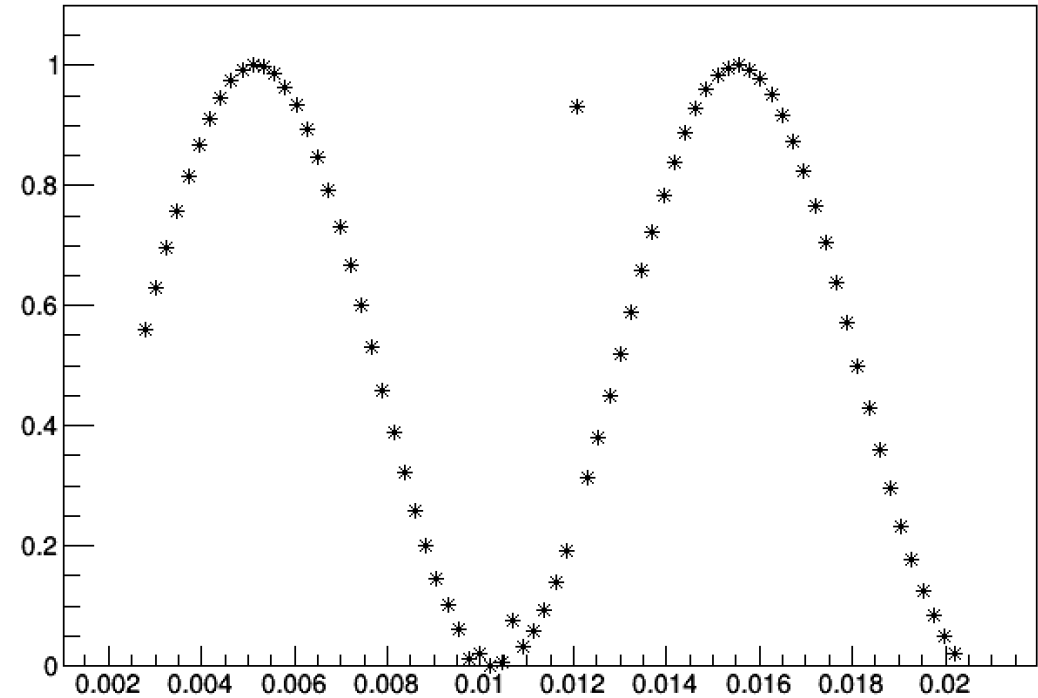
$$B_1(1) = B_1(3) = 25 \mu\text{T}$$

$$\omega = 37911 * 2\pi \quad (\text{same } \omega - \omega_0(2))$$

phase



amplitude



$$B_0(1) = 1300.1 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37917 \text{ Hz}\right) \quad (\text{same } \omega_0(1) - \omega_0(2))$$

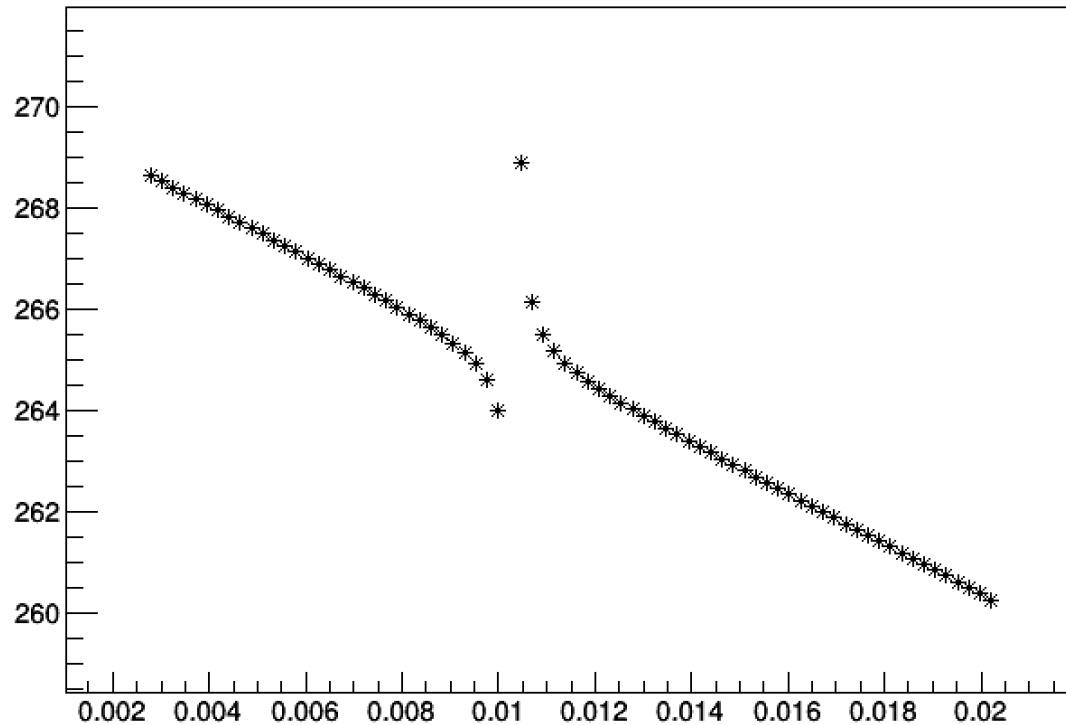
$$B_0(2) = 1300.0 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37914 \text{ Hz}\right)$$

$$B_0(3) = 1299.8 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37908 \text{ Hz}\right) \quad (\text{same } \omega_0(3) - \omega_0(2))$$

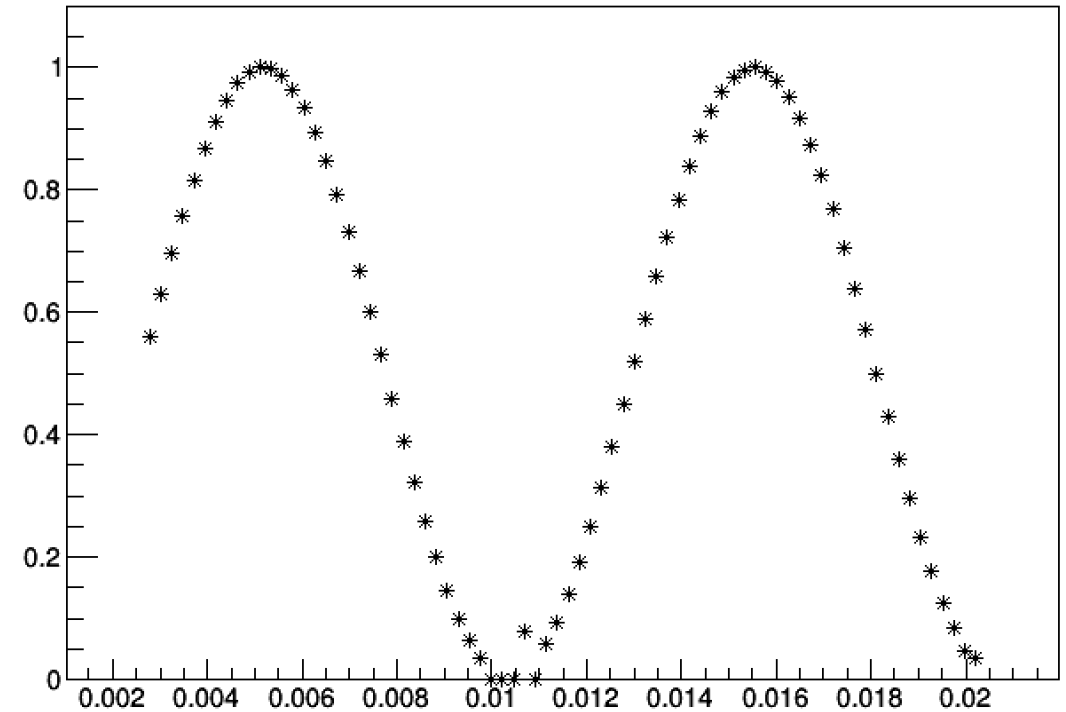
$$B_1(1) = B_1(3) = 100 \mu\text{T} \quad \text{and SF length} = 10 \text{ cm (instead of 40)}$$

$$\omega = 37911 * 2\pi \quad (\text{same } \omega - \omega_0(2))$$

phase



amplitude



$$B_0 (1) = 1300.1 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37917 \text{ Hz}\right)$$

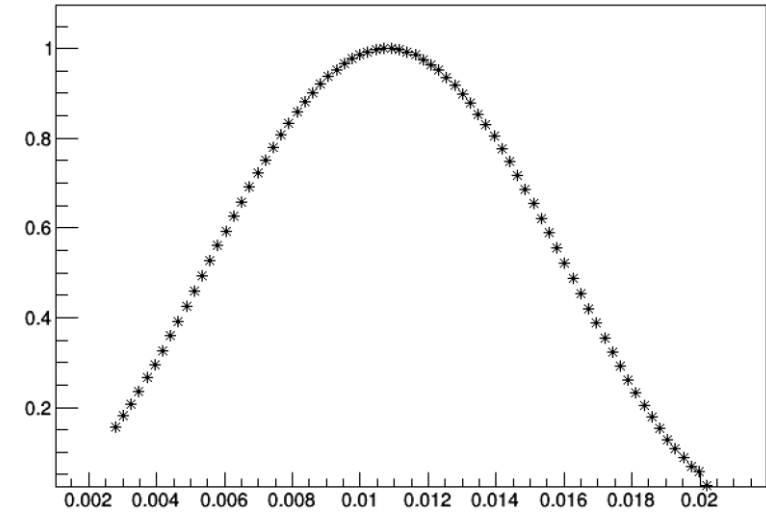
$$B_0 (2) = 1300.0 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37914 \text{ Hz}\right)$$

$$B_0 (3) = 1299.8 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 37908 \text{ Hz}\right)$$

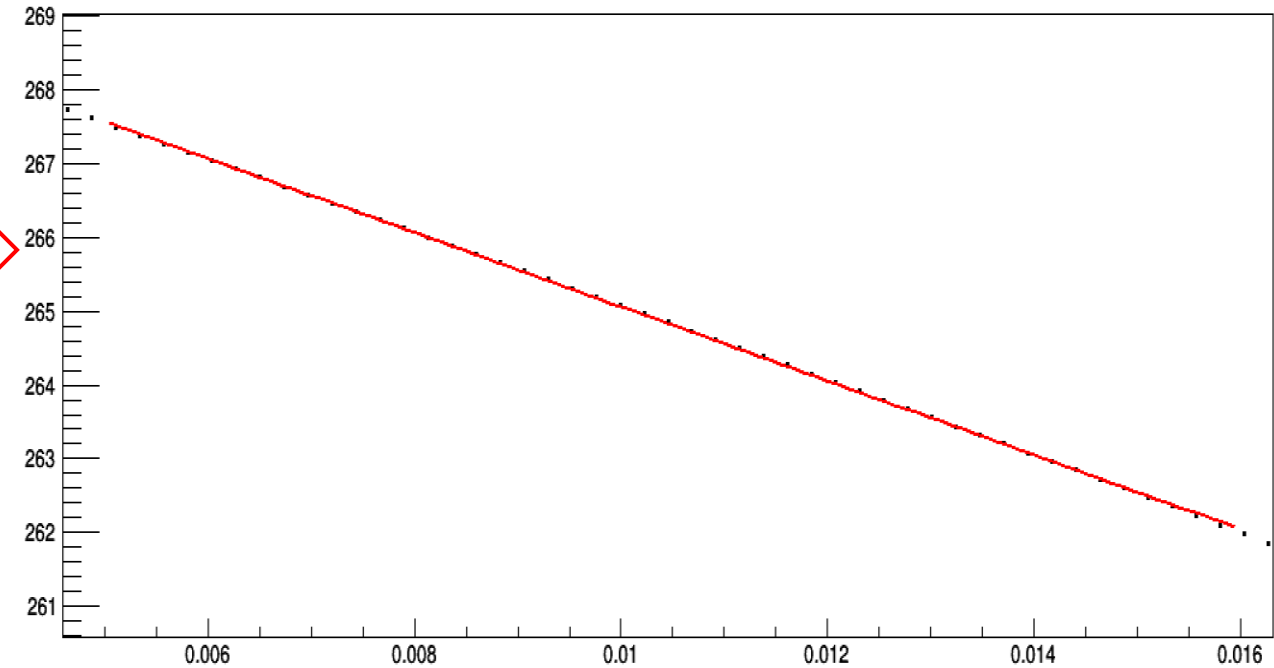
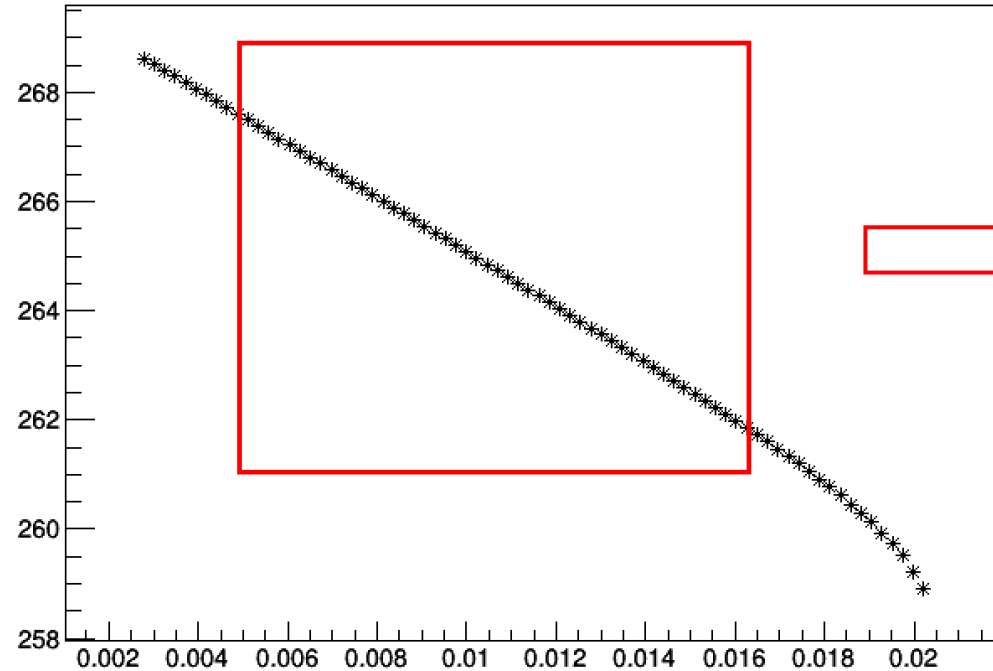
$$B_1 (1) = B_1 (3) = 48 \mu\text{T} \quad \text{and SF length} = 10 \text{ cm}$$

$$\omega = 37911 * 2\pi$$

amplitude



phase



Simulation status:

1) Rotating frame

- Analytical tool (constant fields, as from NIM A 589 (2008) 318–329)
- “Multi-matrices tool” (time dependent intensity NIM A 786 (2015) 71–77)

2) Abs. system with multi-matrices approach (any $B(t)$ field) (under test, Rabi scan seems ok)

Rabi scan (abs. sys.)

$$B_x = 2B_1 \cos(\omega t + \varphi)$$

(phase-averaged results)

spin flipper length = 40 cm

neutron velocity = 700 m/s (5.65 Å)

spin flipper crossing time = 571 μs

$B_0 = 130 \mu\text{T}$ ($\omega_0 = -\gamma B_0 = 23822$)

$B_1 = -\pi/(\tau * \gamma) = 30 \mu\text{T}$ ($\omega_1 = -\gamma B_1 = 5498$)

Rabi formula with $\Delta = \omega - \omega'_0$

$$\mathcal{P}_{\text{Rabi}}(\Delta) = \frac{\omega_1^2}{\Delta^2 + \omega_1^2} \sin^2 \left(\frac{\tau}{2} \cdot \sqrt{\Delta^2 + \omega_1^2} \right)$$

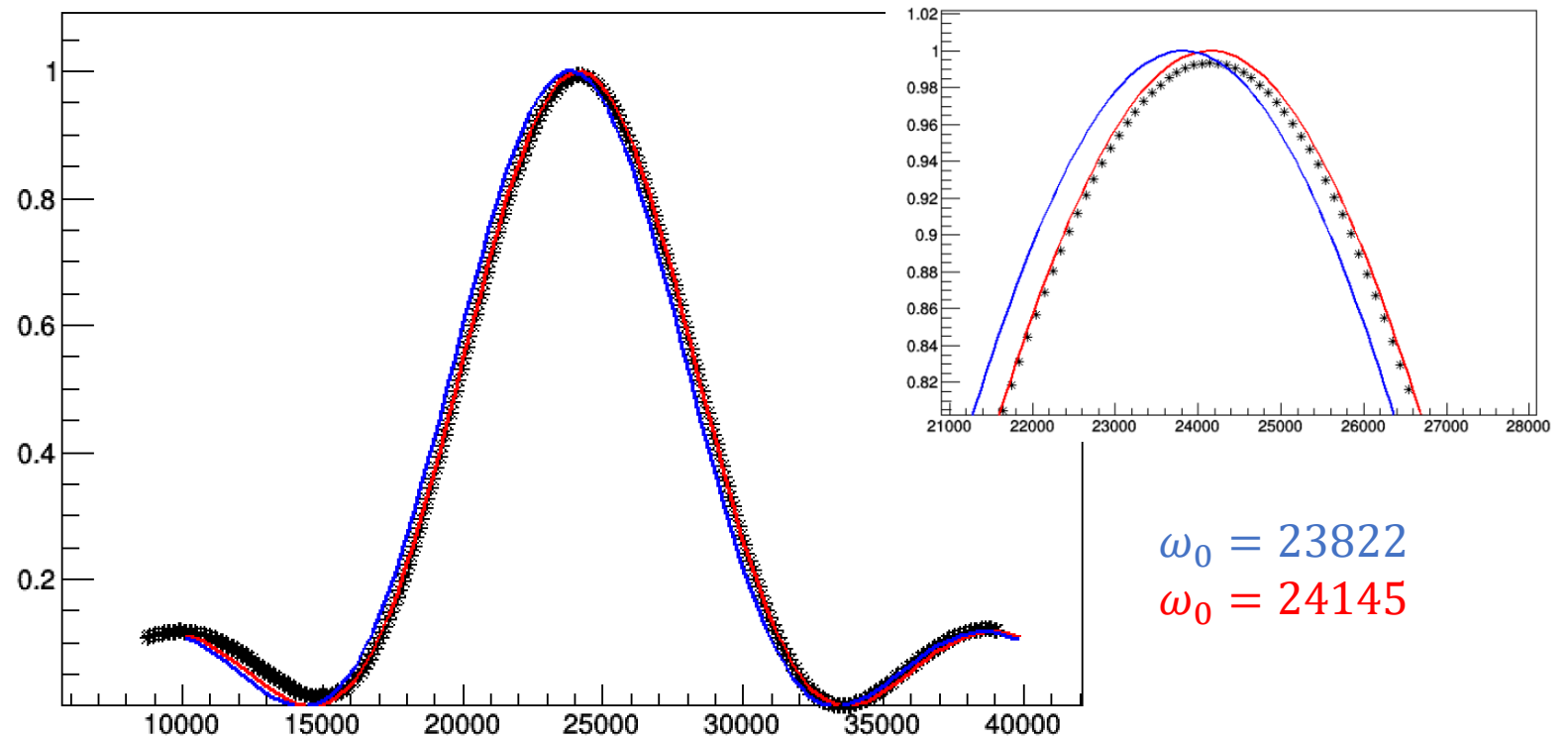
Bloch-Siegert frequency shift

$$\omega'_0 = \omega_0 + \delta_{\text{BS}} = \omega_0 \cdot \left(1 + \frac{1}{4} \left(\frac{\omega_1}{\omega_0} \right)^2 \right)$$

Theoretical ω'_0 value = 24139

Observed ω'_0 value = 24145

Max = 0.9935



Ramsey phase scan (abs. sys.)

$$B_0(1) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

$$B_0(2) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

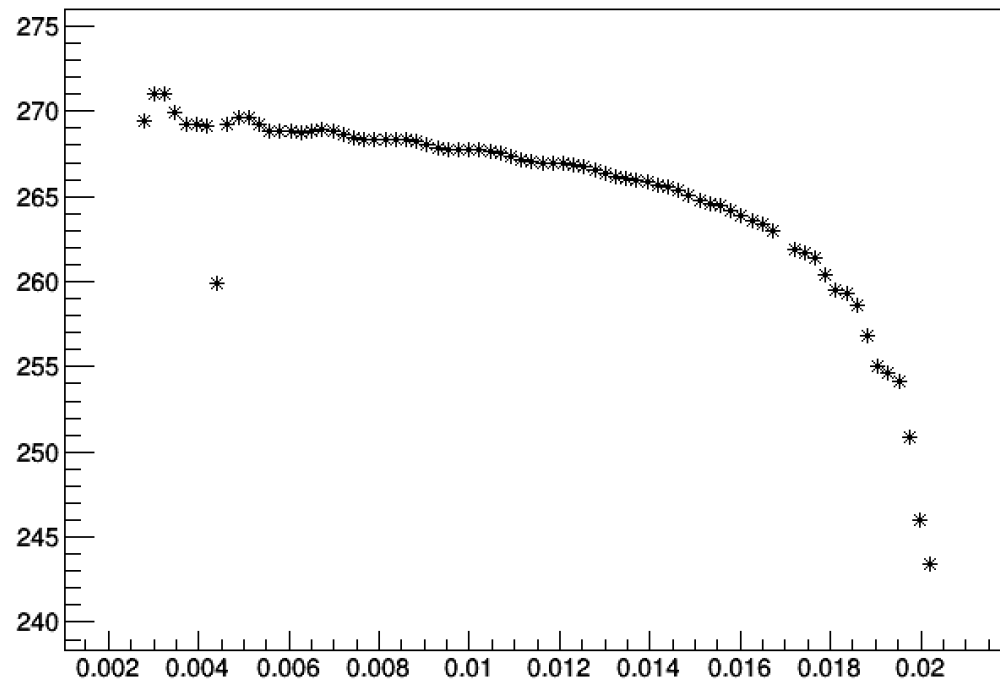
$$B_0(3) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

$$B_1(1) = B_1(3) = 12 \mu\text{T}$$

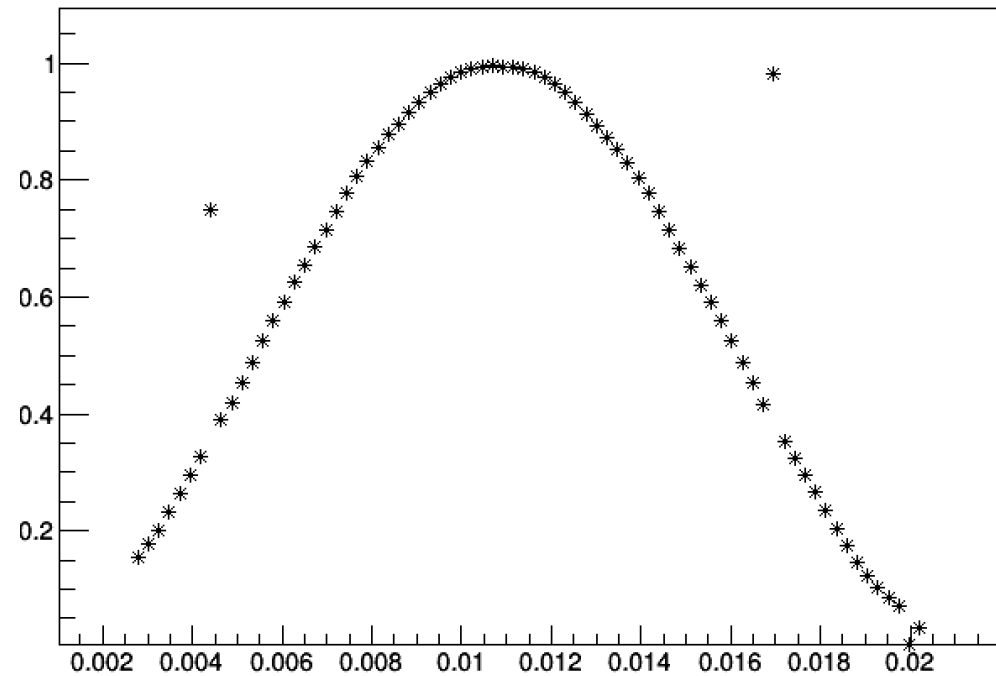
$$\omega = -\gamma B_0(2)$$

(phase-averaged results)

phase



amplitude



Ramsey phase scan (abs. sys.)

$$B_0(1) = 129.75 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3784 \text{ Hz}\right)$$

$$B_0(2) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

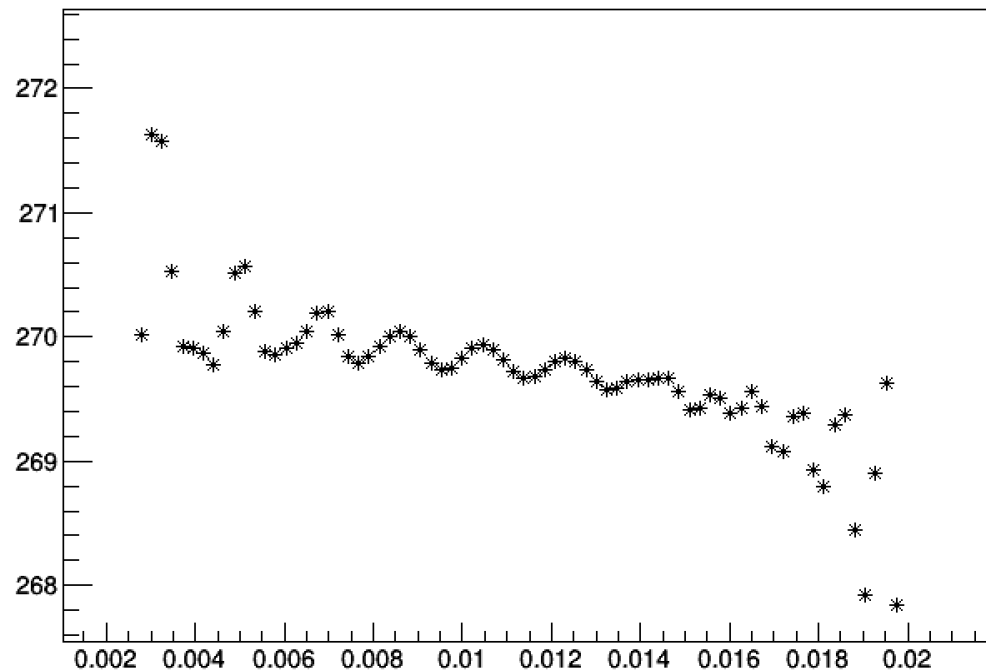
$$B_0(3) = 129.75 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3784 \text{ Hz}\right)$$

$$B_1(1) = B_1(3) = 12 \mu\text{T}$$

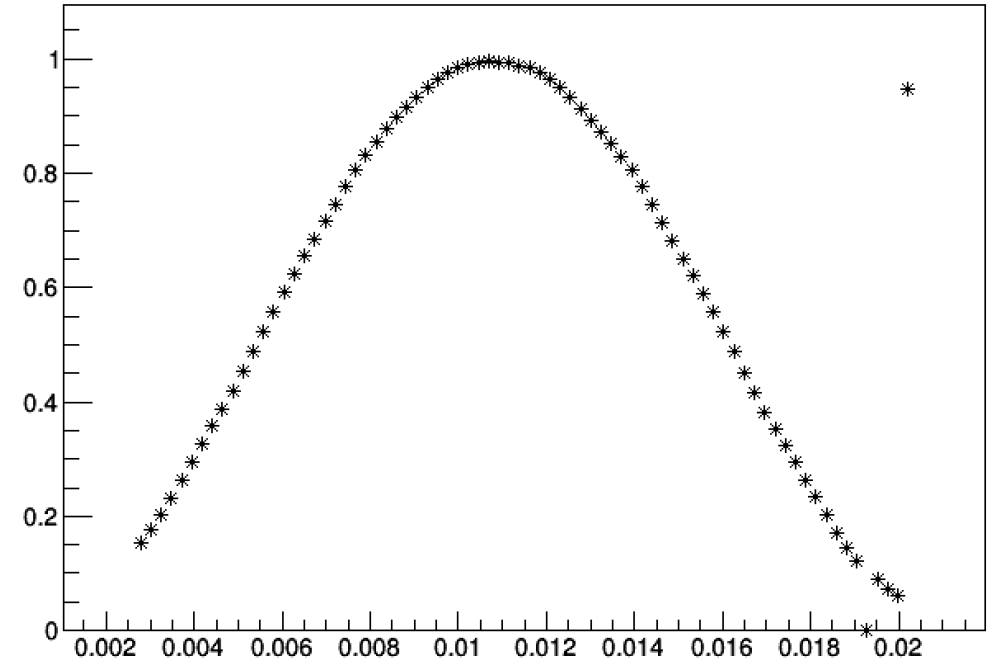
$$\omega = -\gamma B_0(2)$$

(phase-averaged results)

phase



amplitude



Ramsey phase scan (abs. sys.)

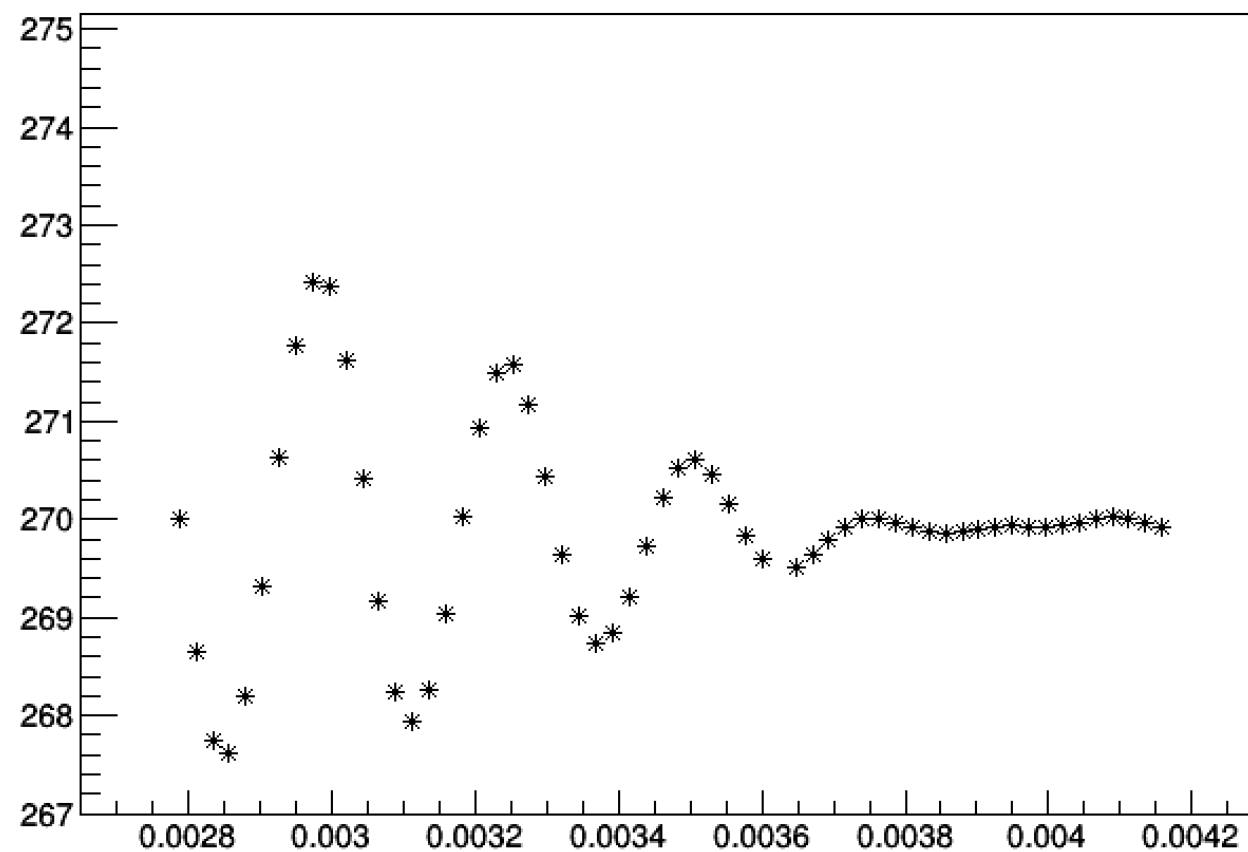
$$B_0(1) = 129.75 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3784 \text{ Hz}\right)$$

$$B_0(2) = 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right)$$

$$B_0(3) = 129.75 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3784 \text{ Hz}\right)$$

$$B_1(1) = B_1(3) = 12 \mu\text{T}$$

$$\omega = -\gamma B_0(2)$$

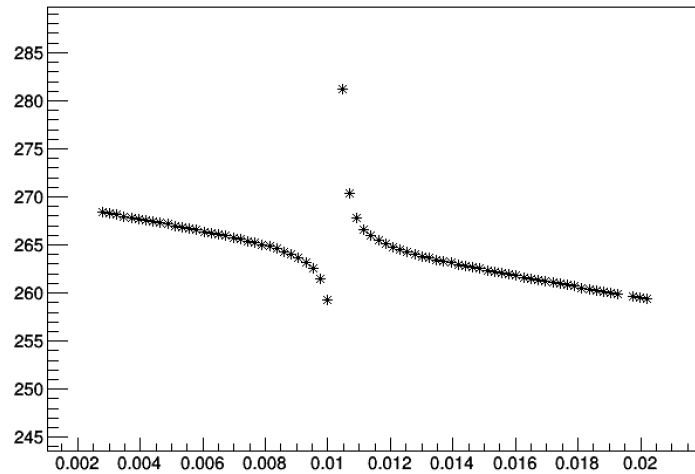


Comparison rot.frame VS abs.sys

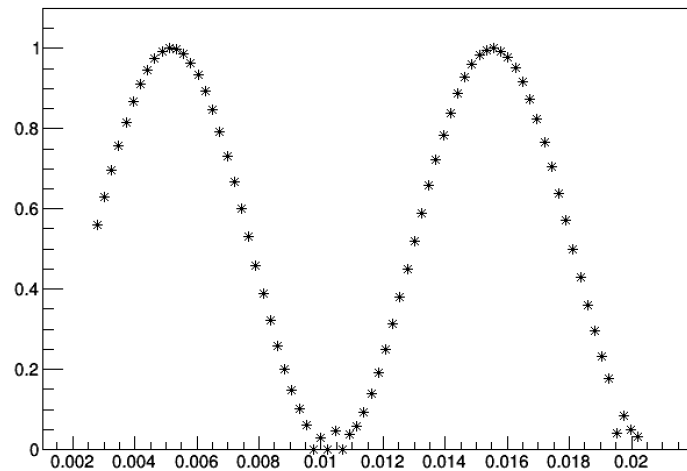
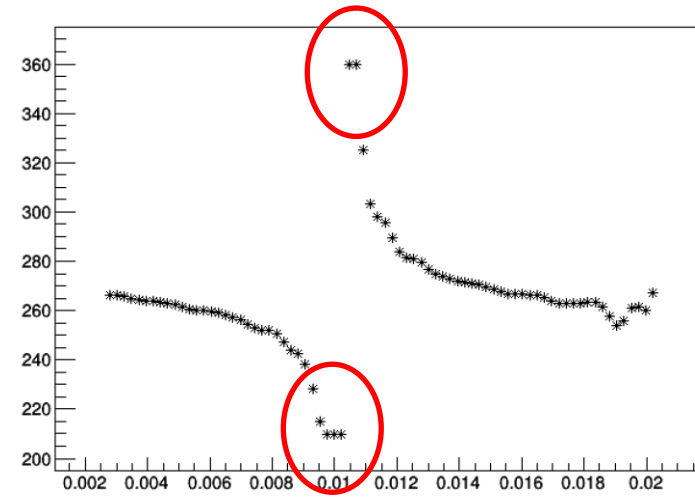
$$\begin{aligned} B0(1) &= 130.1 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3794 \text{ Hz}\right) \\ B0(2) &= 130 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3791 \text{ Hz}\right) \\ B0(3) &= 129.8 \mu\text{T} \quad \left(-\frac{\gamma B_0}{2\pi} = 3786 \text{ Hz}\right) \end{aligned}$$

$$B1(1) = B1(3) = 25 \mu\text{T}$$

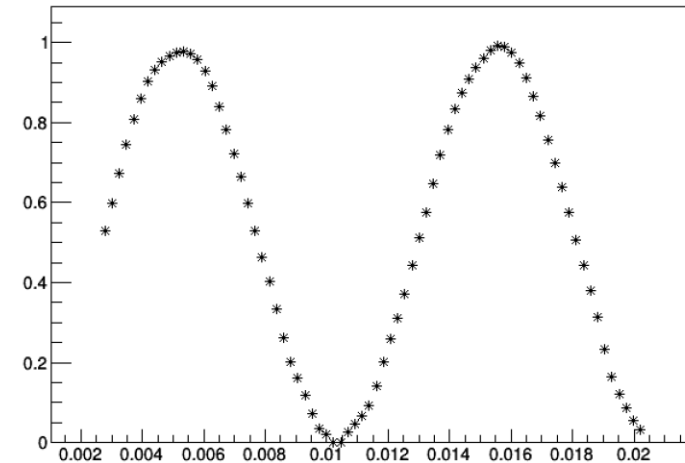
$$\omega = 3788 * 2\pi$$



phase



amplitude

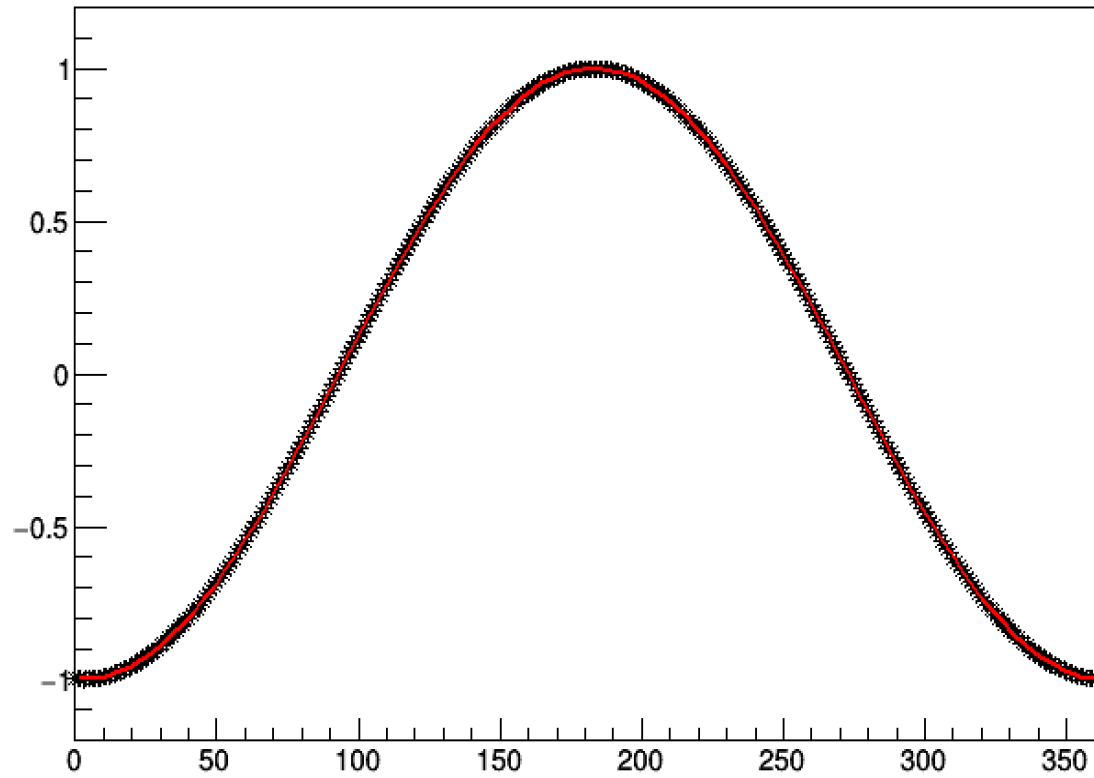


Comparison rot.frame VS abs.sys.

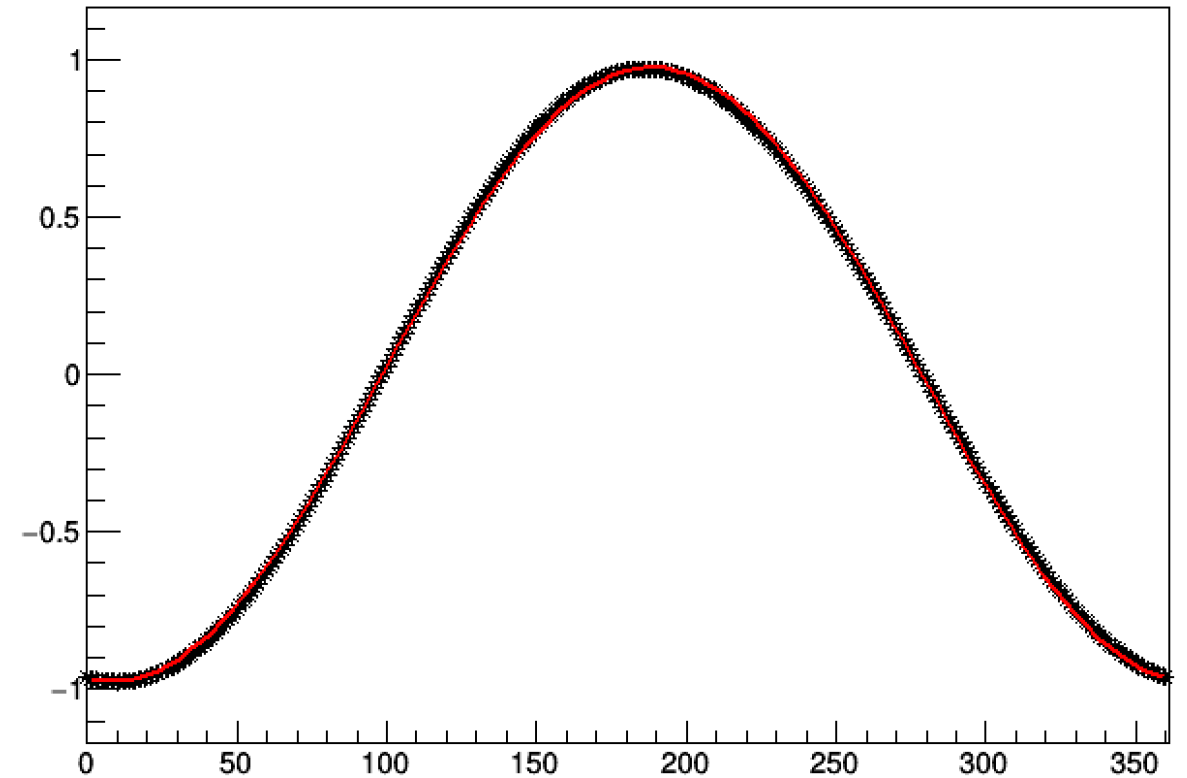
T (free prec. time) = 2.2 ms

$\sim \pi/2$ flip

rot.frame



abs. sys.

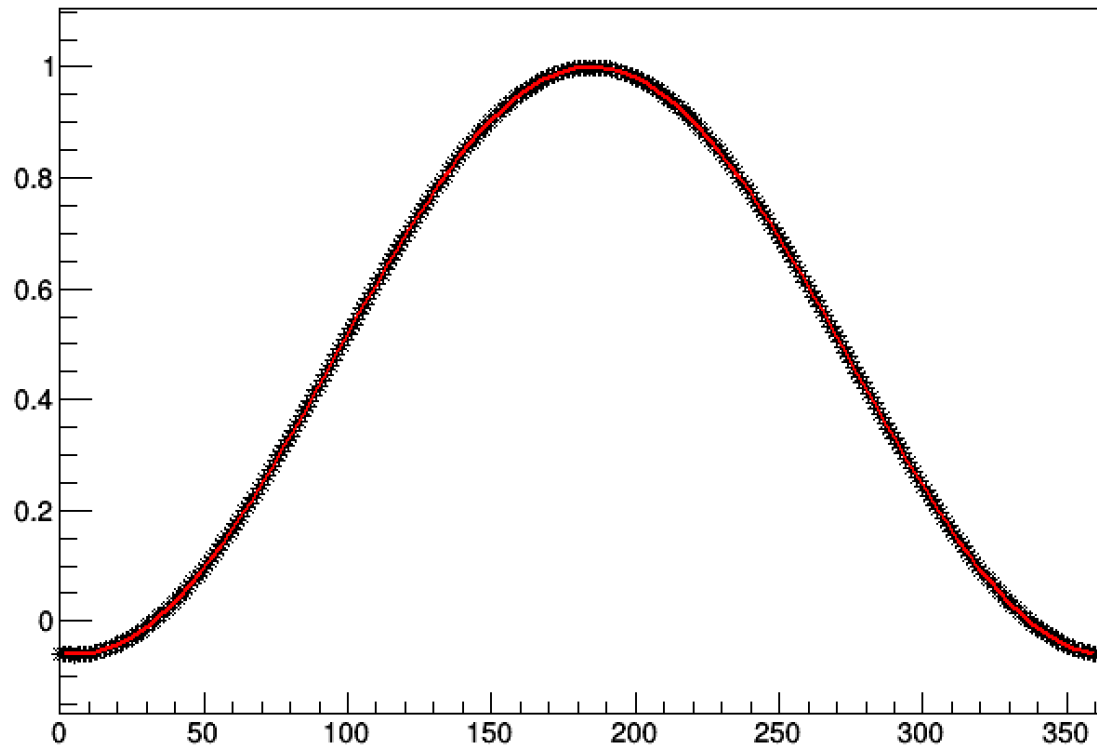


Comparison rot.frame VS abs.sys

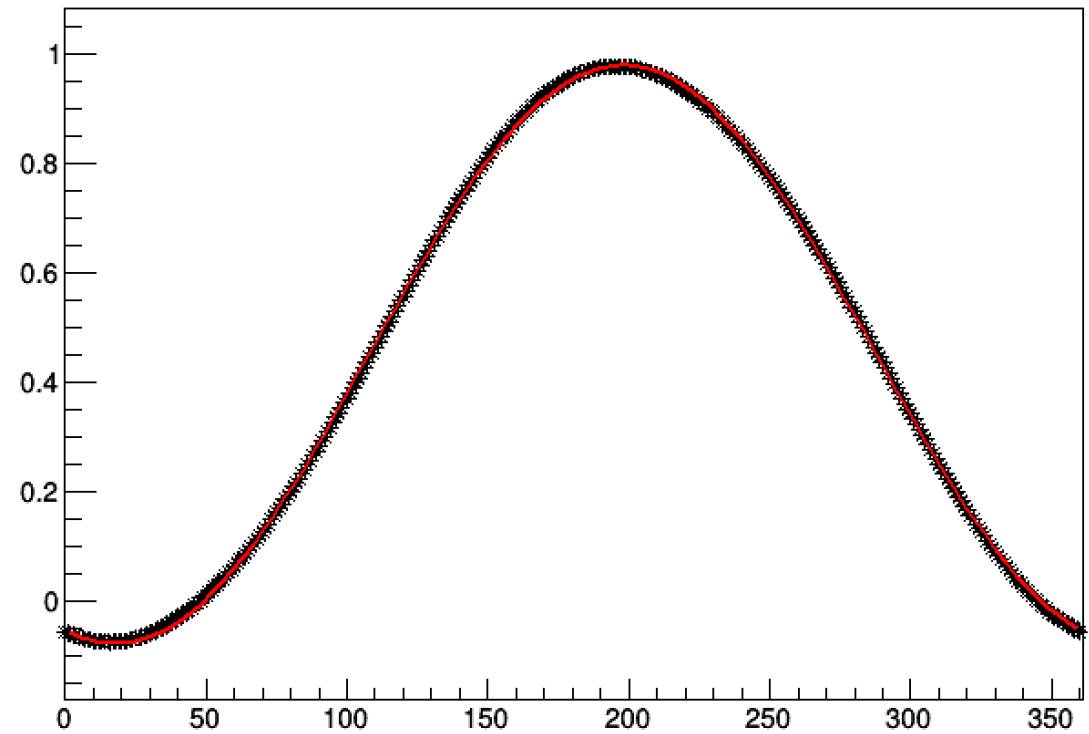
T (free prec. time) = 3.3 ms

$\sim (3/4)\pi$ flip

rot.frame



abs. sys.

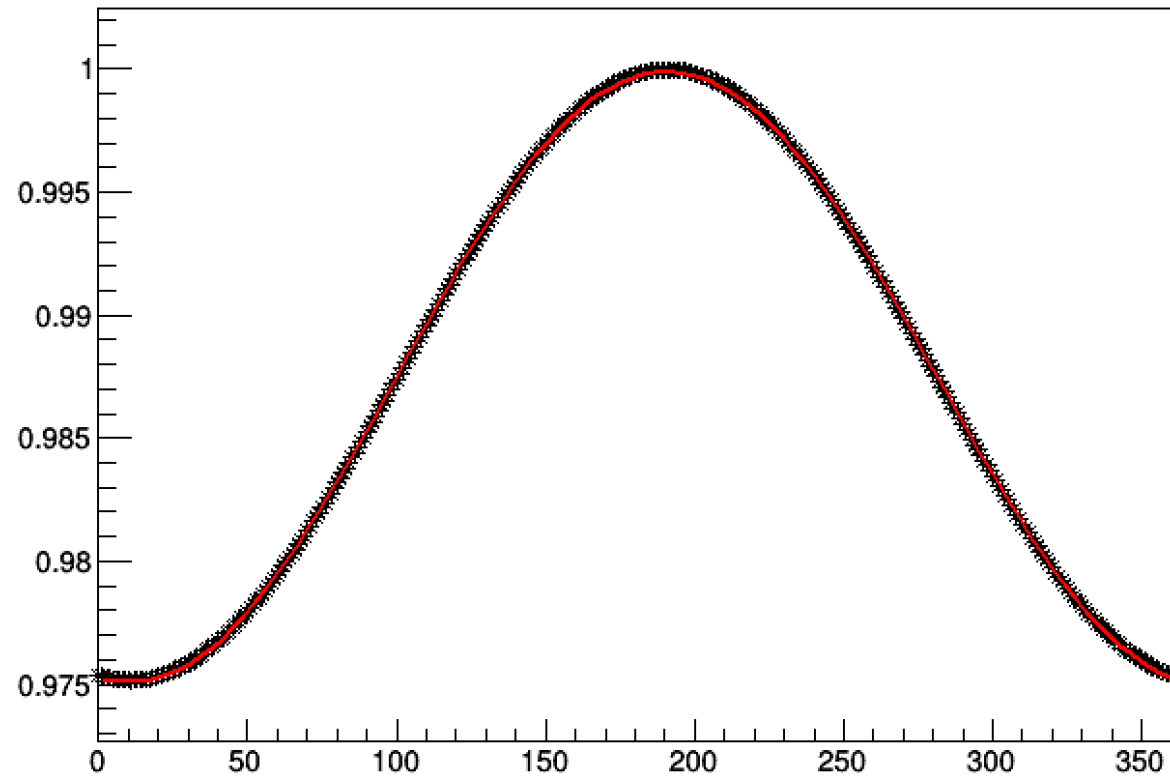


Comparison rot.frame VS abs.sys

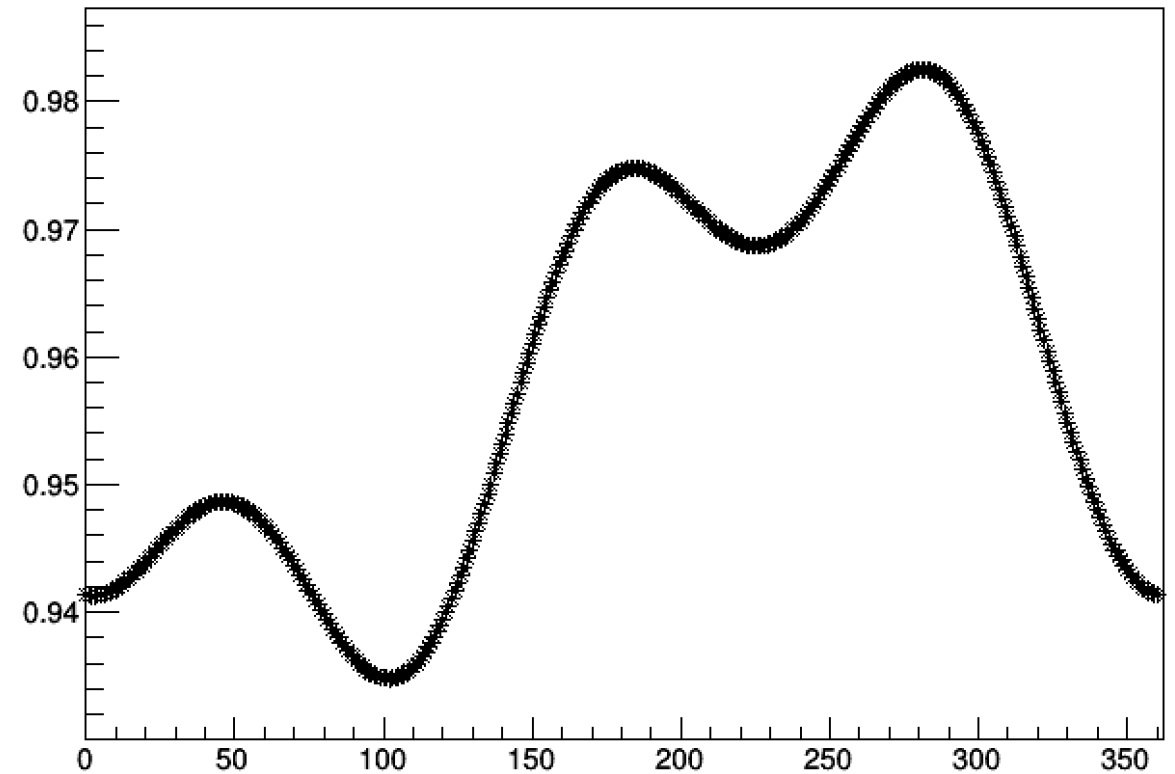
T (free prec. time) = 4.3 ms

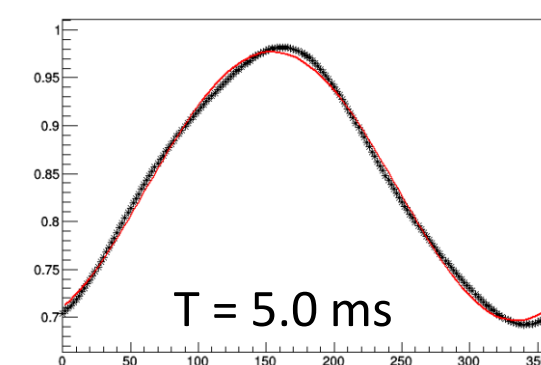
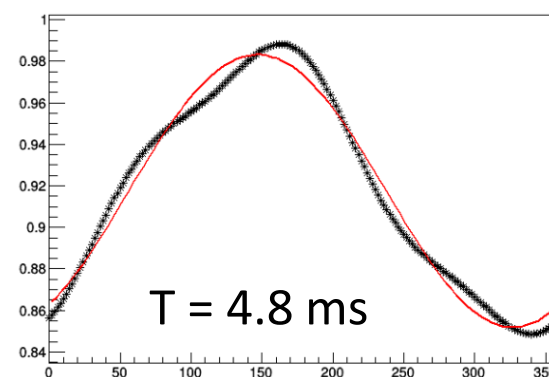
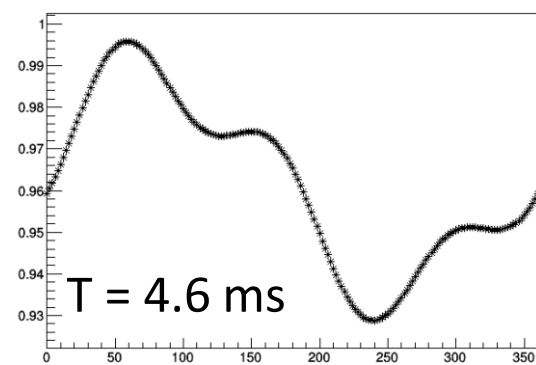
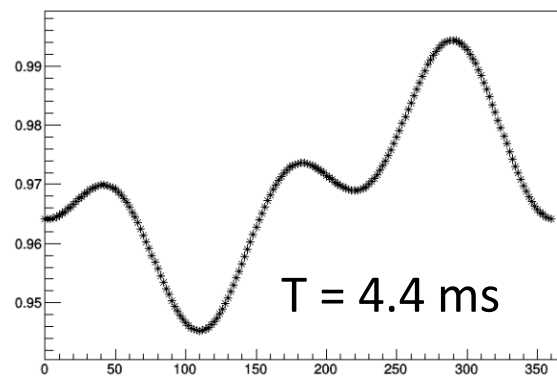
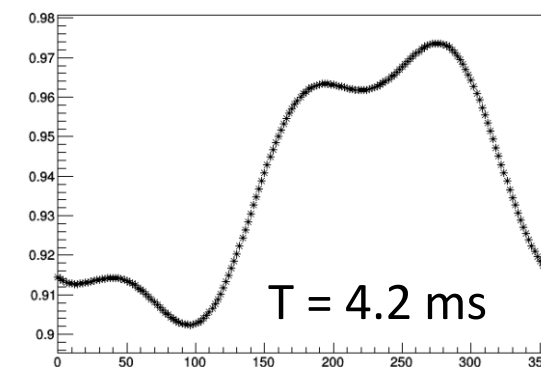
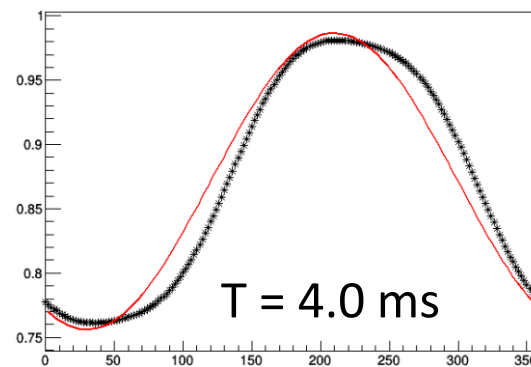
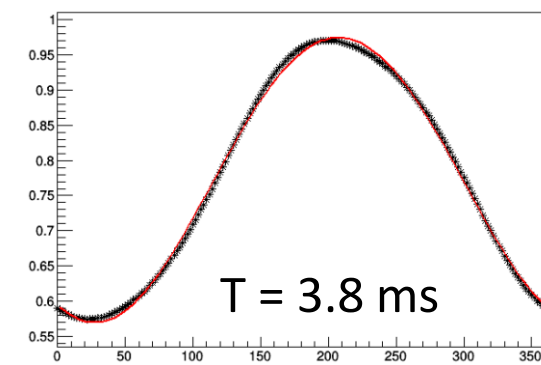
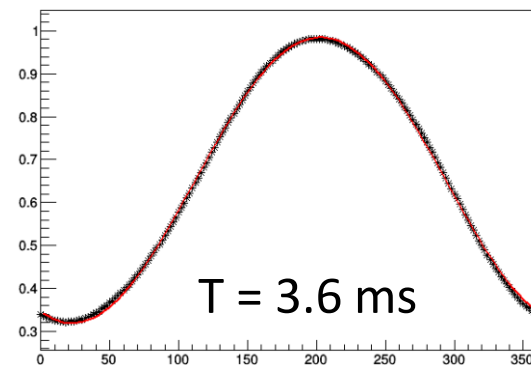
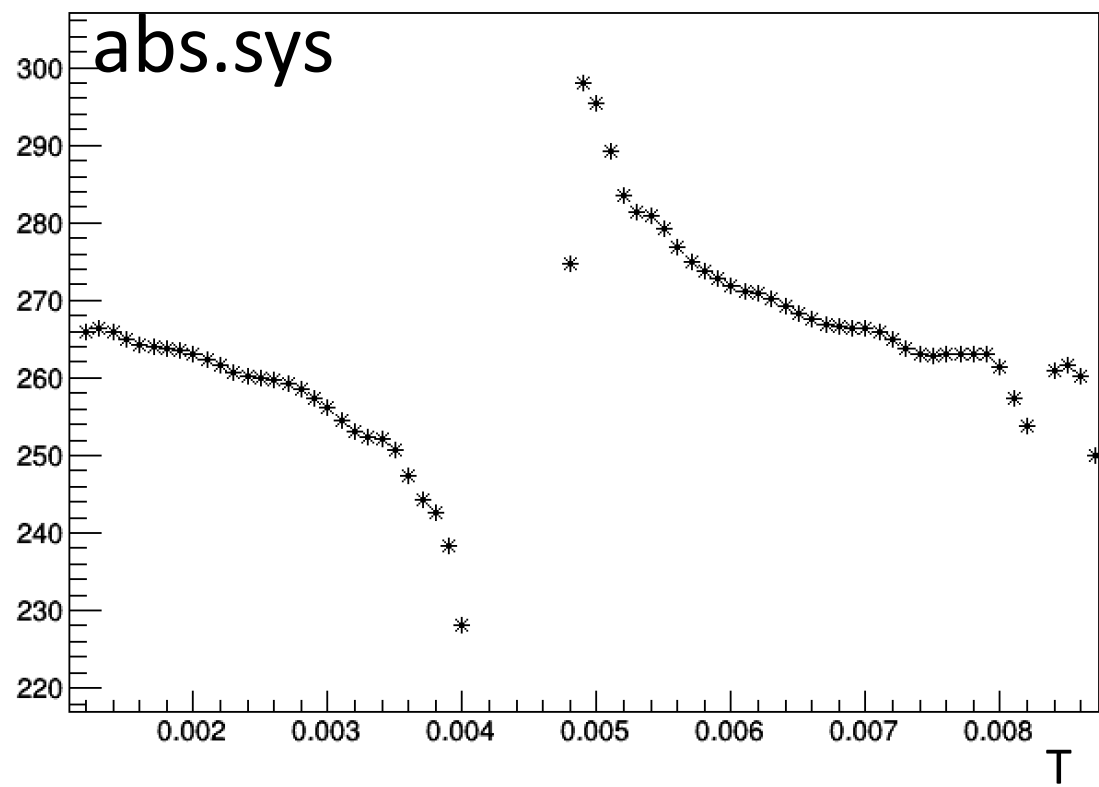
$< \approx \pi$ flip

rot.frame



abs. sys.





(phase-averaged results)

$l = 0.4$; //spin flipper length

$L = 2.6$; //distance between spin flippers

$B0_1 = 130.0e-6$;

$B0_2 = 130.0e-6$;

$B0_3 = 130.0e-6$;

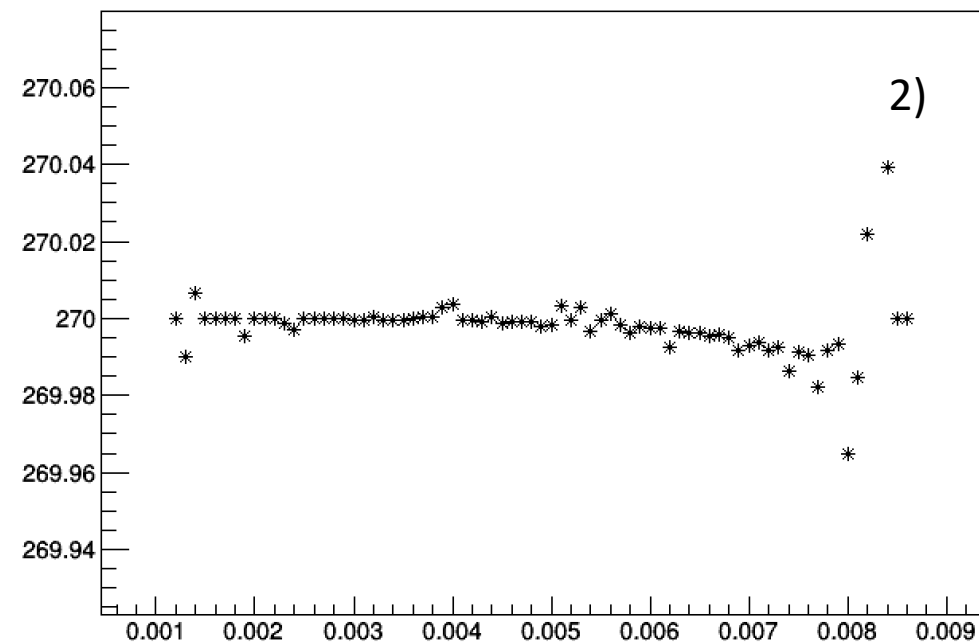
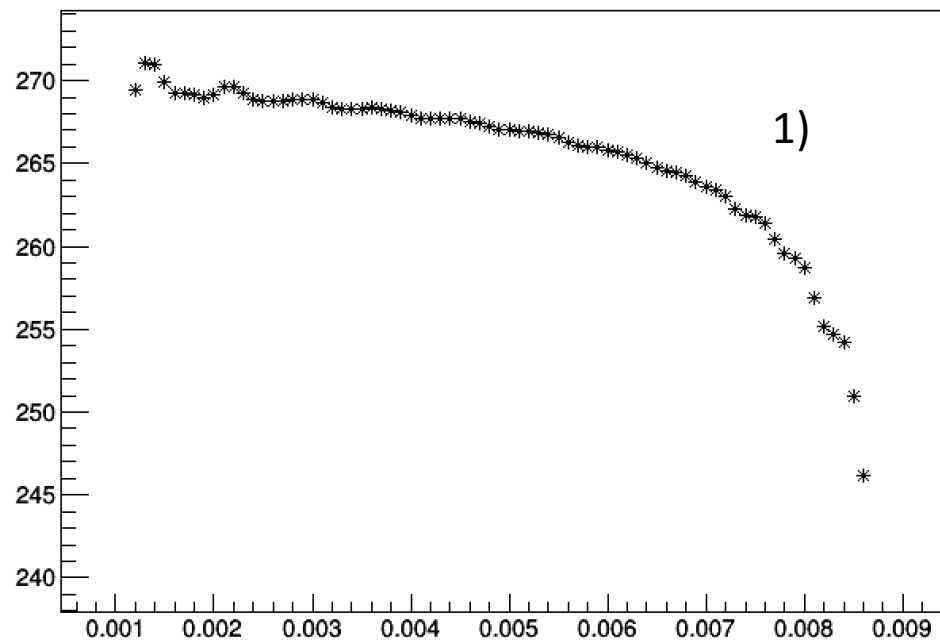
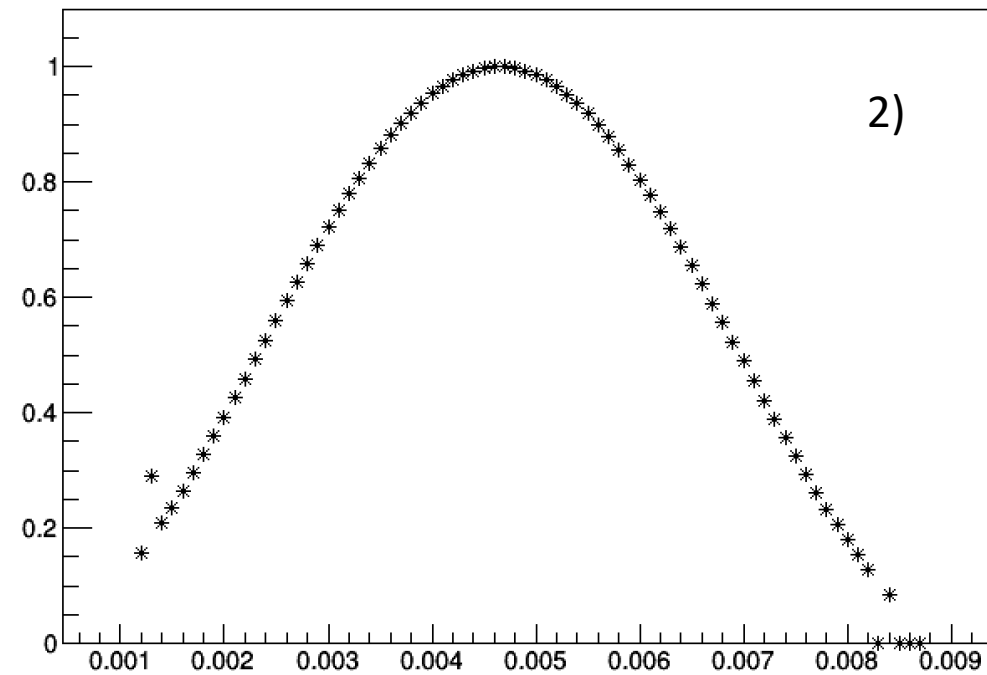
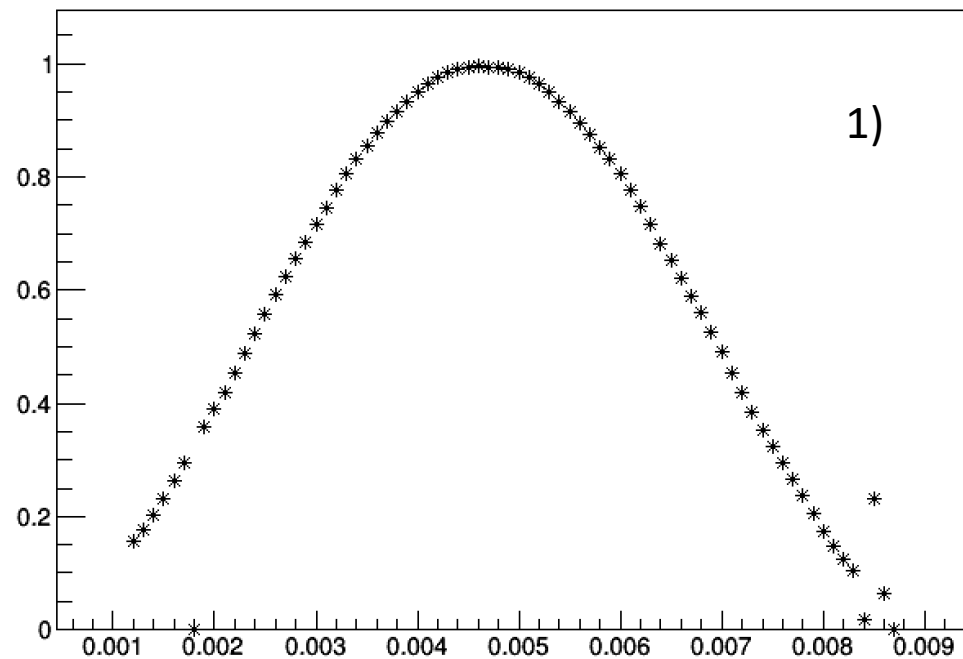
$B1_1 = 12.e-6$;

$B1_3 = 12.e-6$;;

$\omega = -\gamma B0_2$ (on resonance);

$$\begin{aligned} 1) \quad & B_x = 2B_1 \cos(\omega t) \\ & B_y = 0 \\ & B_z = B_0 \end{aligned}$$

$$\begin{aligned} 2) \quad & B_x = B_1 \cos(\omega t) \\ & B_y = B_1 \sin(\omega t) \\ & B_z = B_0 \end{aligned}$$



(phase-averaged results)

$l = 0.4$; //spin flipper length

$L = 2.6$; //distance between spin flippers

$B0_1 = 130.1e-6$;

$B0_2 = 130.0e-6$;

$B0_3 = 129.8e-6$;

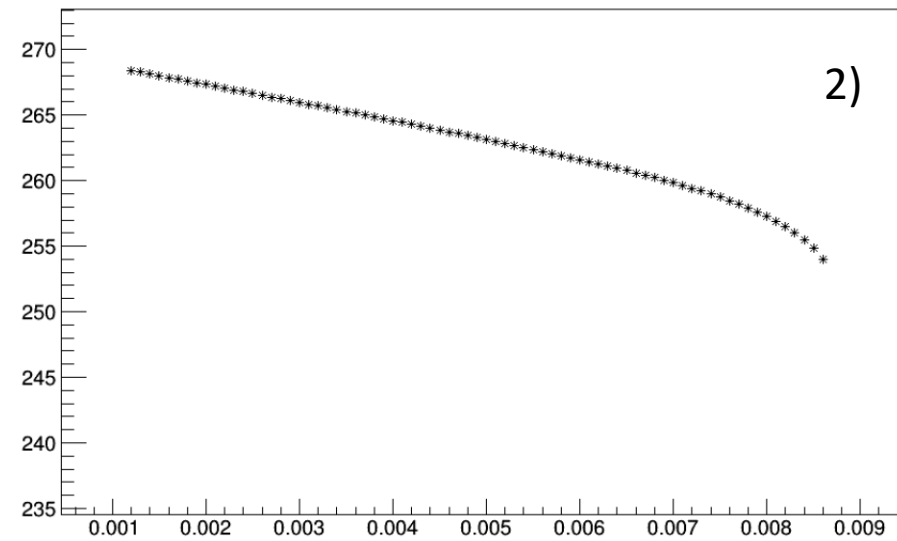
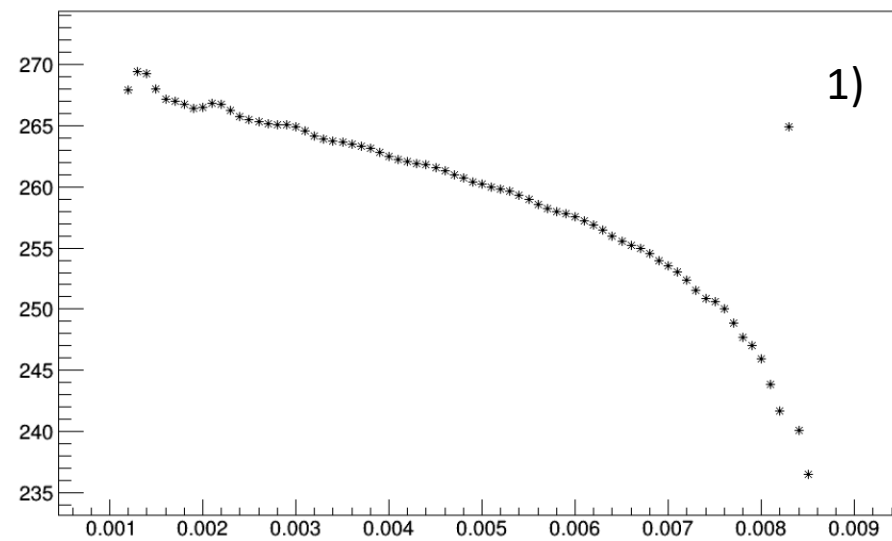
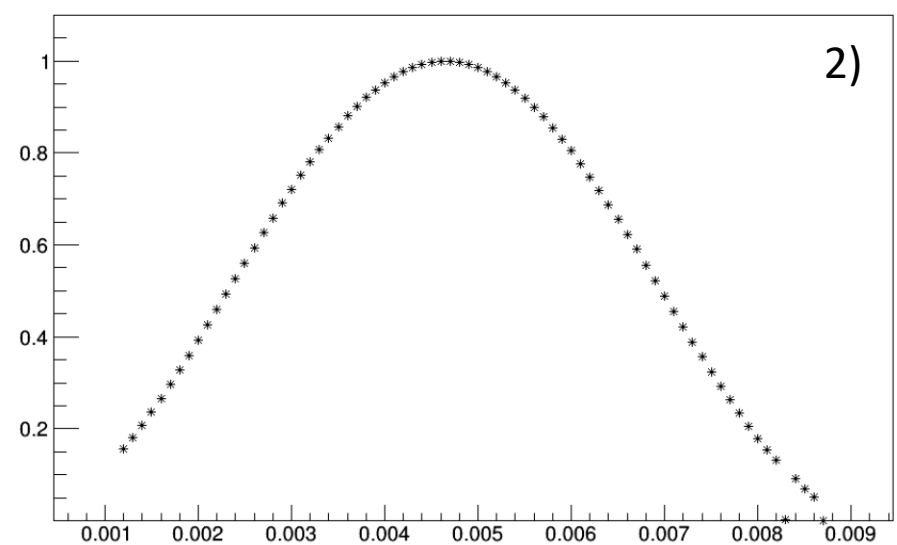
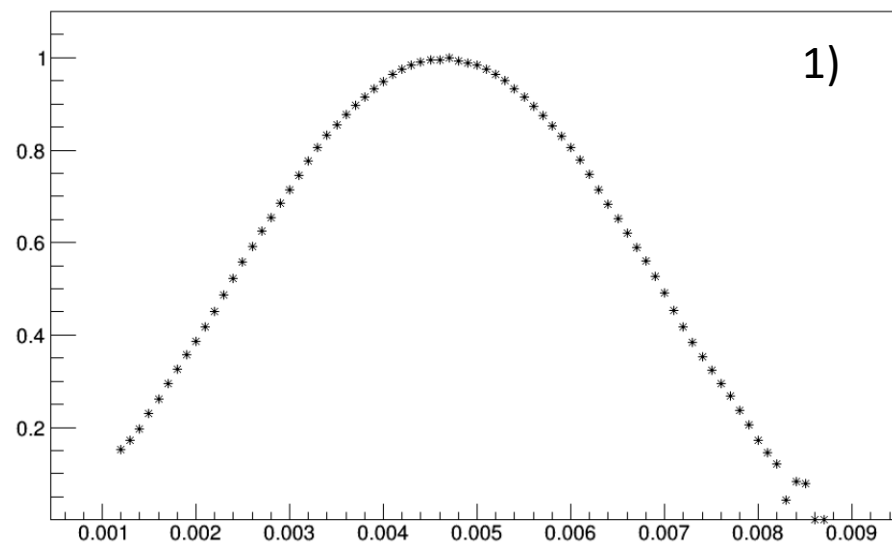
$B1_1 = 12.e-6$;

$B1_3 = 12.e-6$;;

$\omega = 3788 \cdot 2 \cdot \pi$;

$$\begin{aligned} 1) \quad & B_x = 2B_1 \cos(\omega t) \\ & B_y = 0 \\ & B_z = B_0 \end{aligned}$$

$$\begin{aligned} 2) \quad & B_x = B_1 \cos(\omega t) \\ & B_y = B_1 \sin(\omega t) \\ & B_z = B_0 \end{aligned}$$



Try to eliminate the Bloch-Siegert frequency shift

$$B0_1 = 130.0e-6;$$

$$B0_2 = 130.0e-6;$$

$$B0_3 = 130.0e-6;$$

$$B1_1 = 12.e-6;$$

$$B1_3 = 12.e-6;;$$

$$\omega = -\gamma B0_2;$$

1) φ_{RDM1} and φ_{RDM2} are random between 0 and 2π (300exp)

$$B_x(SF1) = 2B_1 \cos(\omega t + \varphi_{RDM1}) + 2B_1 \cos(\sqrt{5}\omega t + \varphi_{RDM2})$$

$$B_y(SF1\&2) = 0$$

$$B_z(SF1\&2) = B_0$$

$$B_x(SF2) = 2B_1 \cos(\omega t + \varphi_{RDM1} + \varphi_{SF}) + 2B_1 \cos(\sqrt{5}\omega t + \varphi_{RDM2} + \varphi_{SF})$$

2) φ_{RDM} is random between 0 and 2π (300exp)

$$B_x(SF1) = 2B_1 \cos(\omega t + \varphi_{RDM}) + 2 * \sqrt{\frac{3}{4}} B_1 \cos(2\omega t + 2\varphi_{RDM})$$

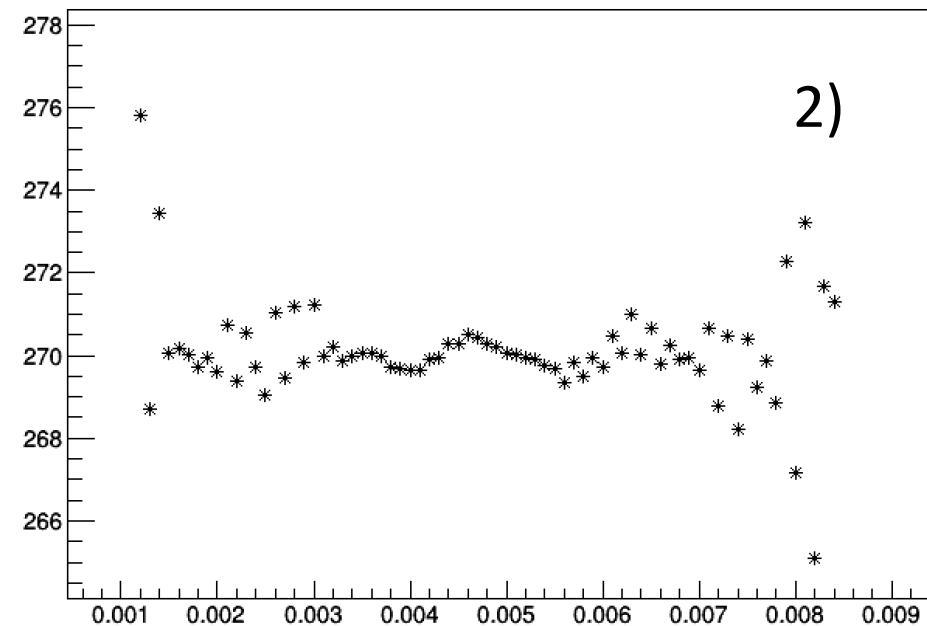
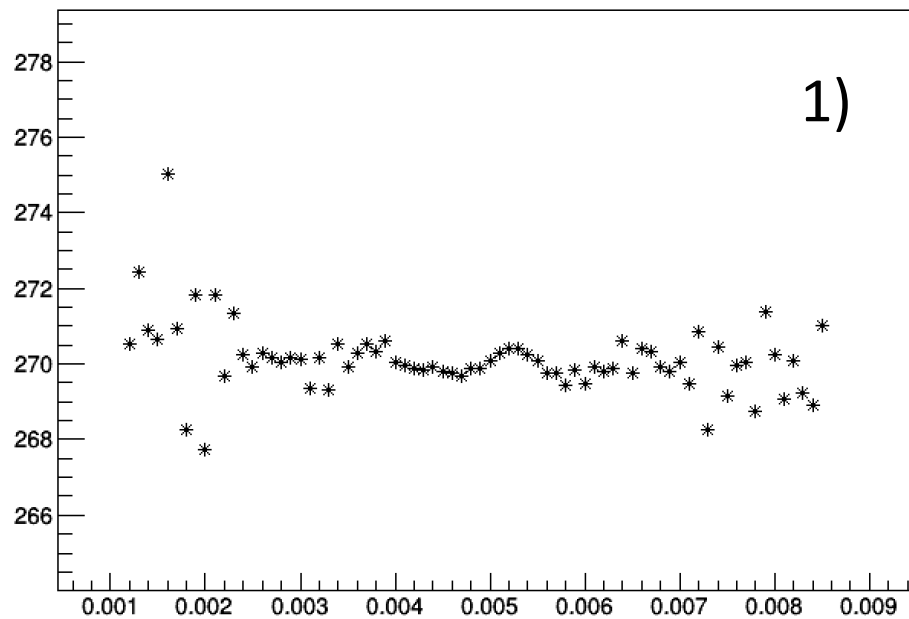
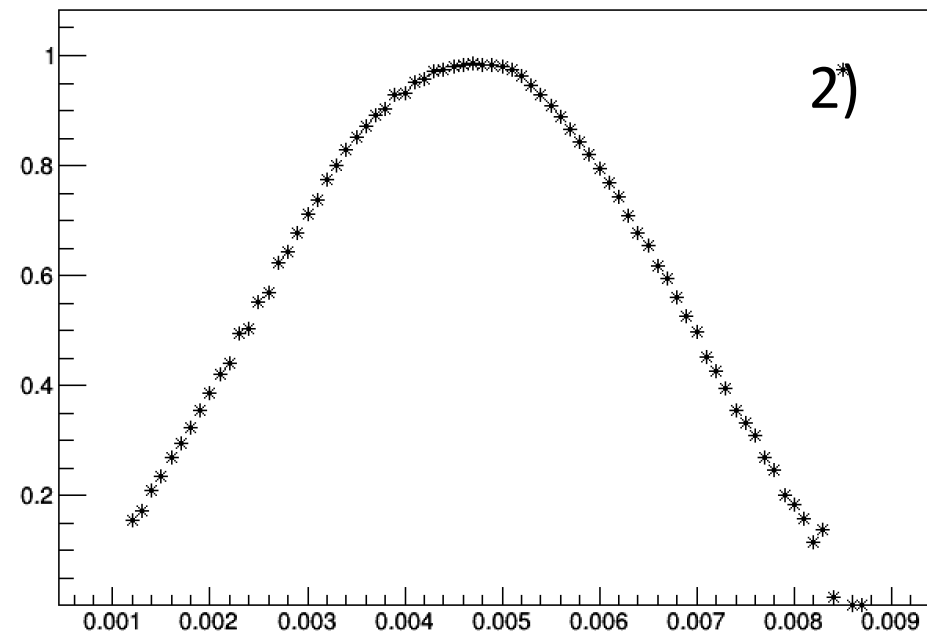
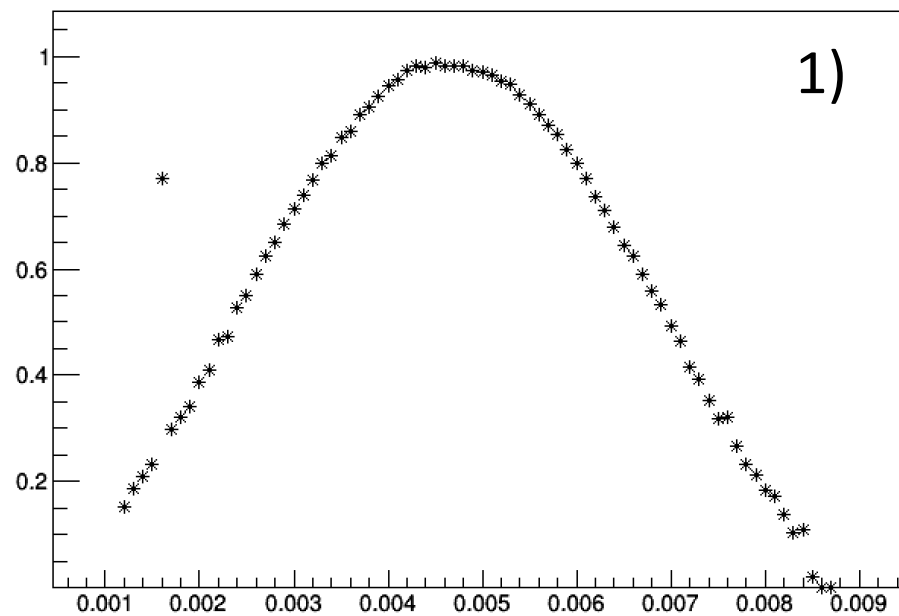
$$B_y(SF1\&2) = 0$$

$$B_z(SF1\&2) = B_0$$

$$B_x(SF2) = 2B_1 \cos(\omega t + \varphi_{RDM} + \varphi_{SF}) + 2 * \sqrt{\frac{3}{4}} B_1 \cos(2\omega t + 2\varphi_{RDM} + \varphi_{SF})$$

NB:

$$\omega_{BS} = \frac{(\gamma B_1)^2}{2(\omega_{RF} + \omega_{B0})}$$



Modulated signal in abs. sys.

D

SF
1

Free Prec
2

SF
3

D = 1.784; //distance chopper SF1

l = 0.4; //spin flipper length

L = 2.6; //distance between spin flippers

B0_1 = 130.1e-6;

B1 = 25.e-6;

B0_2 = 130.0e-6;

omega = 3788.*2.*pi;

B0_3 = 129.8e-6;

$$B_x(SF_1) = -\gamma * 2 * B1 * \left(\frac{t_1}{t}\right)^{p_1} \cos(\omega t)$$

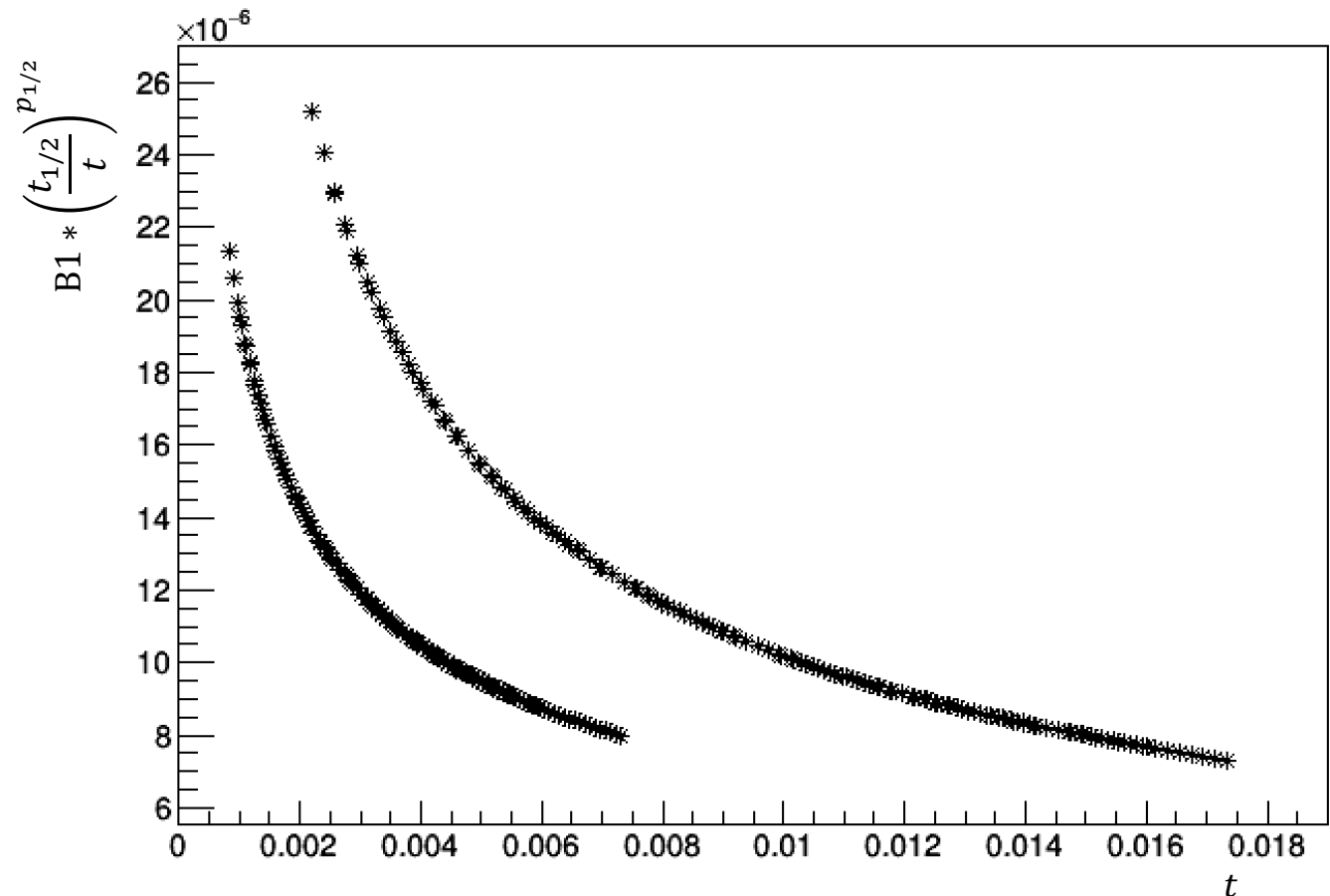
$$B_x(SF_2) = -\gamma * 2 * B1 * \left(\frac{t_2}{t}\right)^{p_2} \cos(\omega t + \varphi_{SF})$$

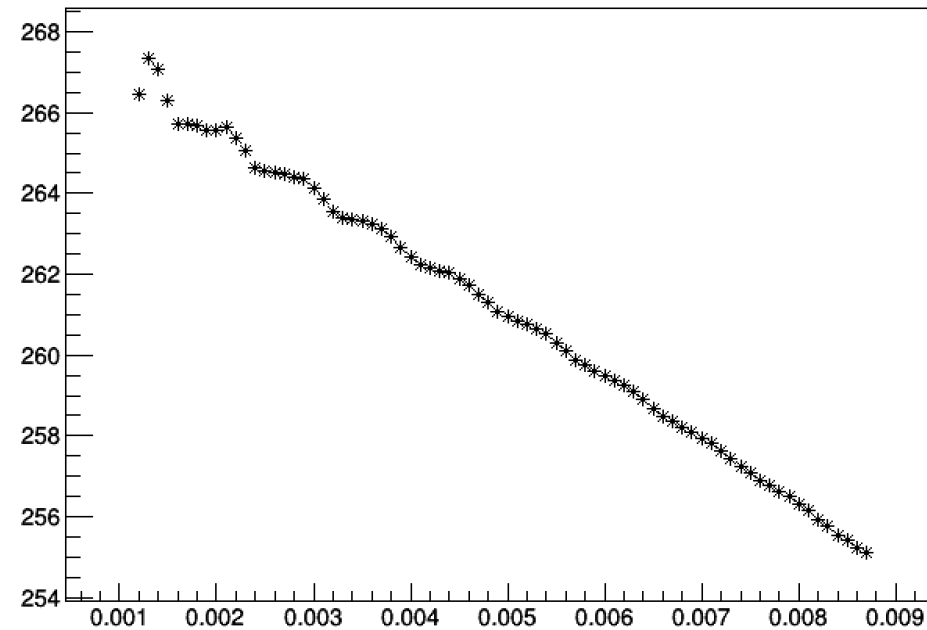
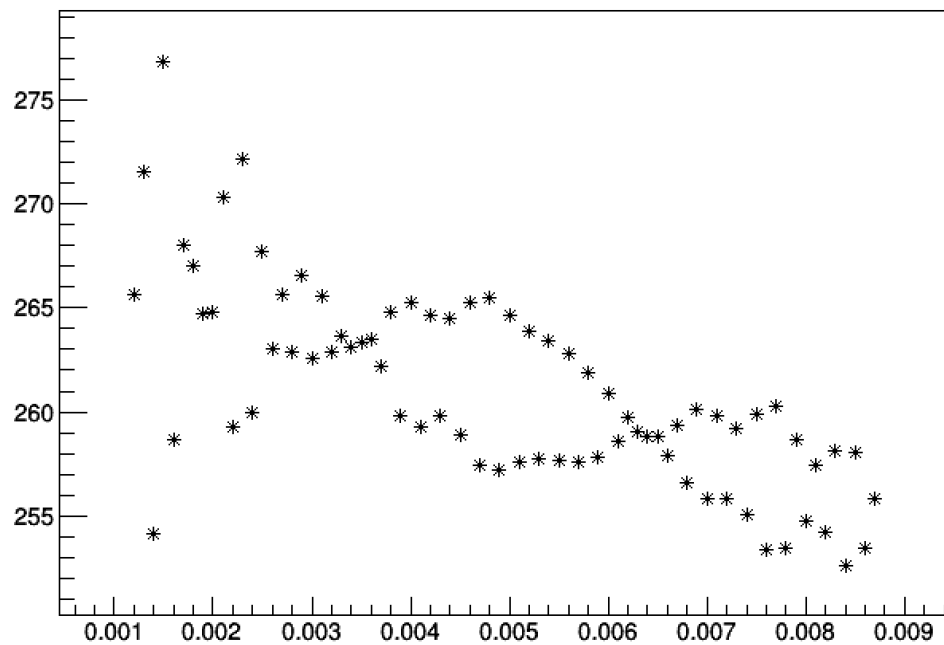
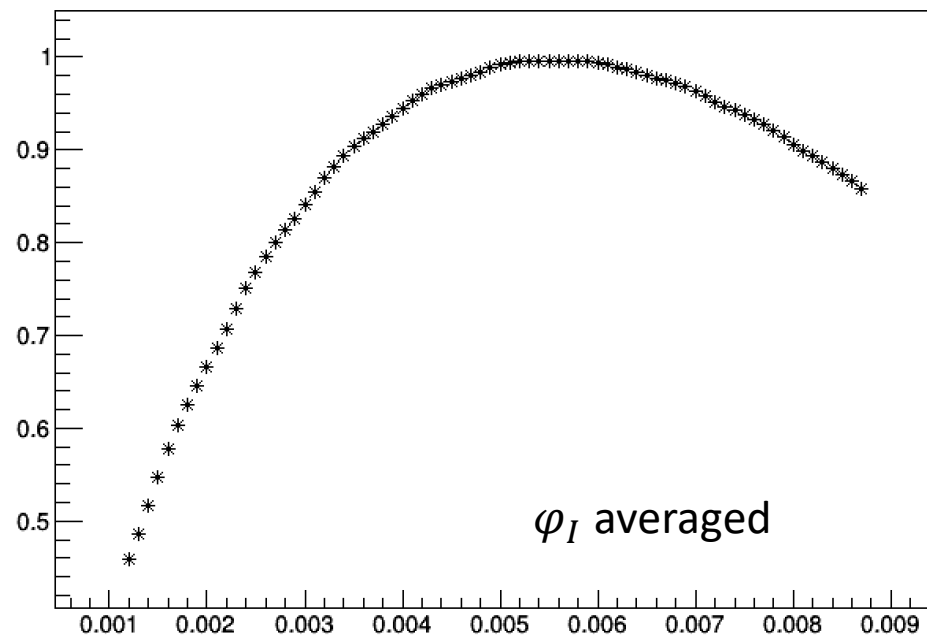
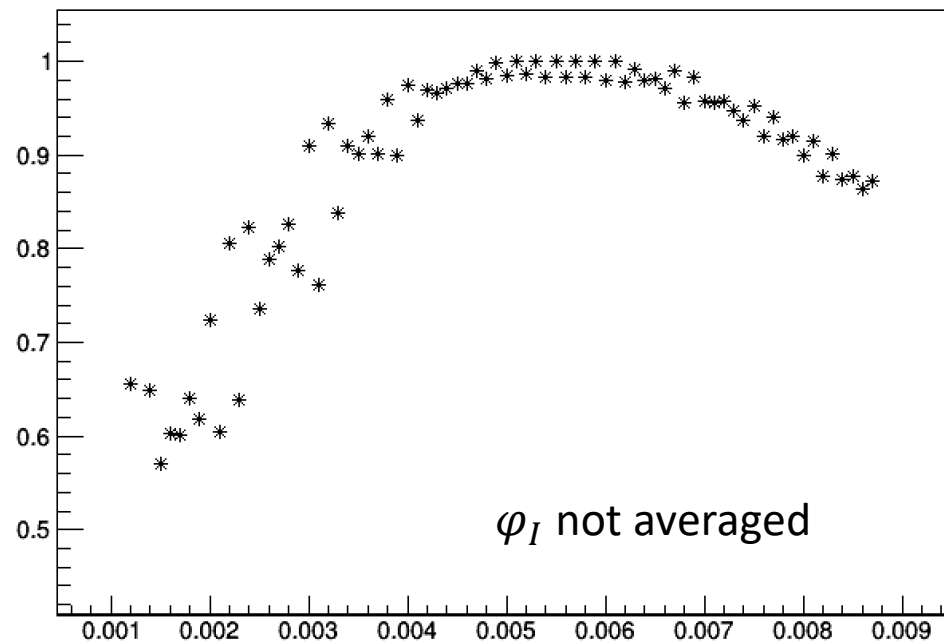
with $t_1 = 0.58 \text{ ms}$

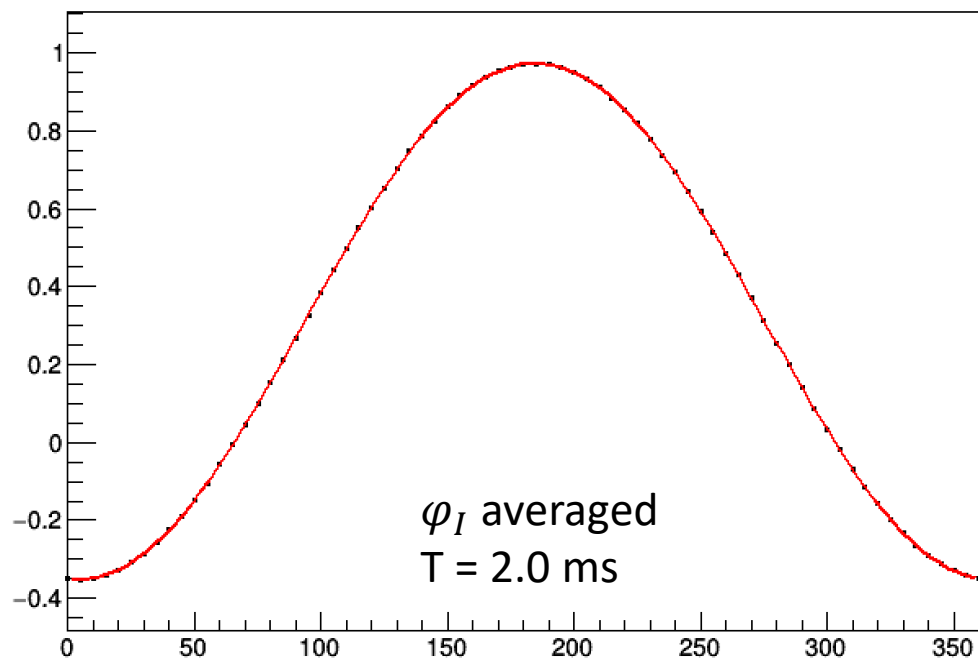
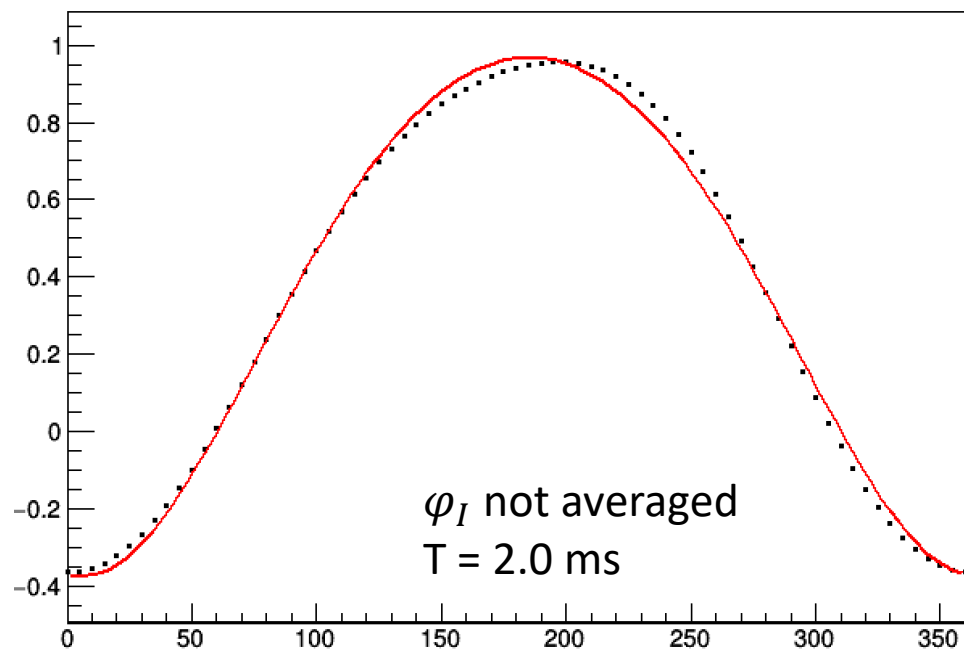
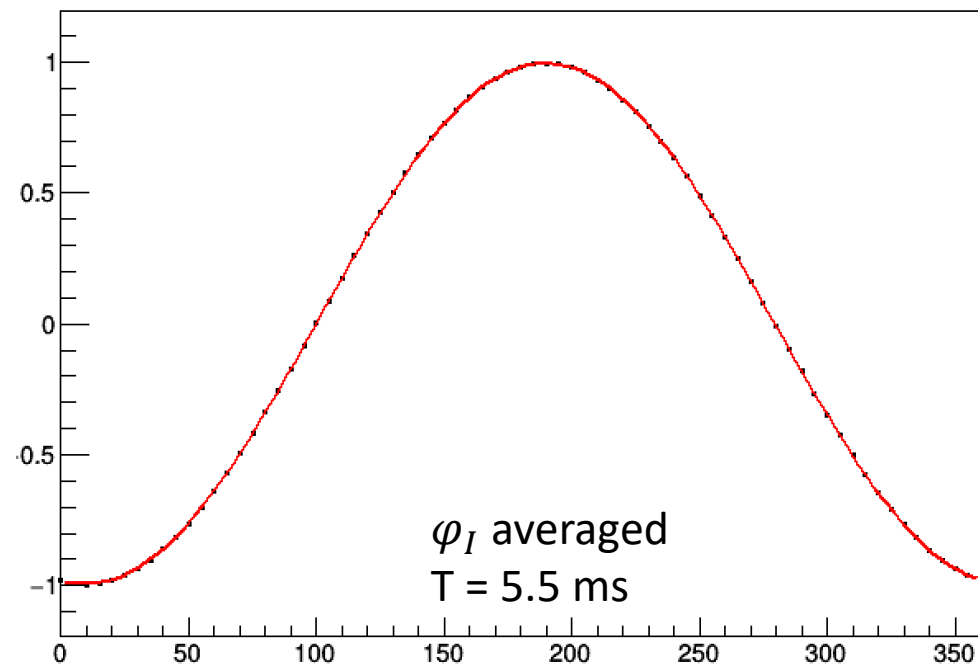
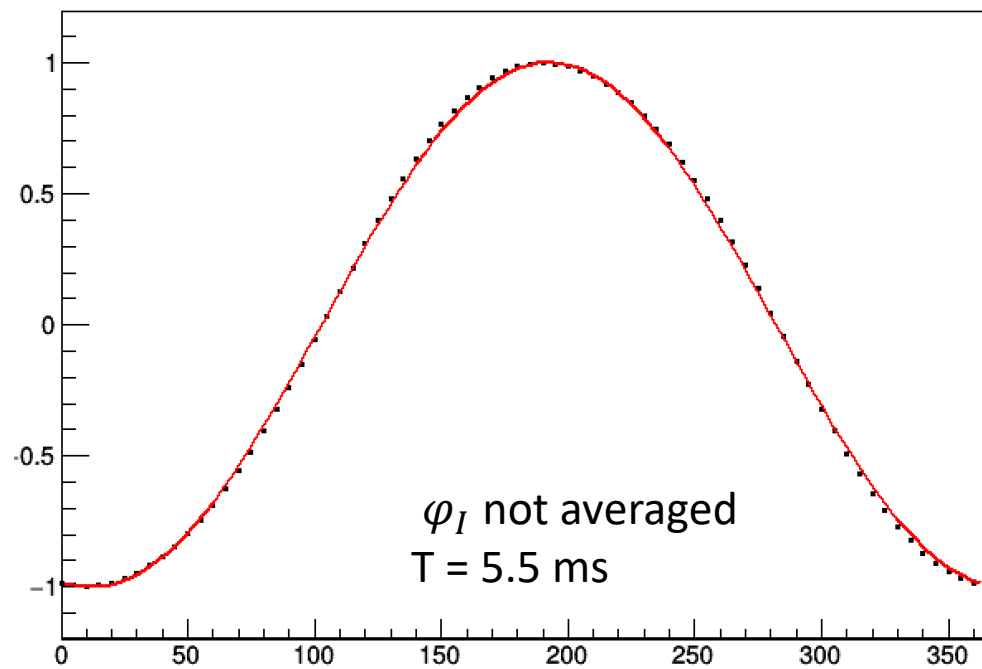
$p_1 = 0.45$

$t_2 = 2.24 \text{ ms}$

$p_2 = 0.6$







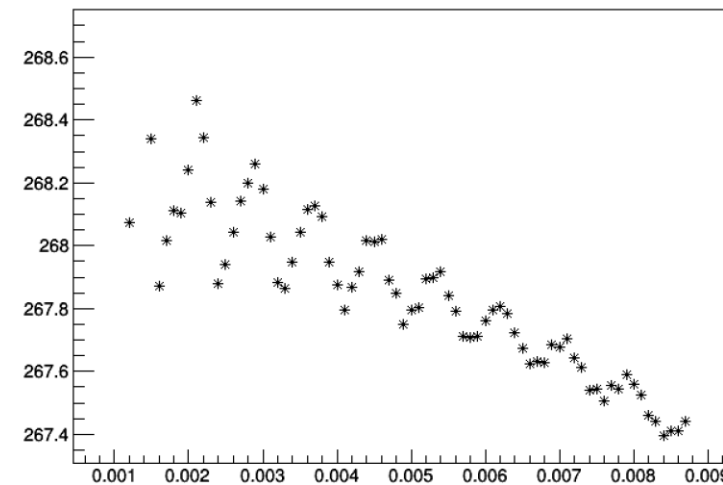
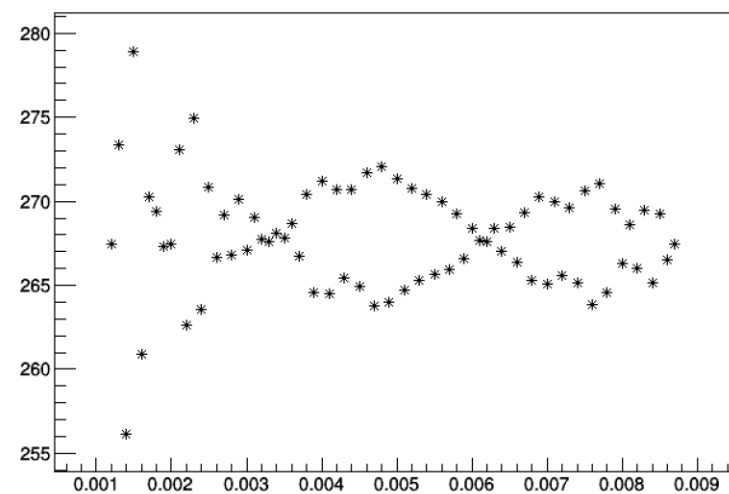
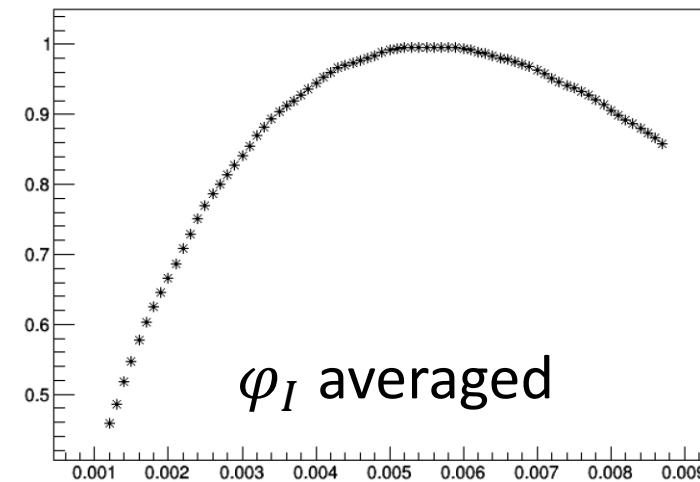
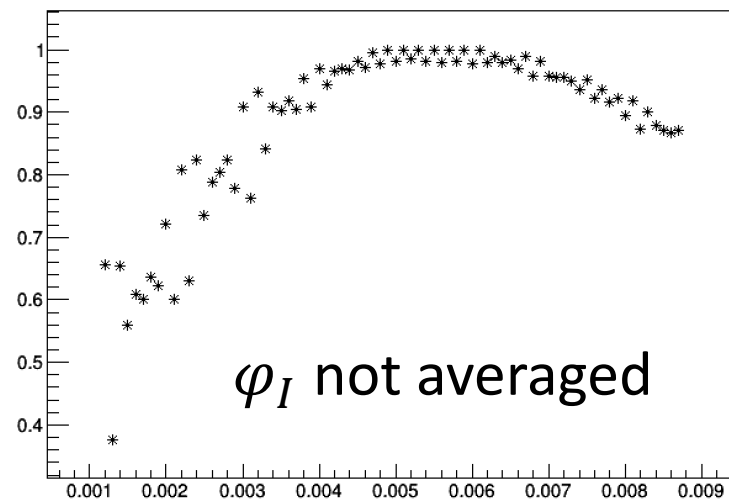
B0_1 = 130.0e-6;

B0_2 = 130.0e-6;

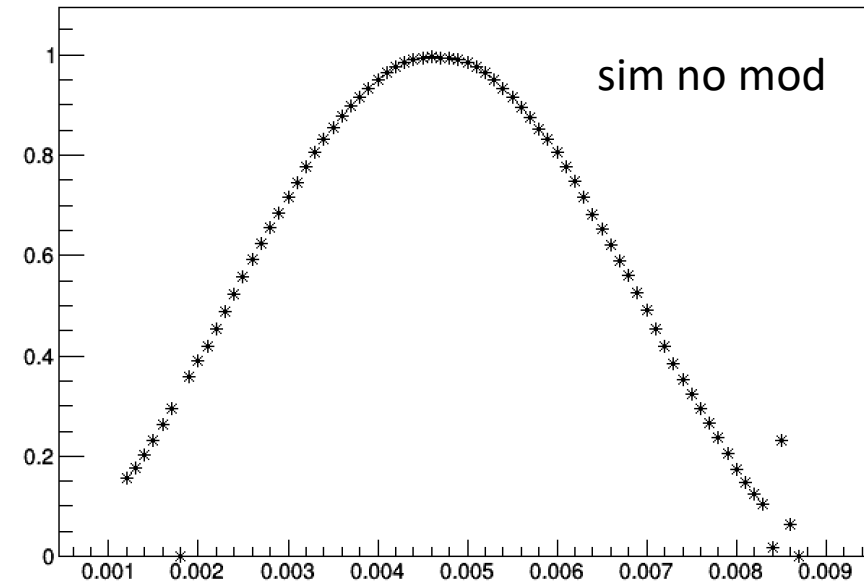
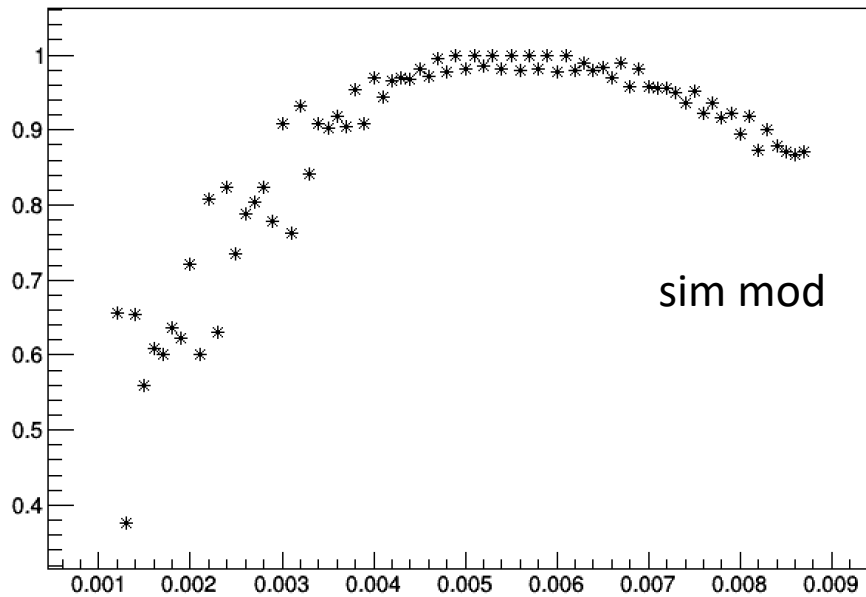
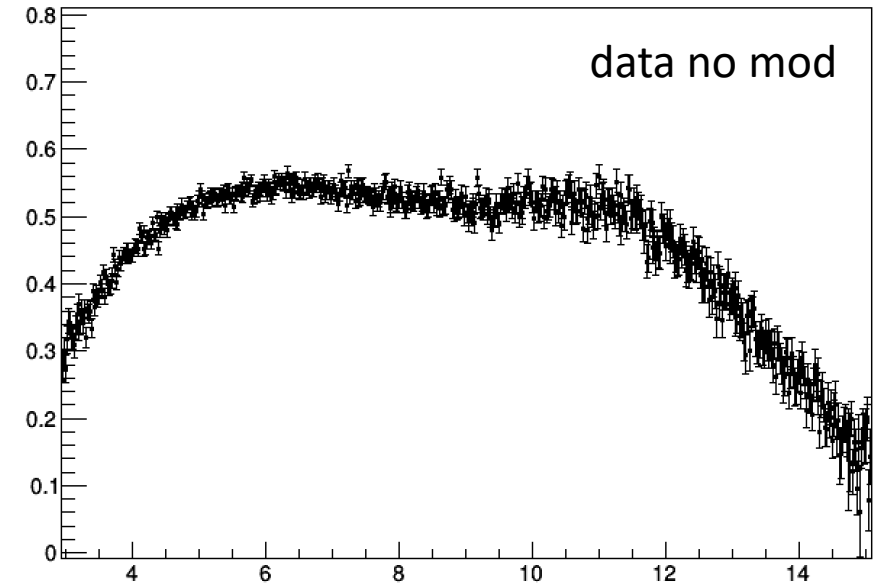
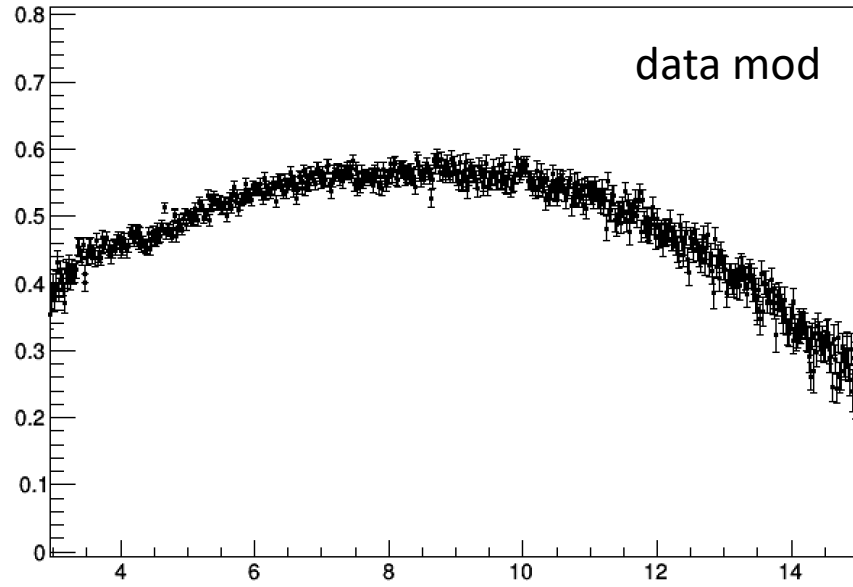
B0_3 = 130.0e-6;

B1 = 25.e-6;

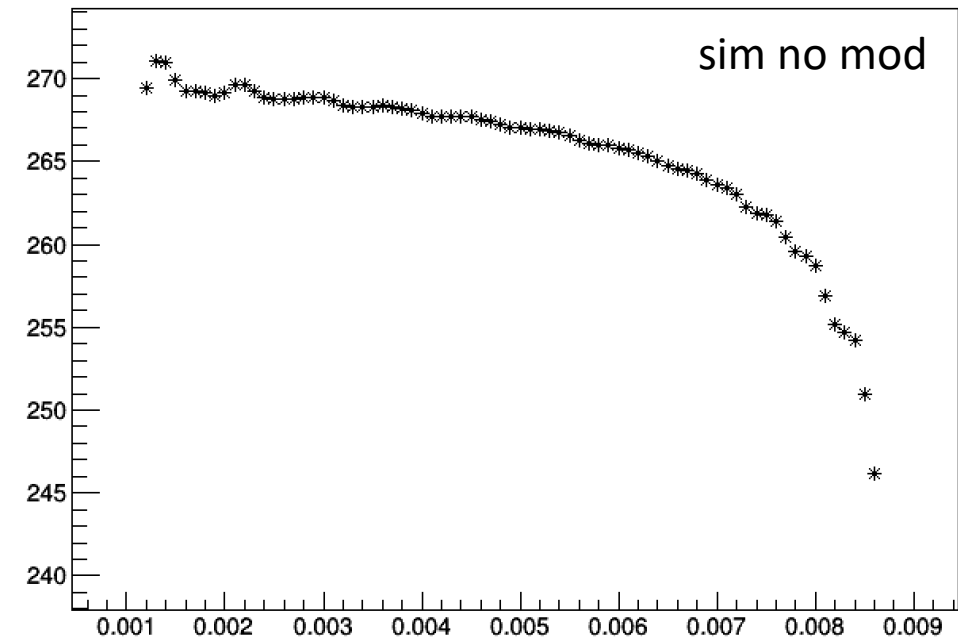
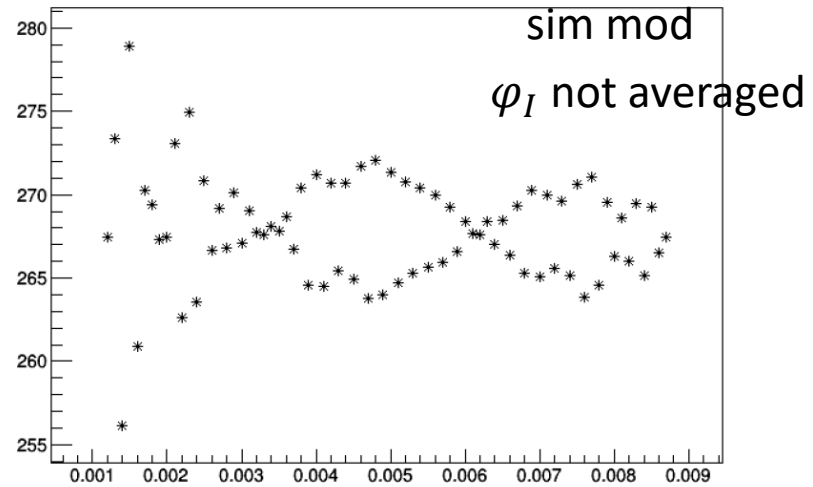
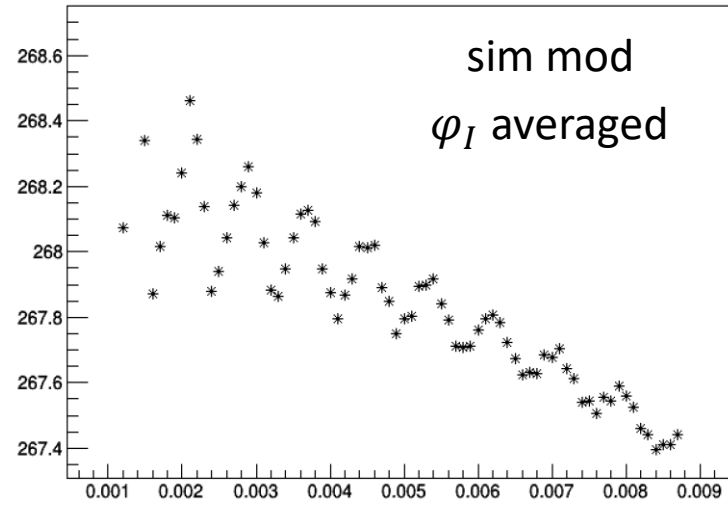
omega = - γ B0_2;



Amplitude comparison



Phase comparison (on resonance)



Summary

- “tangent effect” -> in the regions where amplitude is small (close to $\pi+\pi$ flip) the asymmetry vs phase shift plot is altered (phase evaluation not easy). The effect is not described in the rotating frame approx.
- Chi2 alterations for the mod. signal seems due to non-random initial phase
- Bloch-Siegert effect can be an issue (there are ways to reduce/eliminate it)
- Pros and contra in the mod VS no mod comparison. To be tested against real data when a more homogeneous B field will be available

Plans

- Validate the tool with real data if available (ex. investigate BS shift with Ivo's setup)
- (make it more realistic: TOF smearing)
- (add systematics)

Hint from Zach: is it really random the initial phase?

Ex.: SF frequency = 3800 Hz, Chopper frequency = 15 Hz, ratio is 253.333 $\rightarrow$ initial phase may assume only 3 values!

B0_1 = 130.0e-6;
B0_2 = 130.0e-6;
B0_3 = 130.0e-6;

B1_1 = 12.e-6;
B1_3 = 12.e-6;;

$\omega = -\gamma B0_2$;
 $B_x = 2B_1 \cos(\omega t)$

